

# EXPERIMENTAL AND MODELLING STUDY OF THE EFFECT OF DIFFUSIONAL LIMITATIONS ON THE NH<sub>3</sub> SCR ACTIVITY

Maria Pia Ruggeri, Isabella Nova, Enrico Tronconi

# Outline

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## Introduction

↳ mass transfer phenomena in SCR honeycomb monolith catalysts

## Kinetic data collected over powdered catalyst

↳ diffusion-free analysis

## Validation runs over monolith catalyst

↳ assessment of mass transfer resistances from powdered vs. monolith data

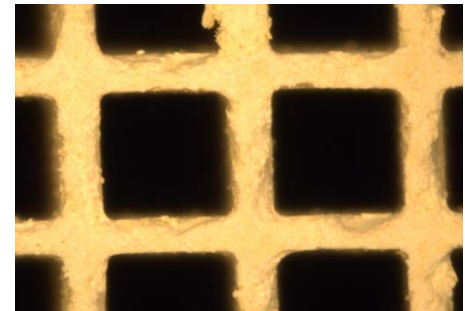
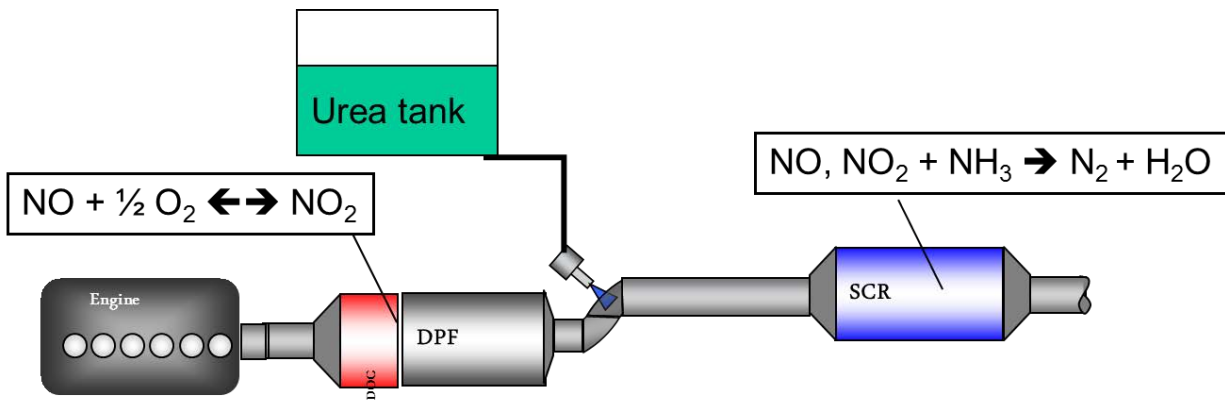
## Model simulations

↳ analysis of internal and external diffusional limitations

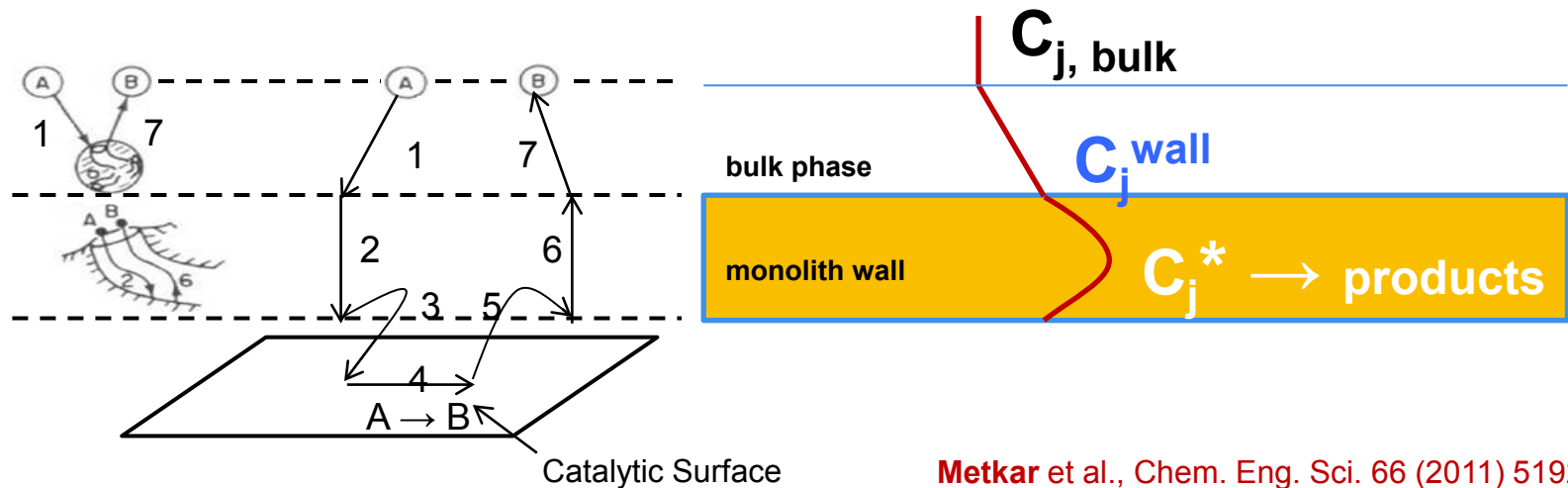
## Conclusions

# Introduction

Development of chemically consistent mathematical models of SCR monolithic converters equipped with V-based extruded or Fe- and Cu-promoted washcoated monoliths for Diesel vehicles.



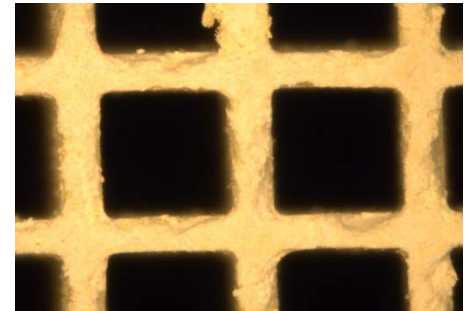
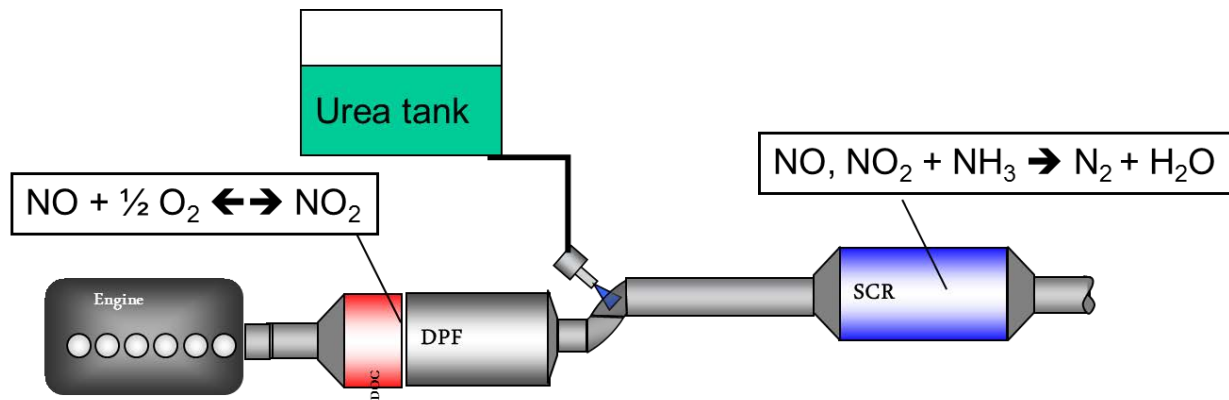
Source: 1st MinNOx conf., 2/2007



Metkar et al., Chem. Eng. Sci. 66 (2011) 5192  
 Nova et al., Ind. Eng. Chem. Res. 50 (2011) 299

# Introduction

Development of chemically consistent mathematical models of SCR monolithic converters equipped with V-based extruded or Fe- and Cu-promoted washcoated monoliths for Diesel vehicles.



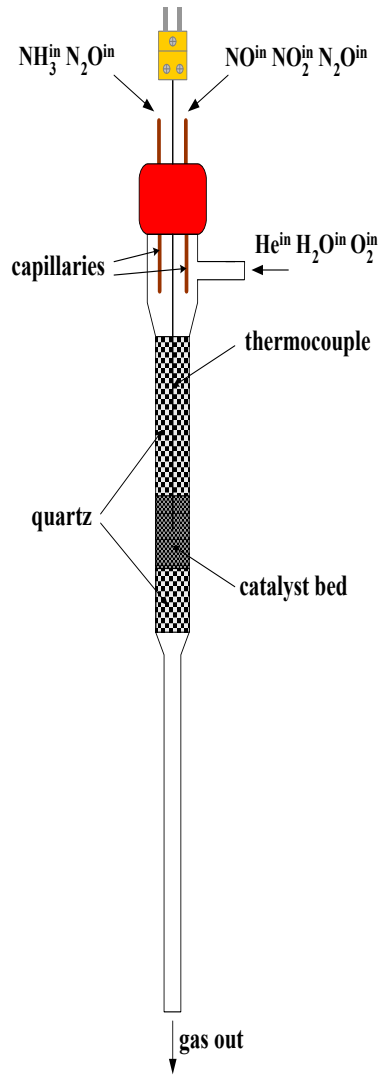
Source: 1st MinNOx conf., 2/2007

## Aim of the work:

quantification of the intra- and interphase diffusional limitations in V-based extruded monolith SCR catalysts

