

# Lawrence Livermore National Laboratory

## Chemical Kinetics Research on HCCI & Diesel Fuels and Computationally Efficient Modeling of High-Efficiency Clean Combustion Engines

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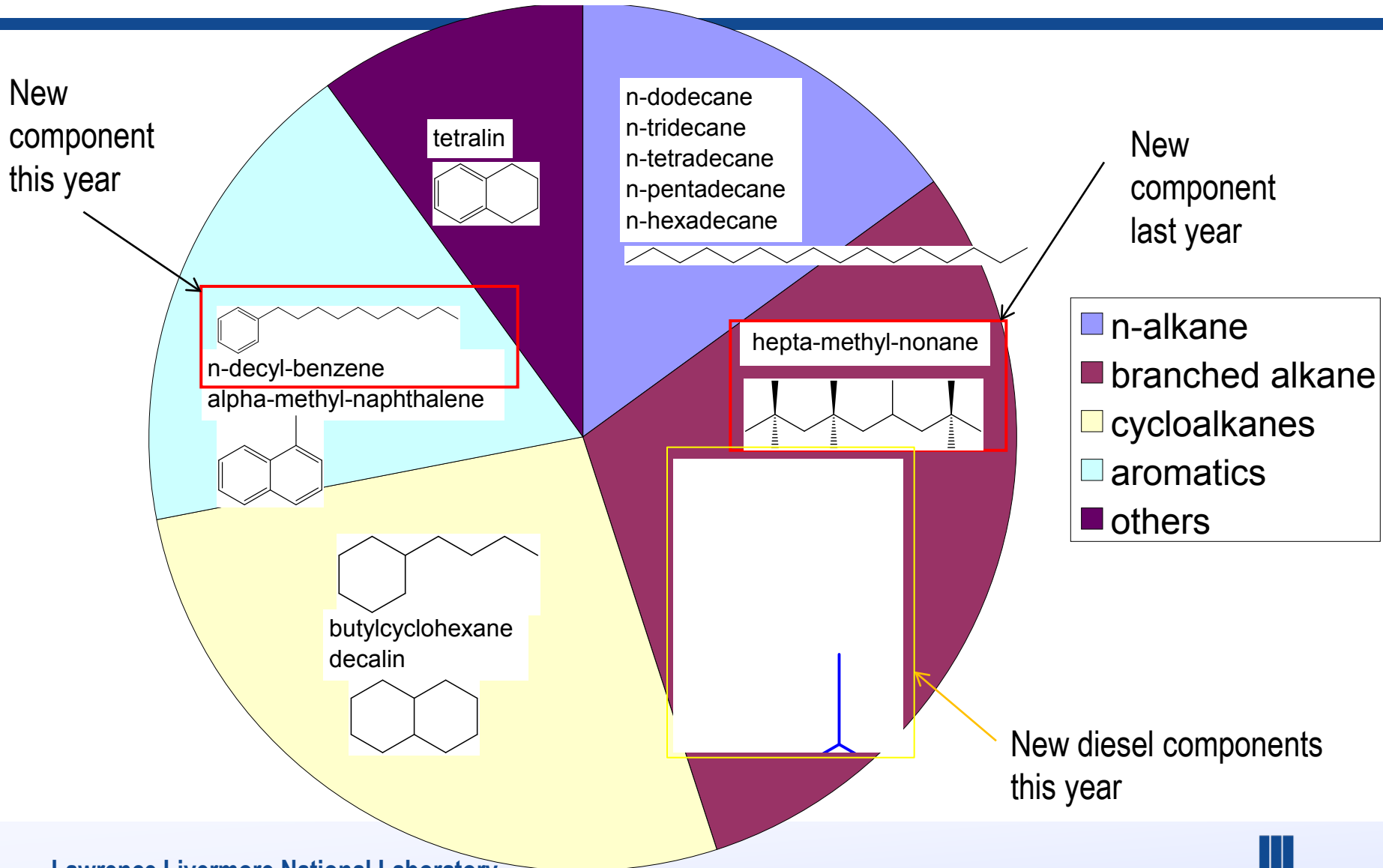
DEER Conference