# **Kinetic data collected over powdered catalyst ... diffusion-free analysis**

# Micro-reactor experiments



average particle size = 90  $\mu\text{m}$

80 mg of catalyst diluted with cordierite up to 160 mg

catalyst bed height = 1 cm

## Experimental conditions:

GHSV = 30'000-70'000  $\text{h}^{-1}$

$\text{H}_2\text{O}$  = 8 %;  $\text{O}_2$  = 2-8 %

$\text{NH}_3$  = 500-1000 ppm

$\text{NO}$  = 0-500 ppm

$\text{NO}_2$  = 0-500 ppm

$\text{NO}/\text{NO}_2$  = 0-1

$T$  = 150-550 $^\circ\text{C}$



## Hypothesis:

1D heterogeneous plug flow dynamic model

isothermal, isobaric

$$\text{Gaseous phase: } \varepsilon \frac{\partial C_i}{\partial t} = -v \frac{\partial C_i}{\partial z} - (1 - \varepsilon) R_i \quad i = \begin{cases} \text{NH}_3 \\ \text{NO} \\ \text{NO}_2 \\ \text{N}_2\text{O} \end{cases}$$

$$\text{Adsorbed phase: } \Omega_j \frac{\partial \theta_j}{\partial t} = -R_j \quad j = \text{NH}_3^*$$

$$R_{i-j} = \left[ \text{mol} / (\text{m}_{\text{cat}}^3 \cdot \text{s}) \right]$$

# V-based catalyst: SCR kinetics

## Ammonia adsorption/desorption



## Ammonia oxidation



## Standard-SCR



## Fast-SCR



## Nitrates formation



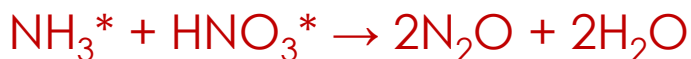
## Nitrates adsorption/desorption



## NO<sub>2</sub>-SCR



## N<sub>2</sub>O formation



$$r_{ads} = k_{ads} C_{\text{NH}_3} (1 - \theta_{\text{NH}_3} - \theta_{\text{HNO}_3})$$

$$r_{des} = \exp\left[k_{des} - \frac{E_{des}}{RT}\right] \theta_{\text{NH}_3}$$

$$r_{ox} = \exp\left(k_{ox} - \frac{E_{ox}}{RT}\right) \theta_{\text{NH}_3} \left(\frac{p_{\text{O}_2}}{0.02}\right)^{0.275}$$

$$r_{\text{NO}} = \frac{\exp\left(k'_{\text{NO}} - \frac{E_{\text{NO}}}{RT}\right) C_{\text{NO}} \theta_{\text{NH}_3}}{\left(1 + K_{\text{NH}_3} \frac{\theta_{\text{NH}_3}}{1 - \theta_{\text{NH}_3}}\right) \left(1 + k_{\text{O}_2} \frac{C_{\text{NO}} \theta_{\text{NH}_3}}{p_{\text{O}_2}^{1/4}}\right)}$$

$$r_{fst} = \exp\left(k_{fst} - \frac{E_{fst}}{RT}\right) \theta_{\text{NH}_3} \theta_{\text{HNO}_3} C_{\text{NO}}$$

$$r_{amm} = \frac{k_{amm} C_{\text{NO}_2}^2 \theta_{\text{NH}_3} (1 - \theta_{\text{NH}_3} - \theta_{\text{HNO}_3})}{\theta_{\text{HNO}_3}}$$

$$r_{nit} = \beta \theta_{\text{HNO}_3} - k_{nit} C_{\text{HNO}_3} (1 - \theta_{\text{NH}_3} - \theta_{\text{HNO}_3})$$

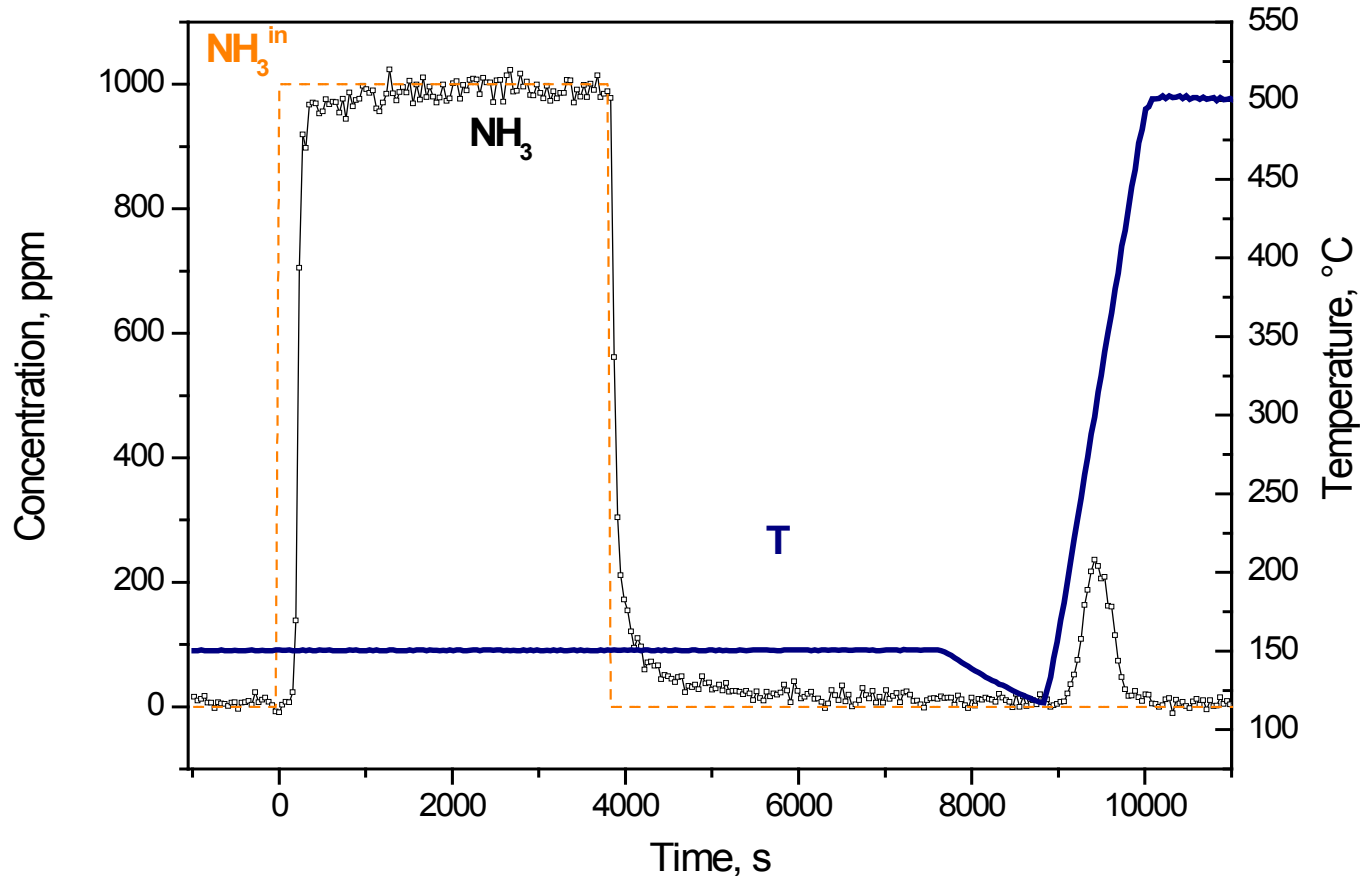
$$r_{\text{NO}_2} = \exp\left(k_{\text{NO}_2} - \frac{E_{\text{NO}_2}}{RT}\right) \theta_{\text{NH}_3} C_{\text{NO}_2}$$

$$r_{\text{N}_2\text{O}} = \exp\left(k_{\text{N}_2\text{O}} - \frac{E_{\text{N}_2\text{O}}}{RT}\right) \theta_{\text{NH}_3} \theta_{\text{HNO}_3}$$



# Podwered catalyst: $\text{NH}_3$ adsorption/desorption

Symbols = experimental



## Experimental conditions:

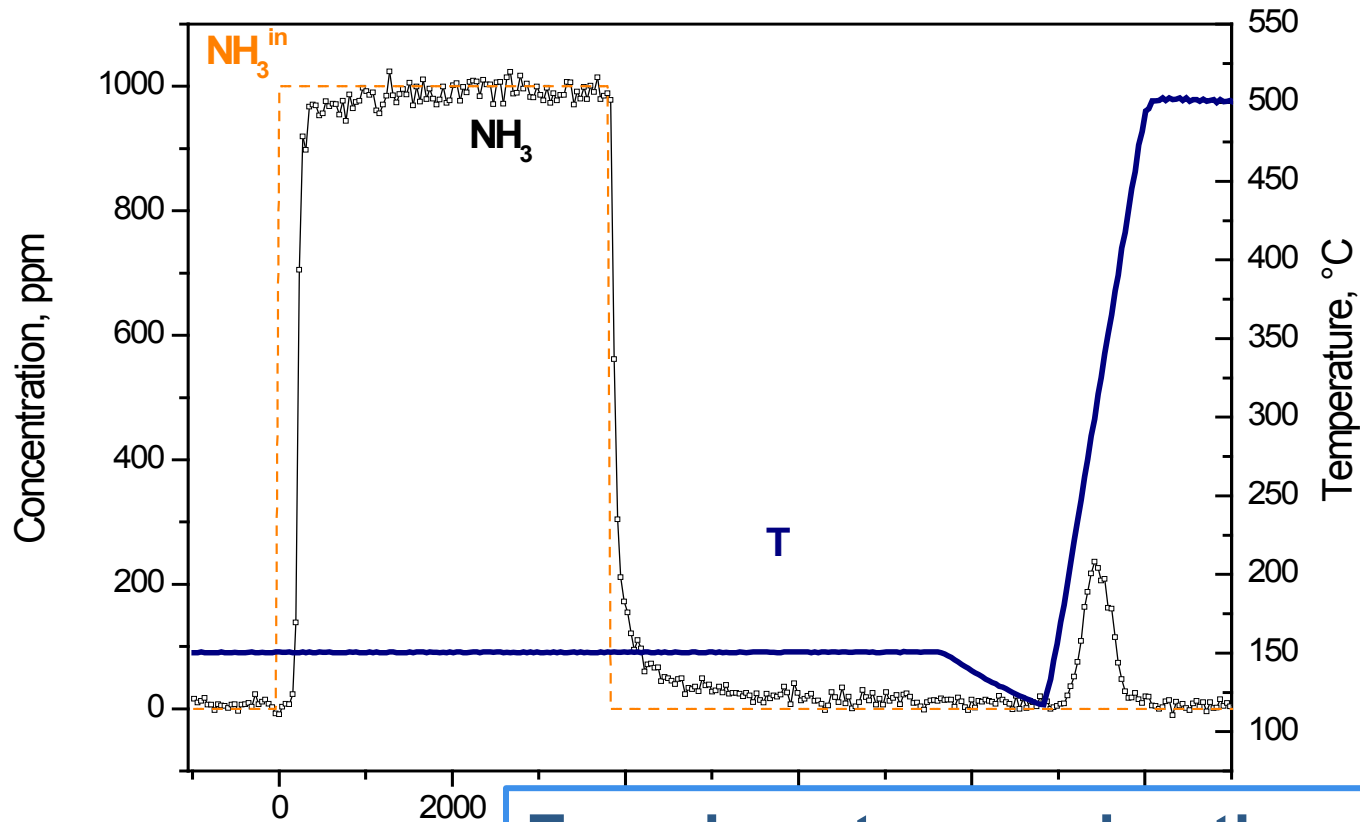
$\text{NH}_3 = 1000 \text{ ppm}$

$\text{H}_2\text{O} = \text{O}_2 = 0\%$ ;  $T_{\text{ads}} = 150^\circ\text{C}$ , heating rate =  $15^\circ\text{C}/\text{min}$

$\text{GHSV} = 30'000 \text{ h}^{-1}$

# Podwered catalyst: $\text{NH}_3$ adsorption/desorption

Symbols = experimental



**Experiments covering the effects of:**  
ammonia concentration  
adsorption temperature  
TPD heating rate

## Experimental conditions:

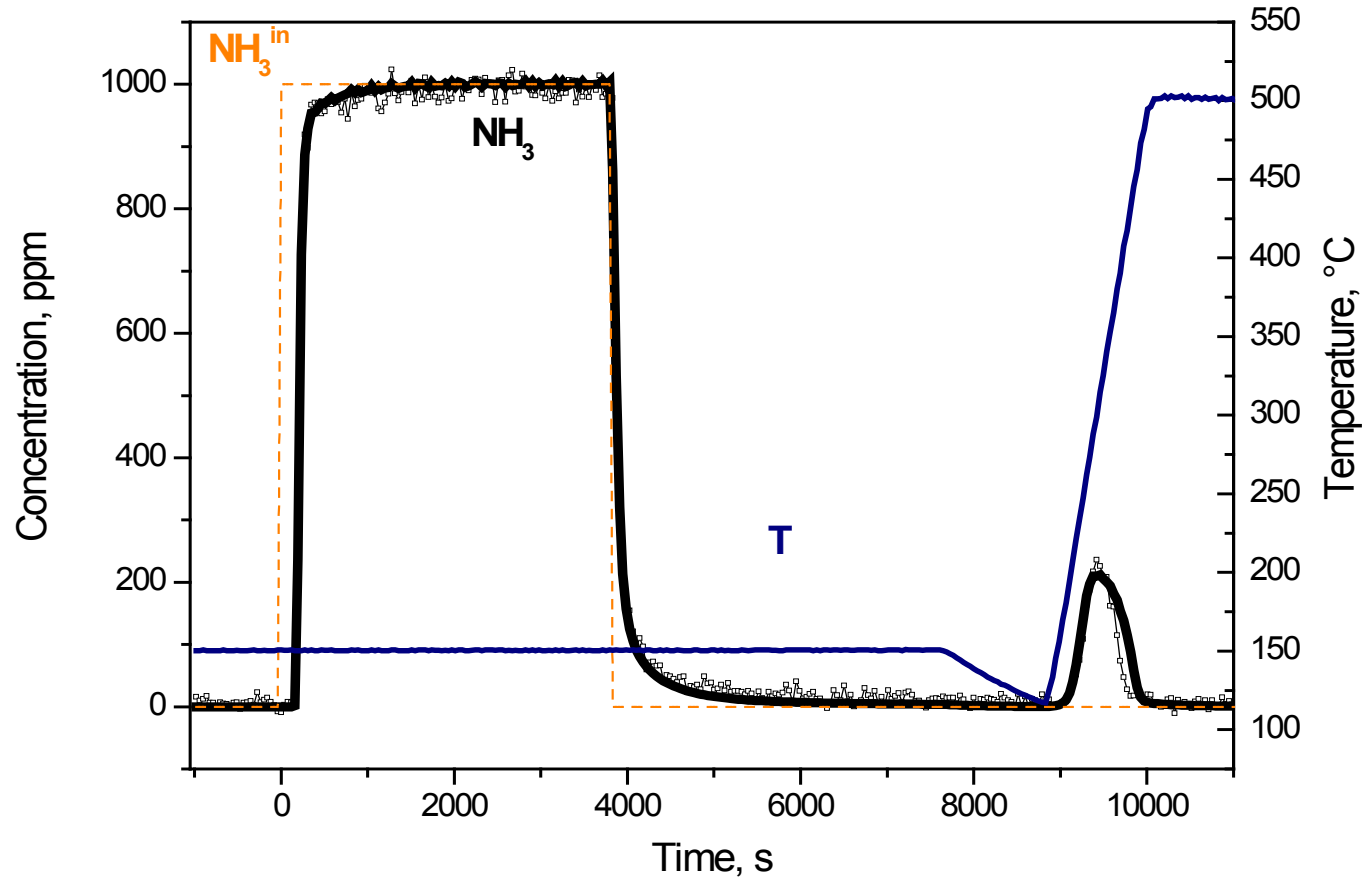
$\text{NH}_3 = 1000 \text{ ppm}$

$\text{H}_2\text{O} = \text{O}_2 = 0\%$ ;  $T_{\text{ads}} = 150^\circ\text{C}$ , heating rate =  $15^\circ\text{C}/\text{min}$