September 27, 2010 – Detroit, MI

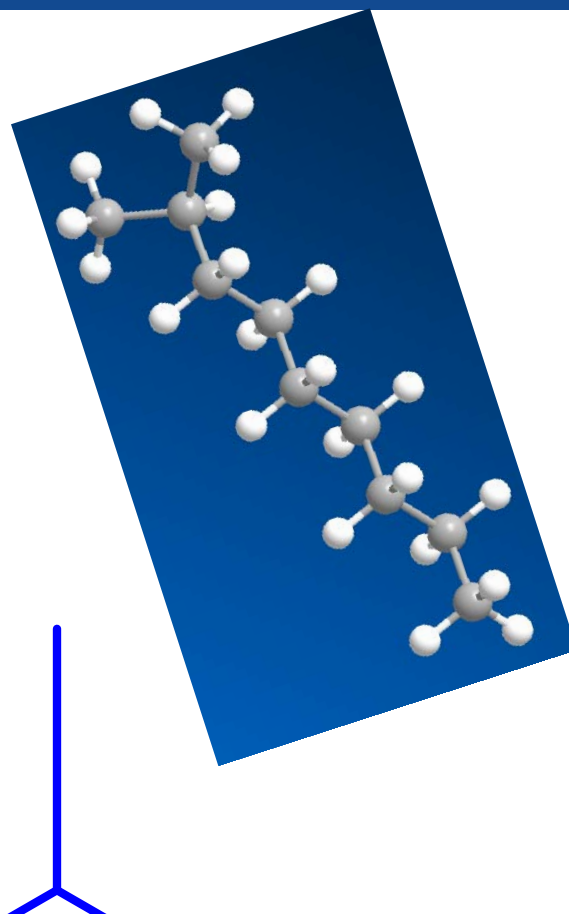
**Sponsor: VTP – Team Leaders Gurpreet Singh and Kevin Stork**

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# We have developed mechanisms for complex long-chain species, enabling more representative diesel surrogates



# We have developed 2-methyl alkane mechanisms up to C20; branched iso-alkanes are significant components in gasoline and diesel fuels



Includes all 2-methyl alkanes up to C20 which covers the entire distillation range for gasoline and diesel fuels