GHSV =  $30'000 \text{ h}^{-1}$

# Podwered catalyst: $\text{NH}_3$ adsorption/desorption

Symbols = experimental  
Thick lines = kinetic fit

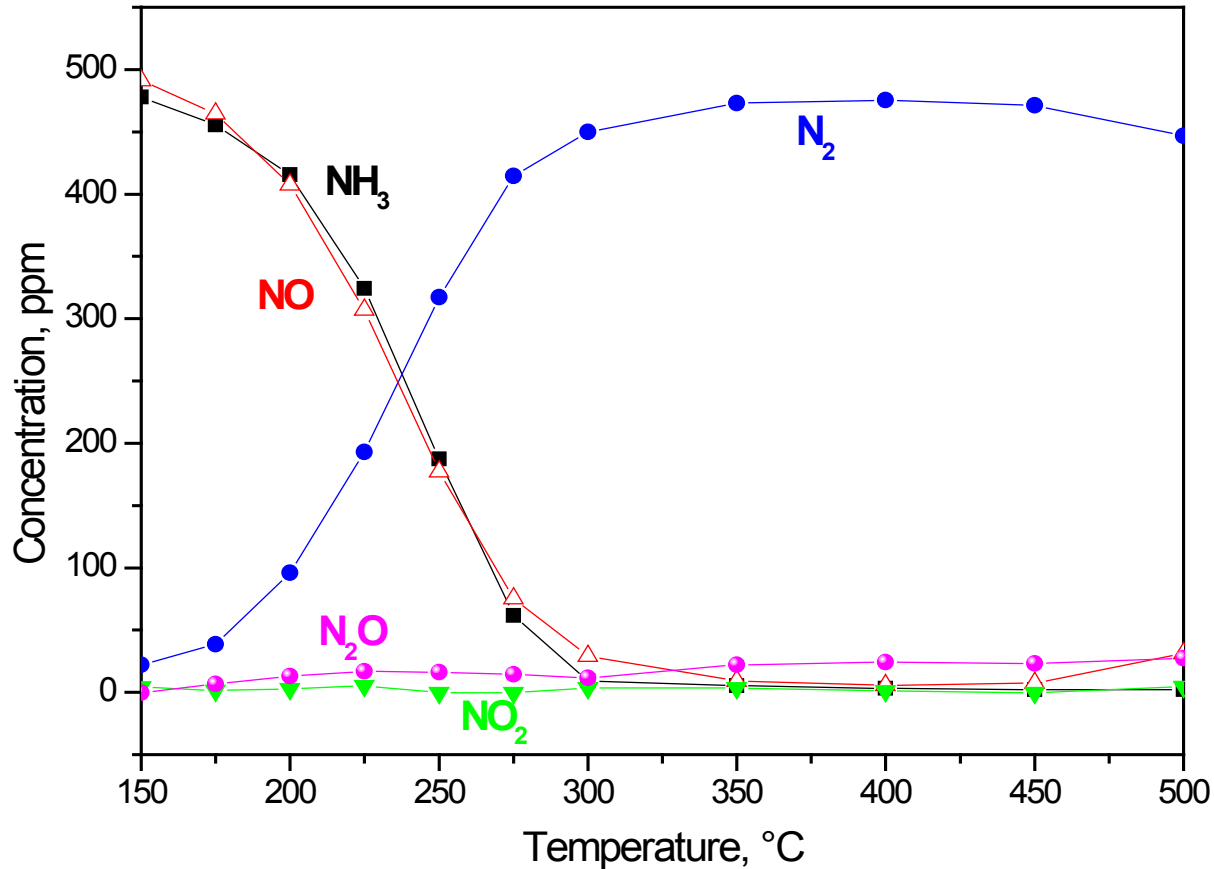


## Experimental conditions:

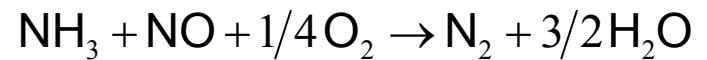
$\text{NH}_3 = 1000 \text{ ppm}$

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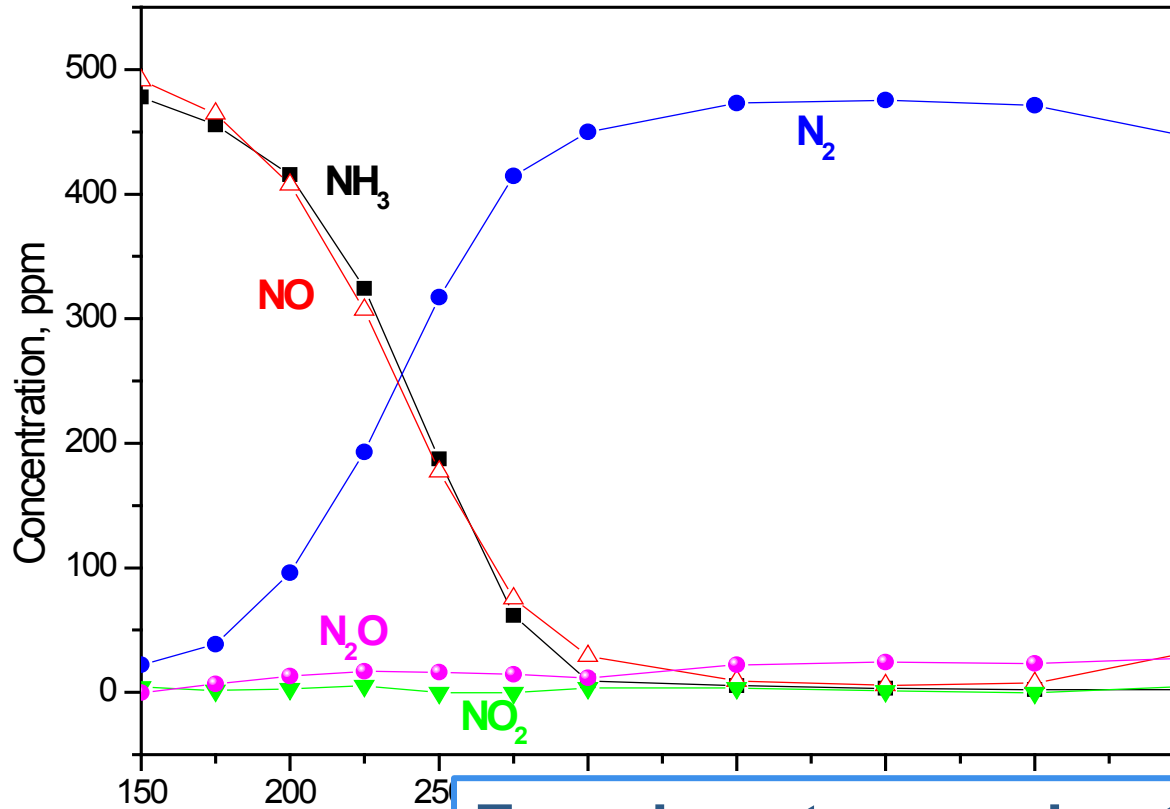
$\text{GHSV} = 30'000 \text{ h}^{-1}$



## Standard SCR



**Experimental conditions:**  
 $\text{NH}_3 = 500 \text{ ppm}$ ;  $\text{NO} = 500 \text{ ppm}$   
 $\text{H}_2\text{O} = 8\%$ ;  $\text{O}_2 = 8\%$   
 $\text{GHSV} = 70'000 \text{ h}^{-1}$



Experiments covering the effects of:

Flow rates

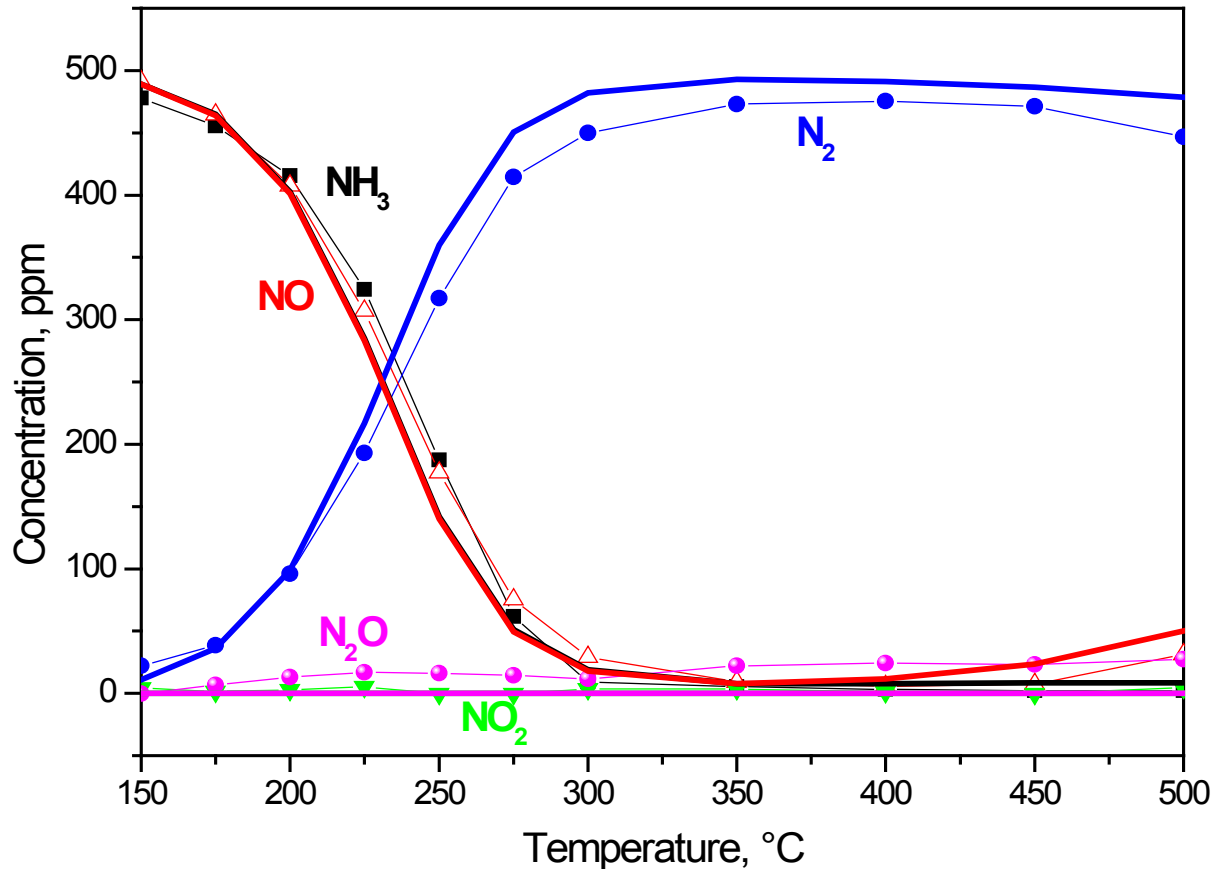
$\text{O}_2$  concentration

Transient behavior

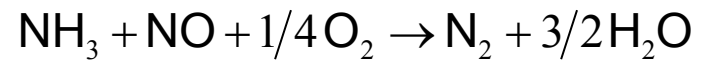
Experimental conditions:  
 $\text{NH}_3 = 500$  ppm;  $\text{NO} = 500$  ppm  
 $\text{H}_2\text{O} = 8\%$ ;  $\text{O}_2 = 8\%$   
GHSV =  $70'000 \text{ h}^{-1}$

# Podwered catalyst: $\text{NH}_3/\text{NO}/\text{O}_2$

Symbols = experimental  
Thick lines = kinetic fit



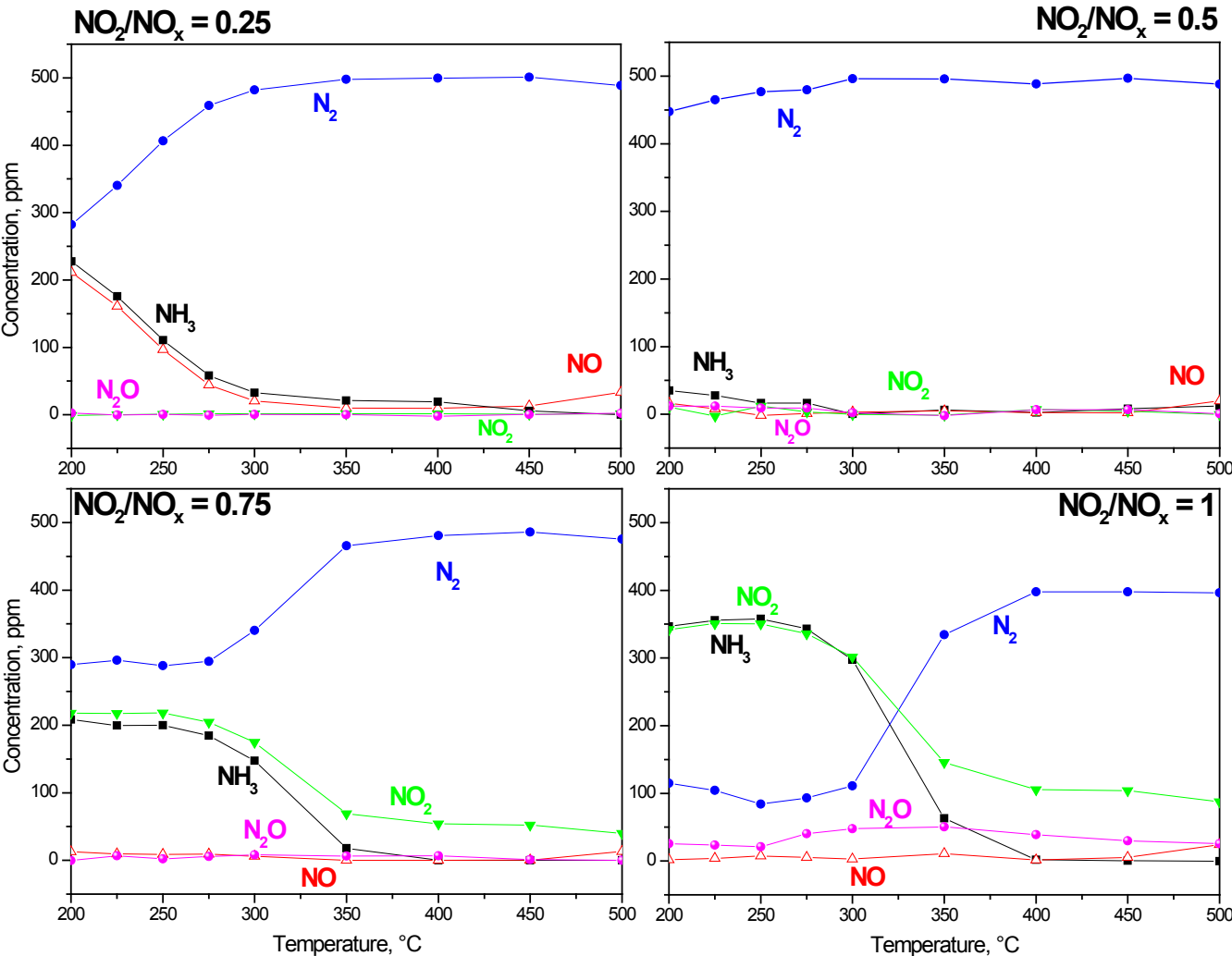
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**Experimental conditions:**  
 $\text{NH}_3 = 500 \text{ ppm}$ ;  $\text{NO} = 500 \text{ ppm}$   
 $\text{H}_2\text{O} = 8\%$ ;  $\text{O}_2 = 8\%$   
 $\text{GHSV} = 70'000 \text{ h}^{-1}$

# Podwered catalyst: $\text{NH}_3/\text{NO}_x/\text{O}_2$

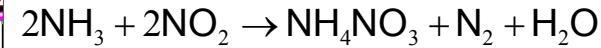
Symbols = experimental



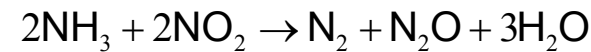
## Fast SCR



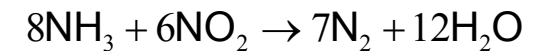
## Formation of $\text{NH}_4\text{NO}_3$



## Formation of $\text{N}_2\text{O}$



## $\text{NO}_2$ SCR



### Experimental conditions:

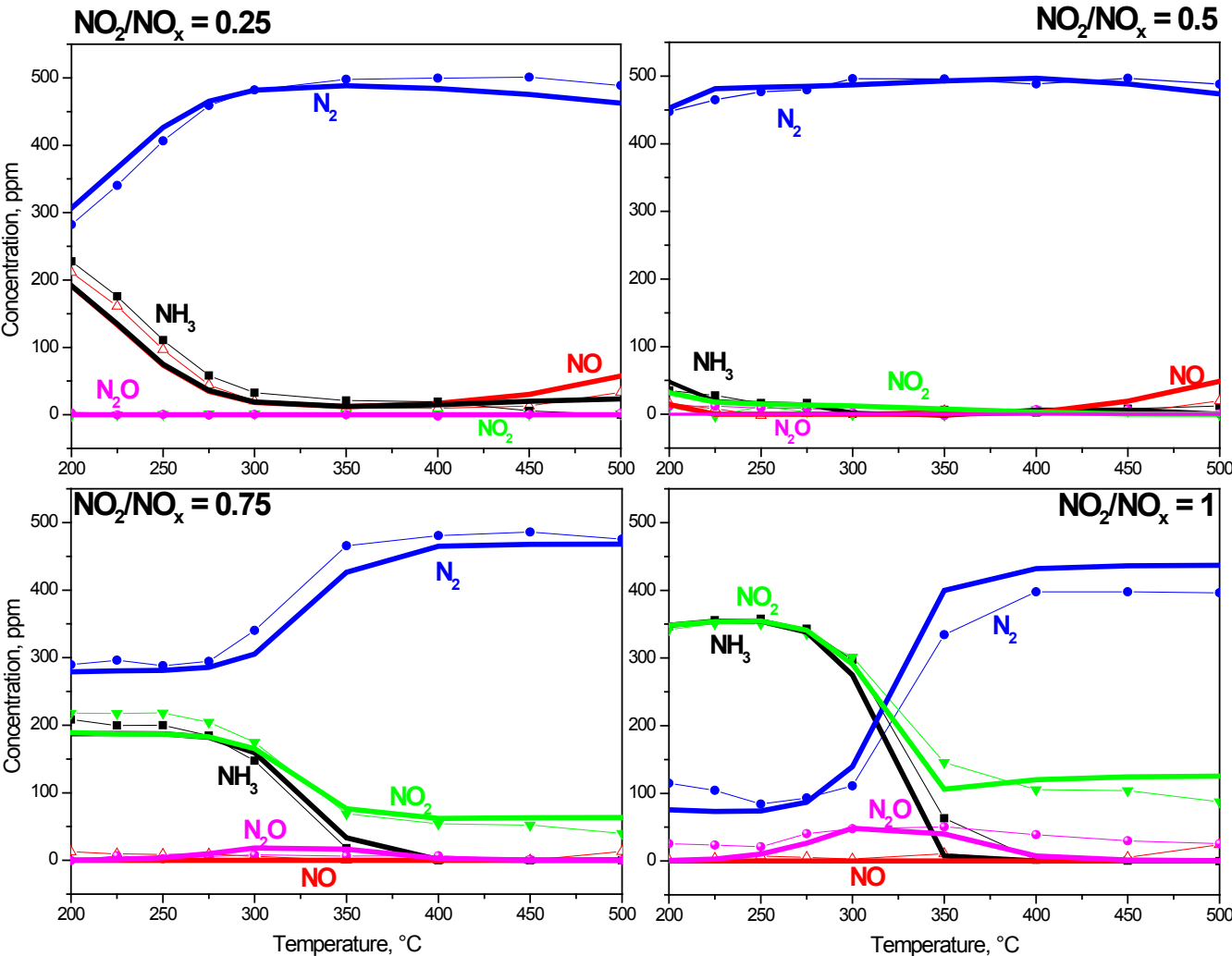
$\text{NH}_3 = 500 \text{ ppm}$ ;  $\text{NO}_x = 500 \text{ ppm}$

$\text{H}_2\text{O} = 8\%$ ;  $\text{O}_2 = 2\%$

$\text{GHSV} = 70'000 \text{ h}^{-1}$

# Podwered catalyst: $\text{NH}_3/\text{NO}_x/\text{O}_2$

Symbols = experimental  
Thick lines = kinetic fit



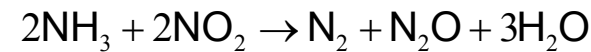
## Fast SCR



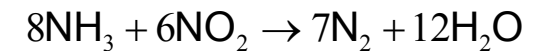
## Formation of $\text{NH}_4\text{NO}_3$



## Formation of $\text{N}_2\text{O}$



## $\text{NO}_2$ SCR



### Experimental conditions:

$\text{NH}_3 = 500 \text{ ppm}$ ;  $\text{NO}_x = 500 \text{ ppm}$

$\text{H}_2\text{O} = 8\%$ ;  $\text{O}_2 = 2\%$

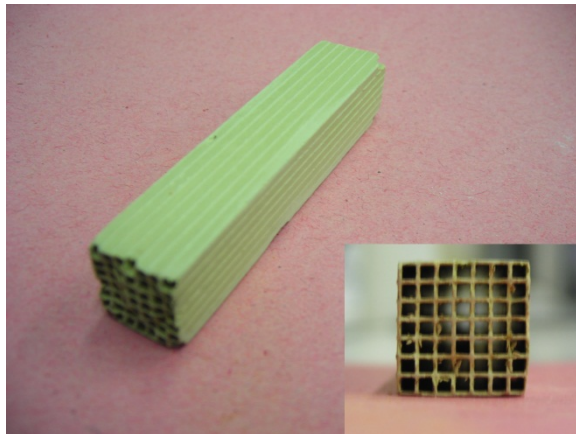
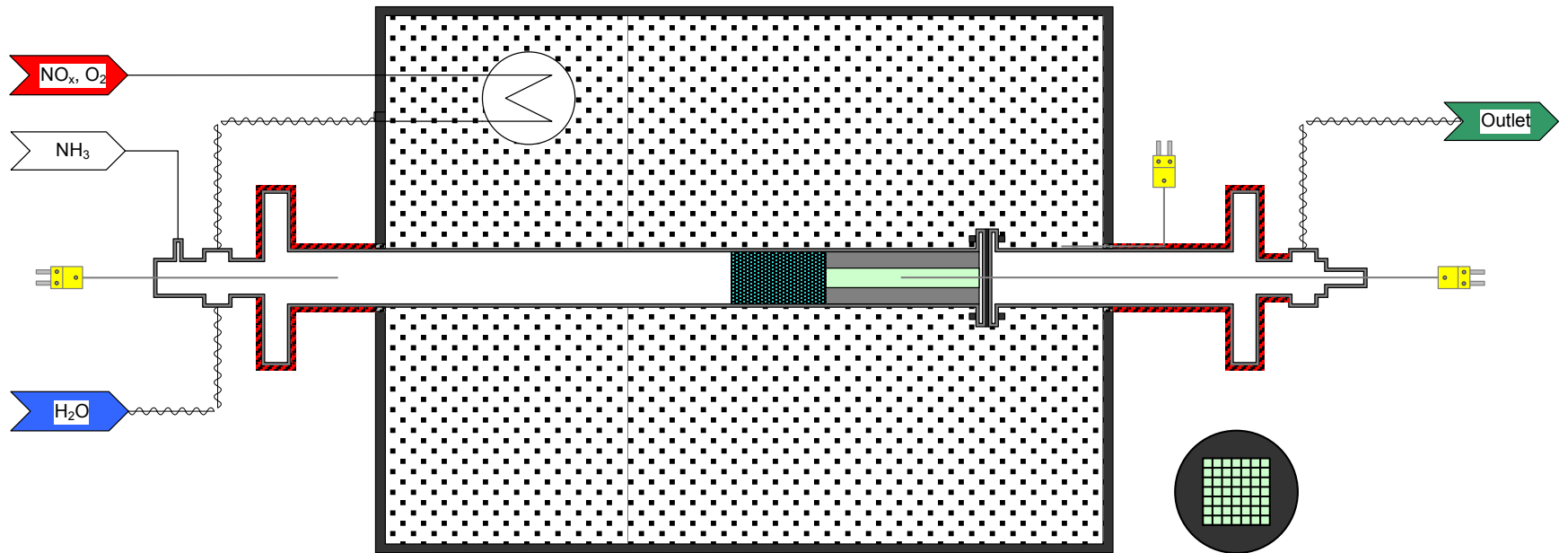
$\text{GHSV} = 70'000 \text{ h}^{-1}$