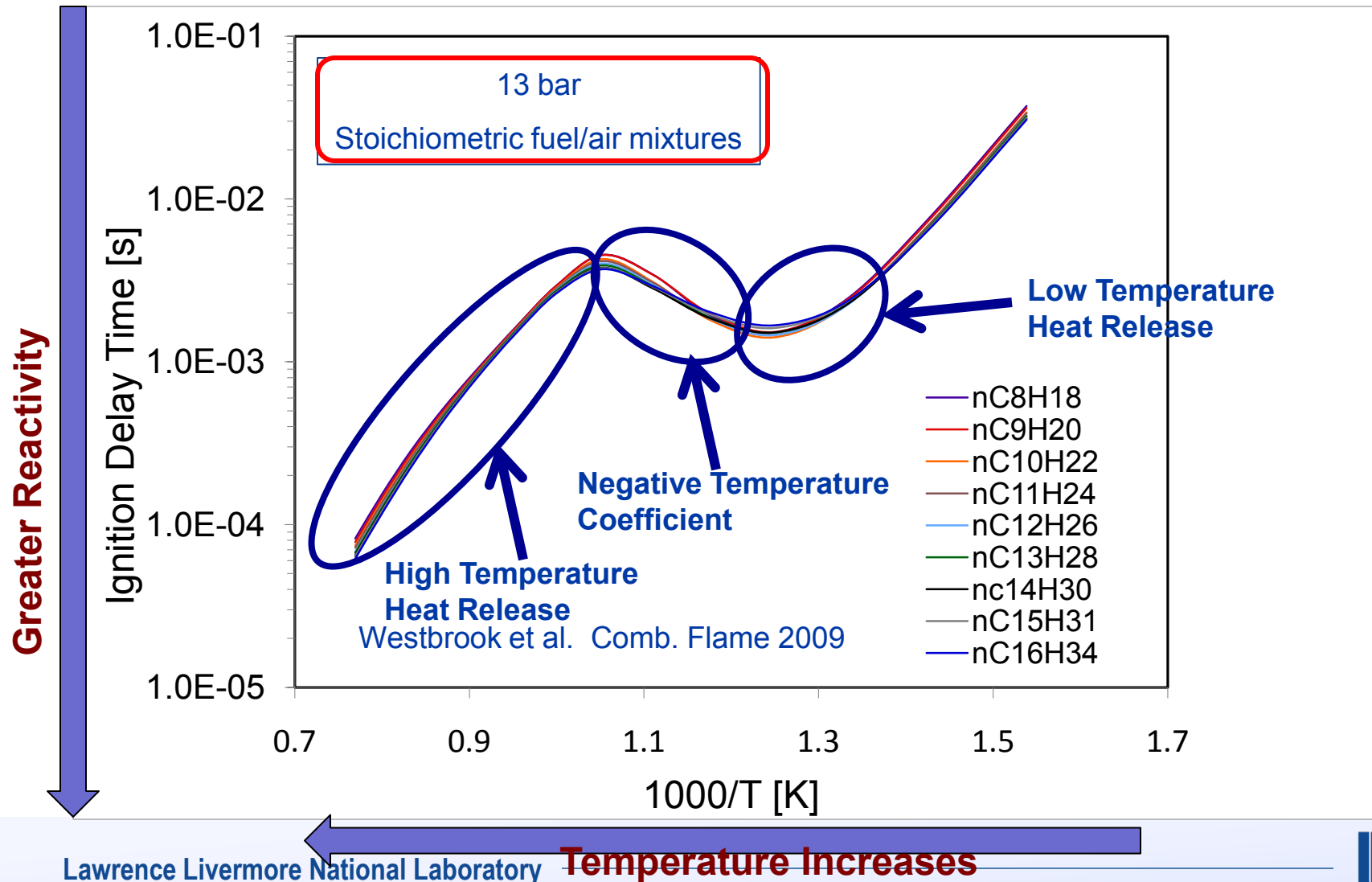
Built with the same reaction rate rules as our successful iso-octane and iso-cetane mechanisms.