# **Validation runs over monolith catalyst**

**... assessment of mass transfer from powdered vs. monolith data**

# Monolith reactor experiments



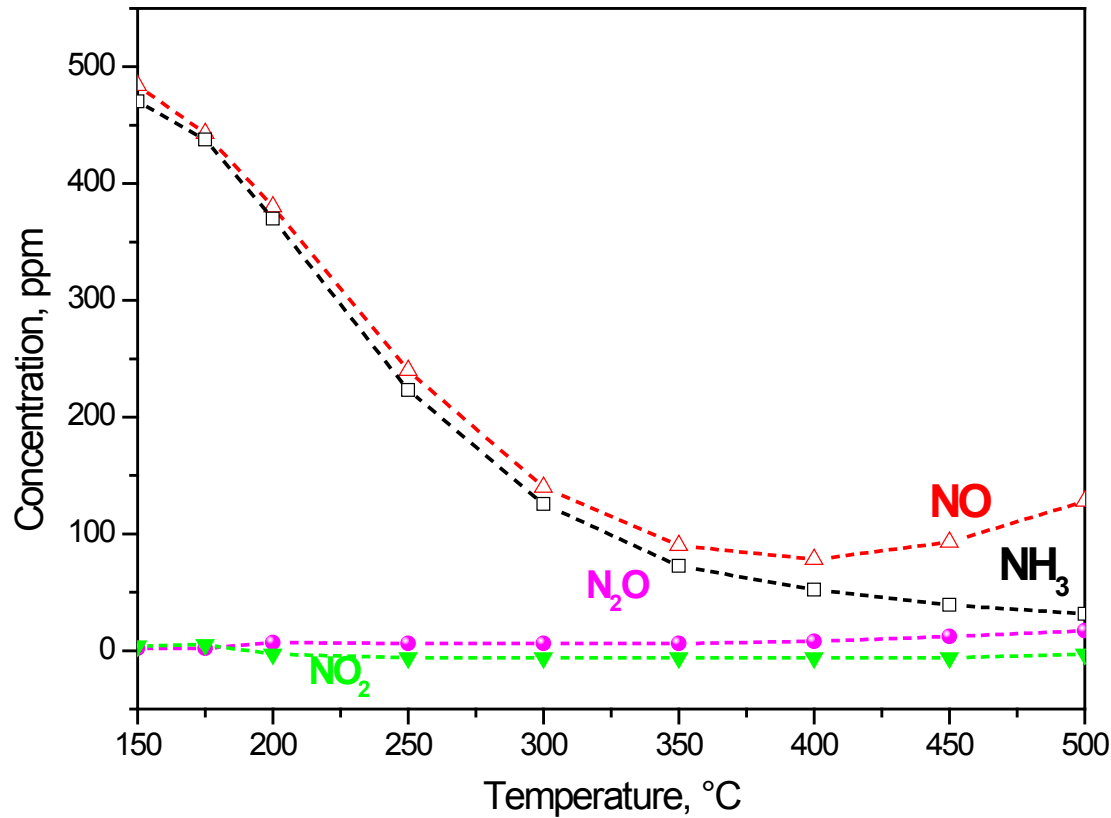
## Sample:

CPSI= 300  
Wall thickness = 0.32 mm  
 $V = 5 \text{ cm}^3$   
Length = 5.2 cm  
Channels = 49

## Experimental conditions:

GHSV = 30'000-70'000  $\text{h}^{-1}$   
 $\text{H}_2\text{O} = 8 \%$ ;  $\text{O}_2 = 2-8 \%$   
 $\text{NH}_3 = 500-1000 \text{ ppm}$   
 $\text{NO} = 0-500 \text{ ppm}$   
 $\text{NO}_2 = 0-500 \text{ ppm}$   
 $\text{NO}/\text{NO}_2 = 0-1$   
 $T = 150-550^\circ\text{C}$

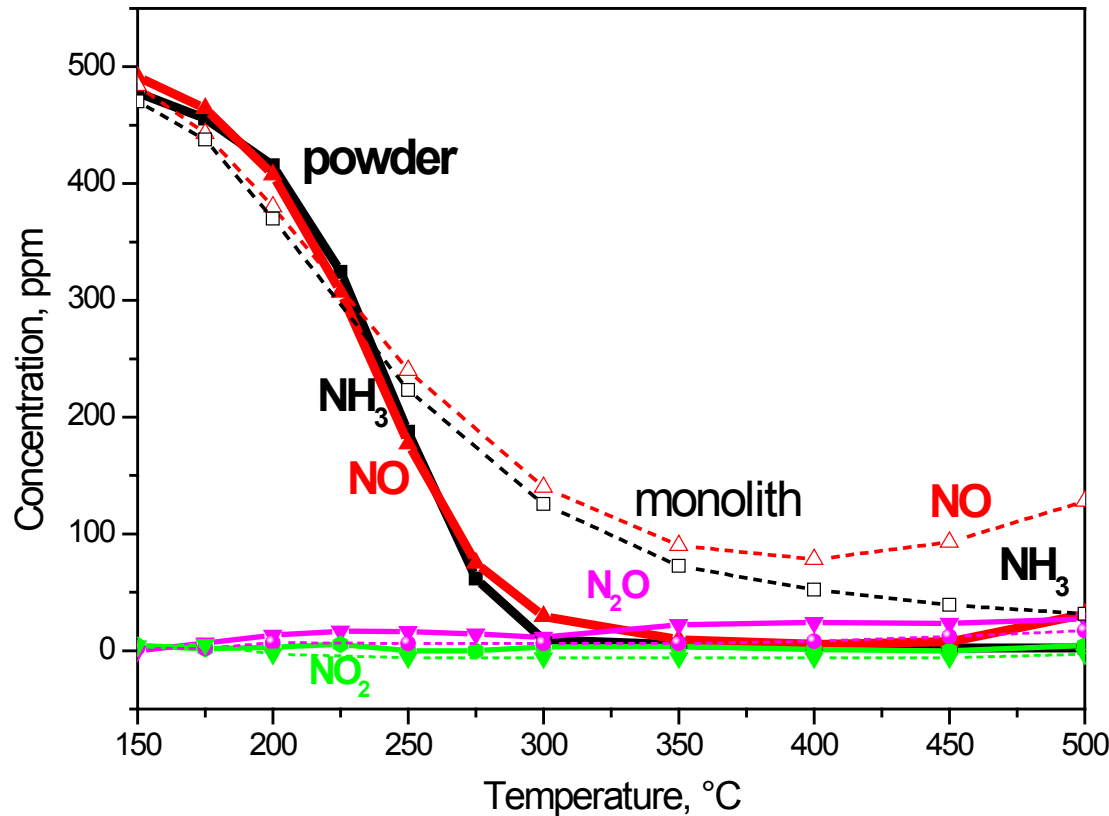
Dashed lines = monolith data



**Experimental conditions:**  
NH<sub>3</sub> = 500 ppm; NO = 500 ppm  
H<sub>2</sub>O = 8%; O<sub>2</sub> = 8%  
GHSV = 70'000 h<sup>-1</sup>

# Monolith vs. powdered data: $\text{NH}_3/\text{NO}/\text{O}_2$

Dashed lines = monolith data  
Thick lines = powder data



The monolith shows  
lower conversions  
at  $T > 250^\circ\text{C}$

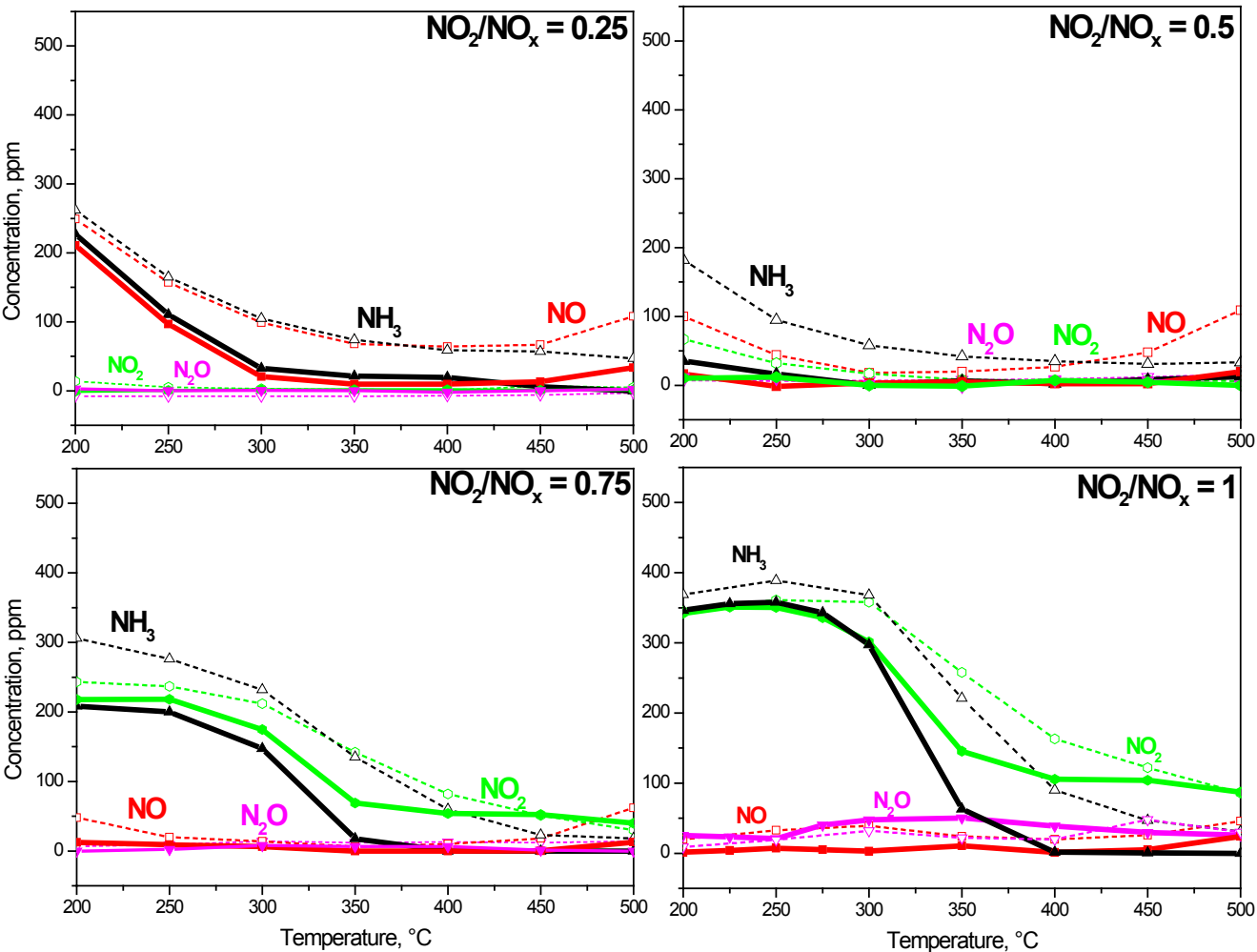


onset of diffusional  
limitations

**Experimental conditions:**  
 $\text{NH}_3 = 500 \text{ ppm}$ ;  $\text{NO} = 500 \text{ ppm}$   
 $\text{H}_2\text{O} = 8\%$ ;  $\text{O}_2 = 8\%$   
 $\text{GHSV} = 70'000 \text{ h}^{-1}$

# Monolith vs. powdered data: $\text{NH}_3/\text{NO}_x/\text{O}_2$

Dashed lines = monolith data  
Thick lines = powdered data



**Consistent deviations in the range  $200 < T < 500^\circ\text{C}$  in the presence of  $\text{NO}_2$**

**Experimental conditions:**  
 $\text{NH}_3 = 500 \text{ ppm}$ ;  $\text{NO}_x = 500 \text{ ppm}$   
 $\text{H}_2\text{O} = 8\%$ ;  $\text{O}_2 = 2\%$   
 $\text{GHSV} = 70'000 \text{ h}^{-1}$

# **Model simulations**

**... analysis of internal and external  
diffusional limitations**

# 1D + 1D model for monolith converters

**Hypothesis:** identical conditions within each channel, negligible axial dispersion and pressure drop

**1D:** heat and mass transfer along the monolith channel

$$\begin{aligned} \text{gas phase} \quad \frac{\delta C_j}{\delta t} &= -\frac{v}{L} \frac{\delta C_j}{\delta z} - \frac{4}{d_h} k_{mt,j} (C_j - C_j^W) \\ \text{solid phase} \quad 0 &= k_{mt,j} (C_j - C_j^W) + R_{eff,j} \end{aligned} \quad j = \text{NH}_3, \text{NO}, \text{NO}_2$$

**External limitations:**  
**mass transfer coefficient**

$$k_{mt,i} = \frac{Sh}{d_h} (D_{m,i}) \quad Sh = Sh_\infty + 8.827 \cdot \left( 1000 \cdot \frac{L}{d_h Sc Re} \right)^{-0.545} \exp\left( -48.2 \cdot \frac{L}{d_h Sc Re} \right)$$

   $Sh_\infty = 2.976$

**1D:** reaction and diffusion within the porous structure of the catalyst

*flat plate assumption*

$$0 = D_{eff,j} \frac{\delta^2 C_j^*}{\delta x^2} + S_W^2 R_j \quad R_{eff,j} = -\frac{D_{eff,j}}{S_W} \frac{\delta C_j^*}{\delta x} \Big|_W$$

**Internal limitations:**  
**effective diffusivity**

$$D_{eff,i} = \varepsilon_M^2 \cdot D_{M,i} + \frac{\varepsilon_\mu^2 \cdot (1+3 \cdot \varepsilon_M)}{1-\varepsilon_M} \cdot D_{\mu i} \quad \varepsilon_i \text{ and } D_i \text{ from morphological data}$$

$$D_{eff,i} \approx 3 \cdot 10^{-6} \text{ m}^2/\text{s} @ 200^\circ\text{C}$$

Chatterjee et al. SAE 2006-01-0468

Tronconi and Forzatti, AIChE J. 38 (1992) 201

Shah and London, in Advances in Heat Transfer, Ac.Press (1978)

Beekman, Ind. Eng. Chem. Res., 30 (1991) 428

# 1D + 1D model for monolith converters



**Intrinsic kinetics**, estimated from powder data

**geometrical and morphological properties of the catalyst** ( $k_{mt,j}$ ,  $D_{eff,j}$ )



**1D + 1D monolith model**

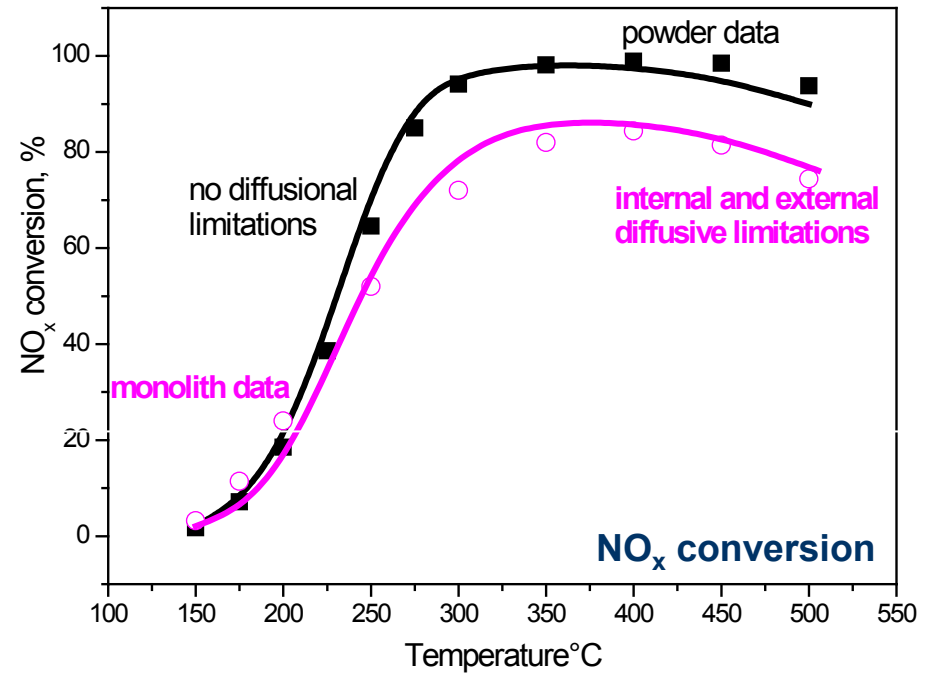
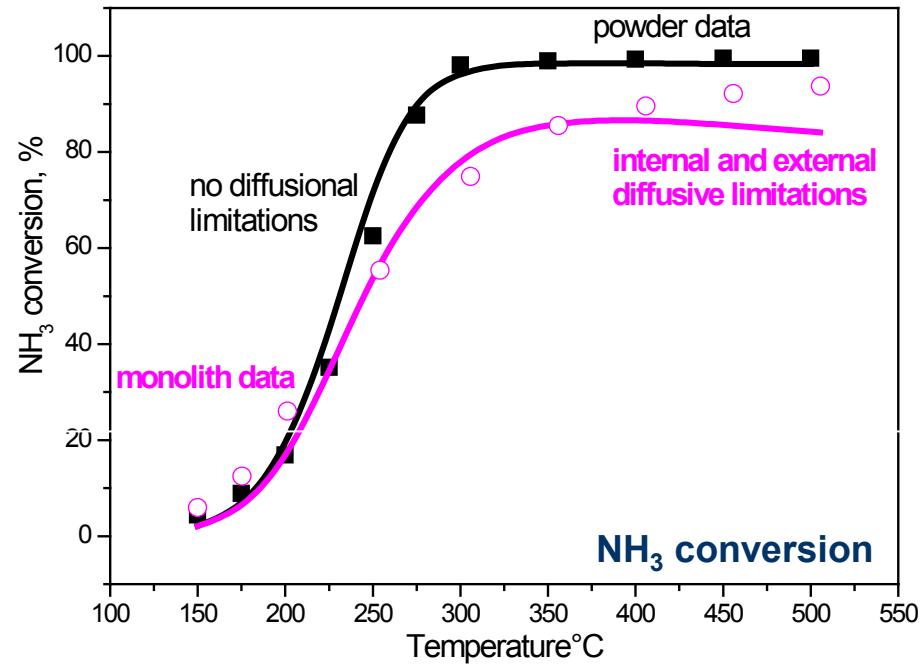
accounting for external and internal diffusional limitations

Decoupling of the contributions of internal and external mass transfer resistances:

- Simulations for **internal** diffusional limitation only:  $k_{mt,j}$  set to  $300 k_{mt,j}$
- Simulations for **external** diffusional limitation only:  $D_{eff,j}$  set to  $30 D_{eff,j}$