**7,900 species**

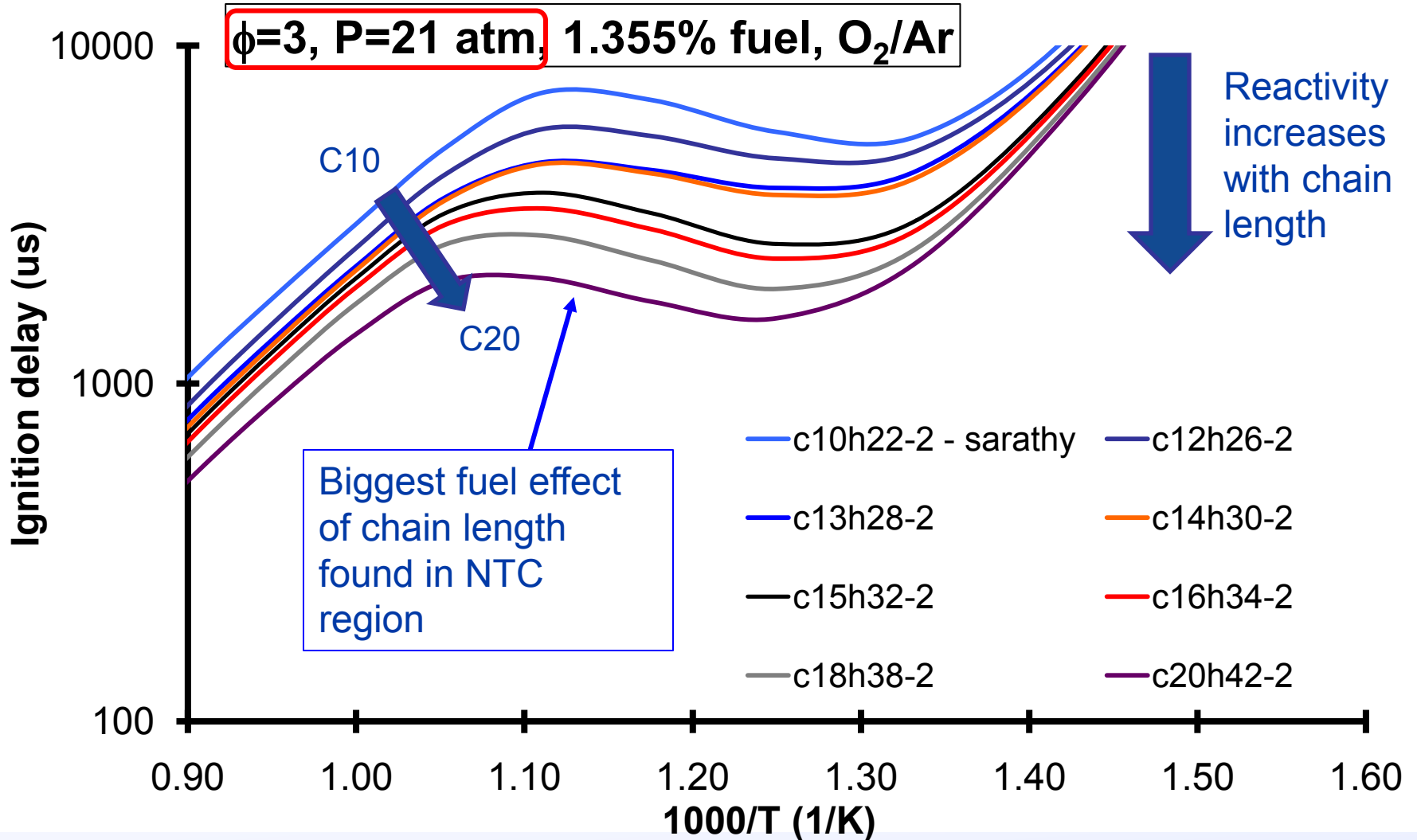
**27,000 reactions**



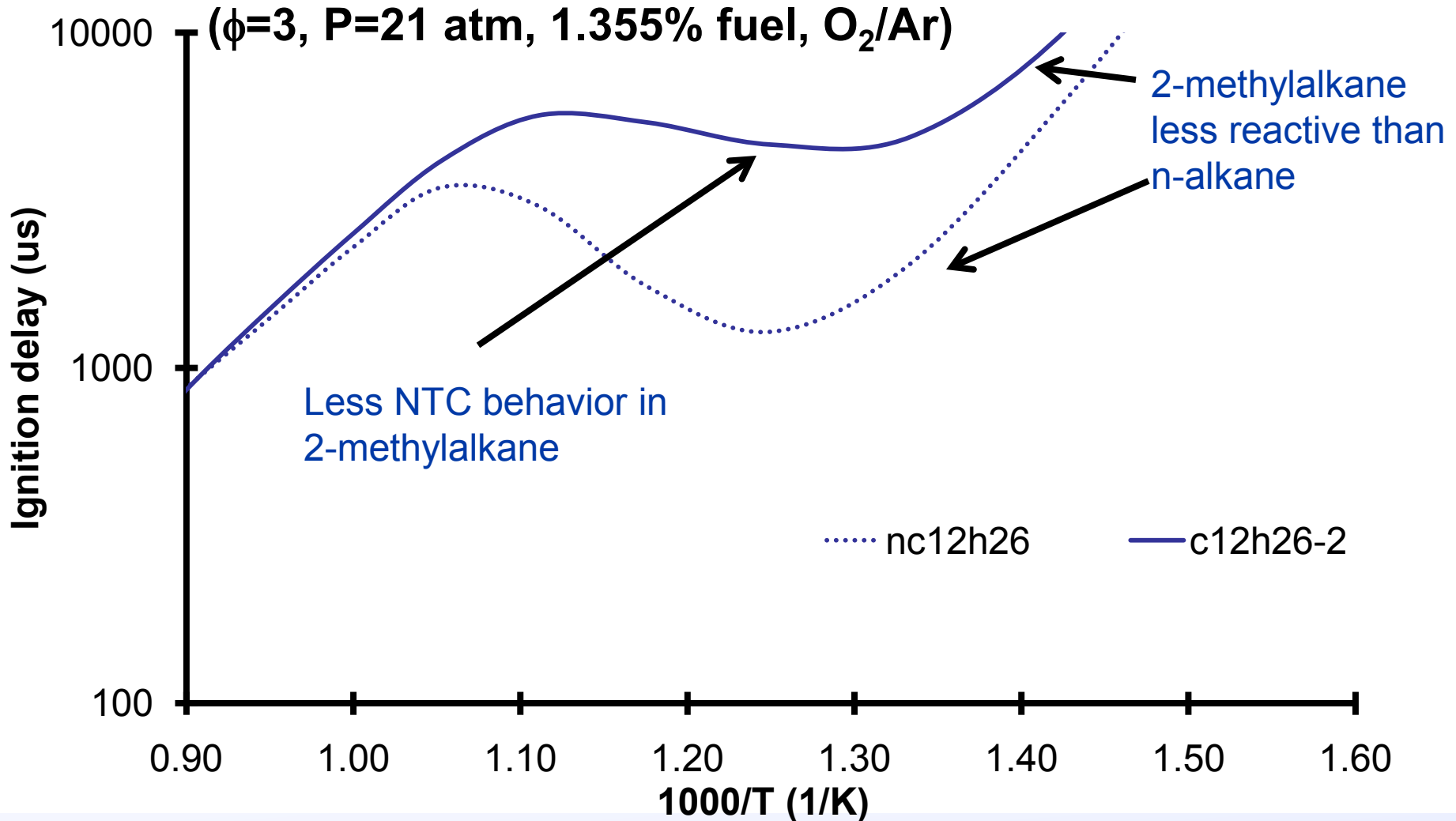
# Our previous work showed that ignition characteristics of normal alkanes depend little on carbon chain length