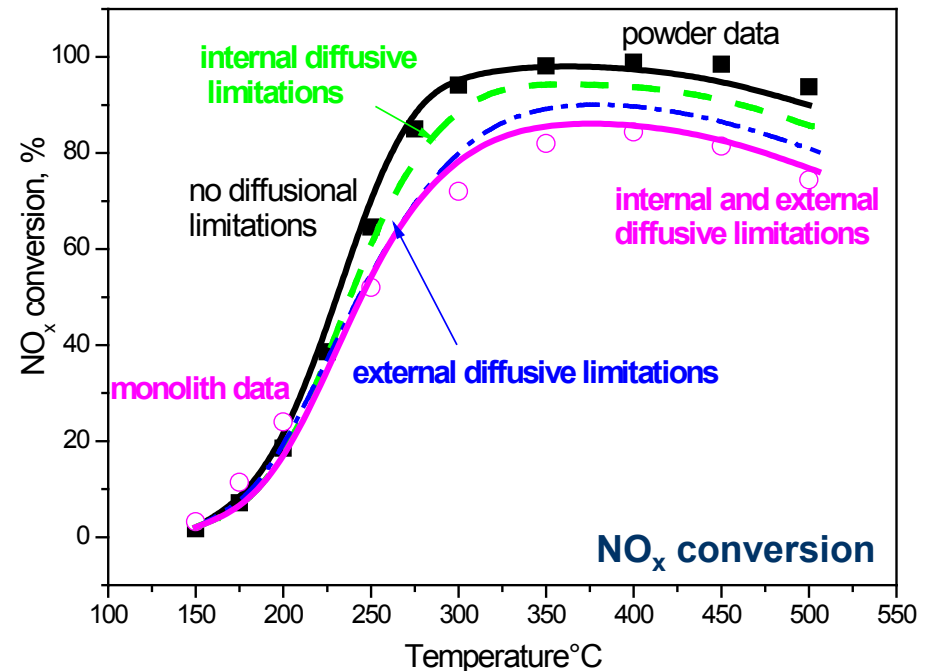
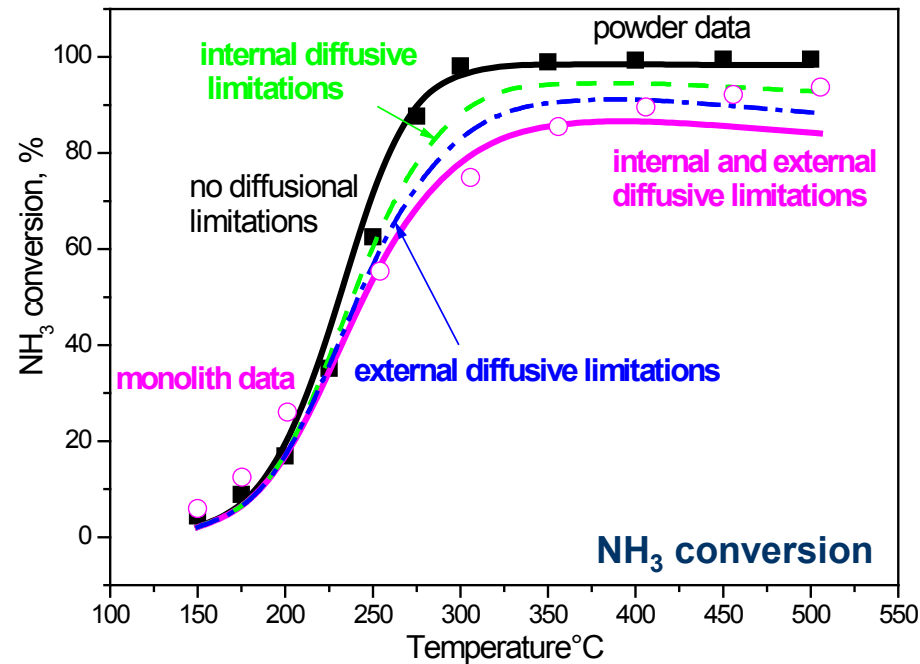
# Model simulations: NH<sub>3</sub>/NO/O<sub>2</sub>



Model simulations in good agreement with monolith data.

**Experimental conditions:**  
NH<sub>3</sub> = 500 ppm; NO = 500 ppm  
H<sub>2</sub>O = 8%; O<sub>2</sub> = 8%  
GHSV = 70'000 h<sup>-1</sup>

# Model simulations: NH<sub>3</sub>/NO/O<sub>2</sub>

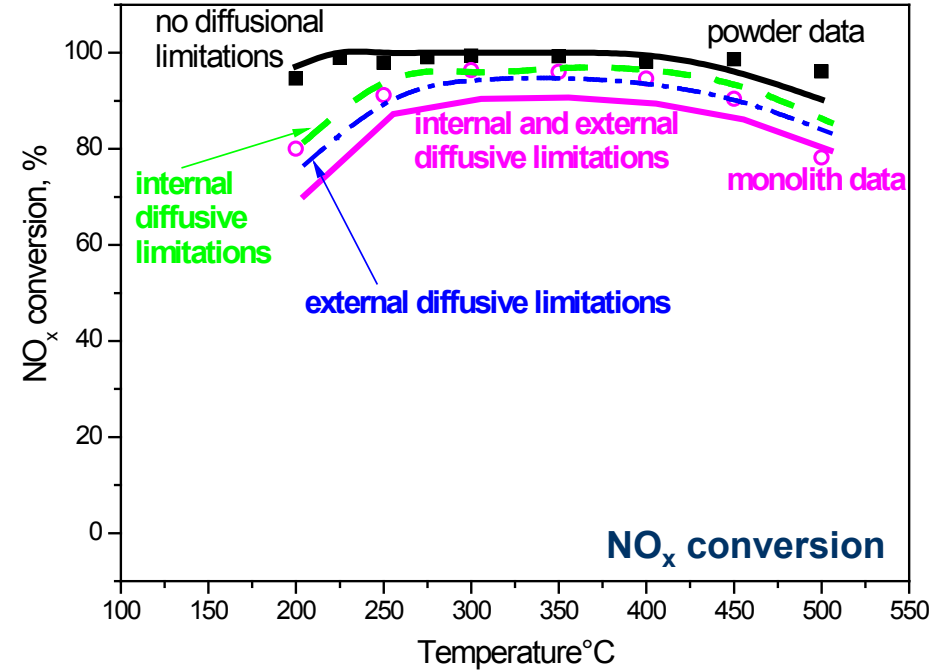
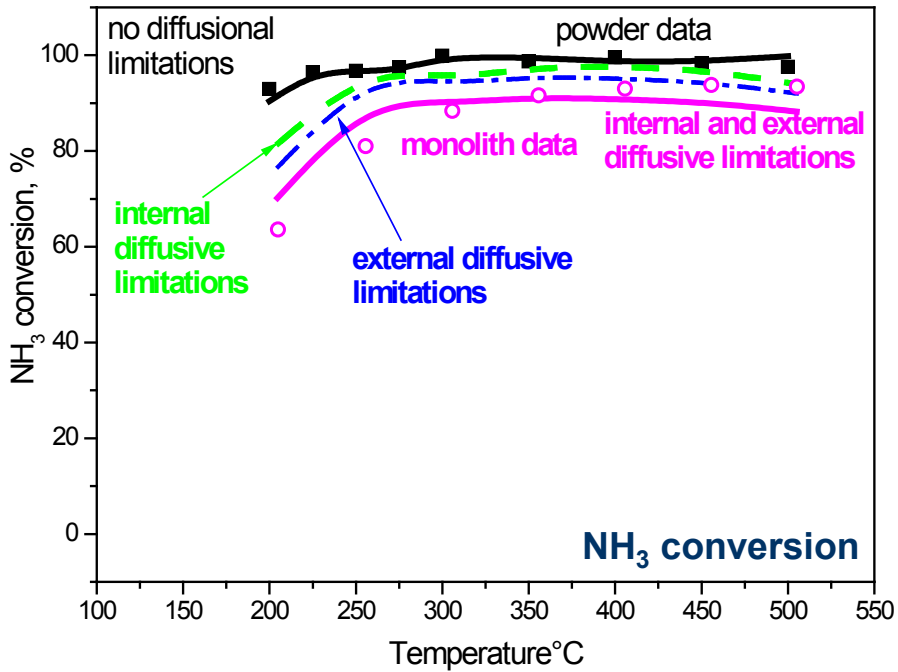


Model simulations in good agreement with monolith data.

Modest **intra-phase** limitations already at 200°C, increasing with T  
**External** diffusional limitations starting from 225°C and dominant at higher temperatures

Experimental conditions:  
NH<sub>3</sub> = 500 ppm; NO = 500 ppm  
H<sub>2</sub>O = 8%; O<sub>2</sub> = 8%  
GHSV = 70'000 h<sup>-1</sup>

# Model simulations: NH<sub>3</sub>/NO/NO<sub>2</sub>/O<sub>2</sub>



Both **intra** and **inter**phase diffusional limitations play a significant role already at 200°C.

**External** mass transfer phenomena are dominant at  $T > 250^\circ\text{C}$ .

**Experimental conditions:**  
NH<sub>3</sub> = 500 ppm; NO = NO<sub>2</sub> = 500 ppm  
H<sub>2</sub>O = 8%; O<sub>2</sub> = 8%  
GHSV = 70'000 h<sup>-1</sup>

# Conclusions

- Important role of mass transfer resistances in reducing  $\text{NH}_3$ -SCR performance pointed out by direct comparison between powder and monolith catalyst data
- Negative deviations observed at  $250^\circ\text{C}$  for the Standard SCR and at lower temperature when  $\text{NO}_2$  was present
- Predictive 1D+1D model simulations show good agreement with data collected at the monolith scale
- Model analysis allowed discrimination between contributions of internal and external diffusional limitations

# Acknowledgements

**V.Schmeisser**  
**L.Zimmermann**  
**B.Bandl-Konrad**

**DAIMLER**

# Thank you for your attention!



Raffaello, The school of Athens, 1509,  
Apostolic Palace, Roma

Politecnico di Milano