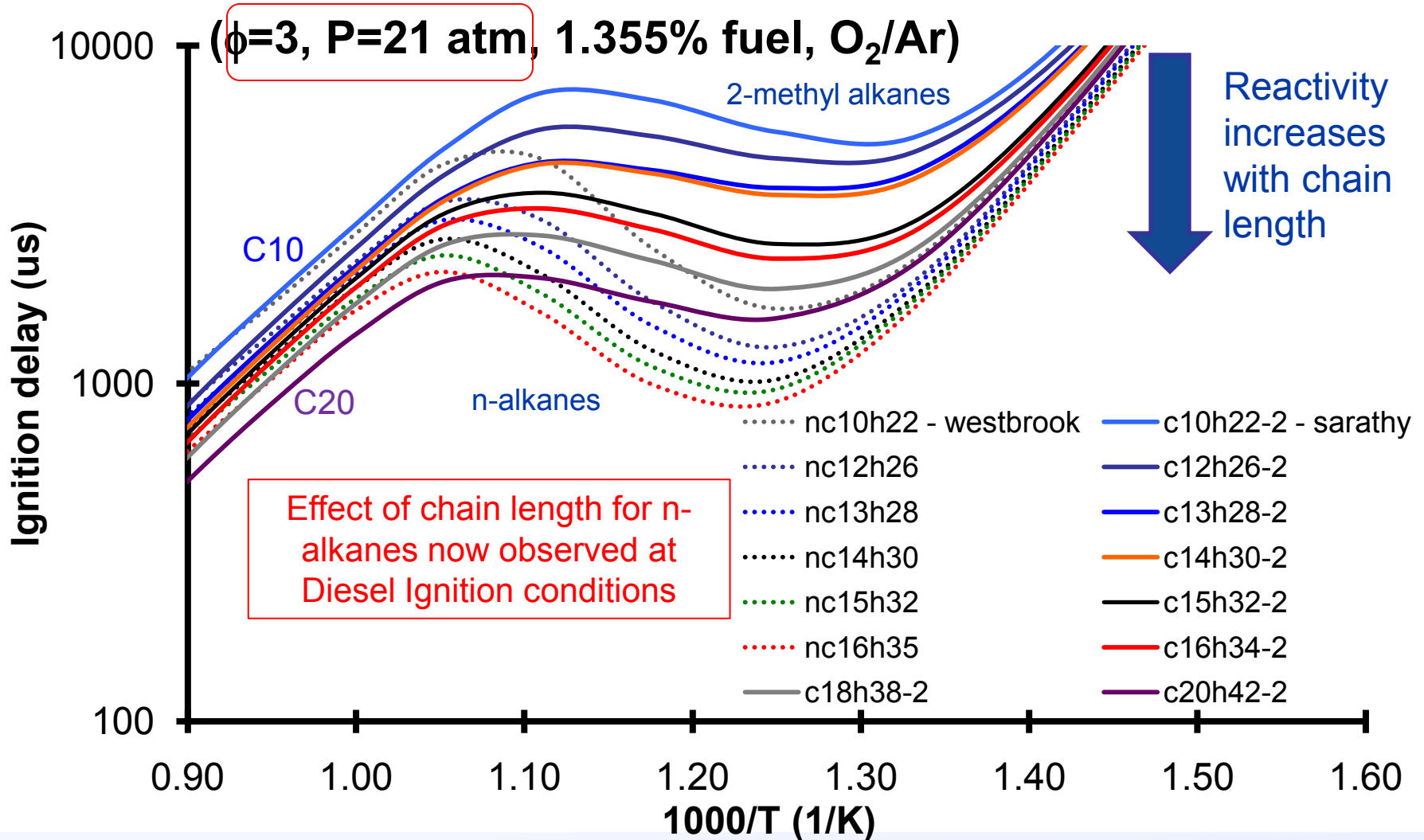
# However, 2-methyl alkanes show more reactivity with chain length at higher equivalence ratio and pressure:



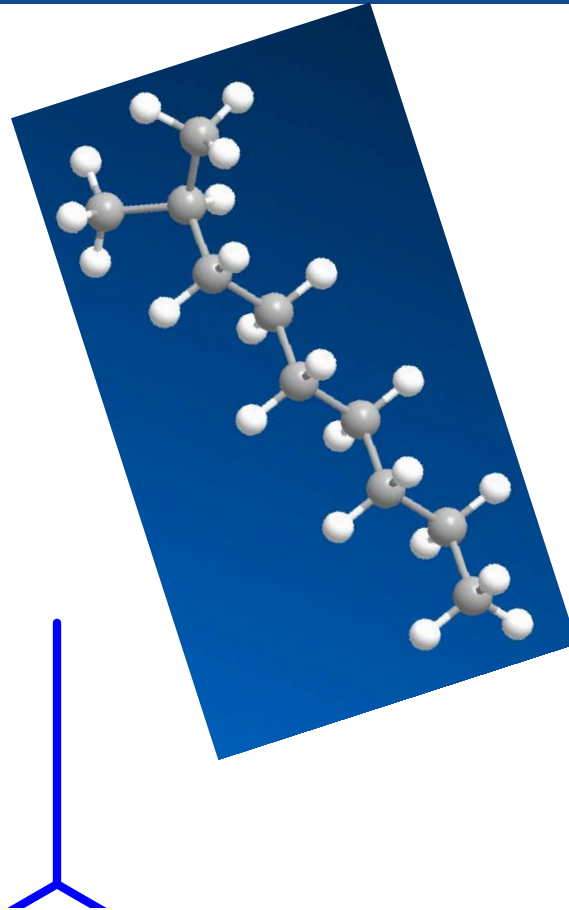
# In general, 2-methylalkanes show less negative temperature coefficient (NTC) behavior than n-alkanes



# At rich conditions, n-alkanes show chain-length reactivity sensitivity



# As mechanisms continue to grow in sophistication, the application of these mechanisms becomes more computationally intensive



Includes all 2-methyl alkanes up to C20 which covers the entire distillation range for gasoline and diesel fuels

Built with the same reaction rate rules as our successful iso-octane and iso-cetane mechanisms.

**7,900 species**  
**27,000 reactions**

**With full (non-sparse) solvers, numerical cost scales with the (# of Species)<sup>3</sup>**





# Solving detailed chemical kinetics combined with 3D fluid dynamics is computationally (and financially) expensive!

## Current state-of-the-art mechanism

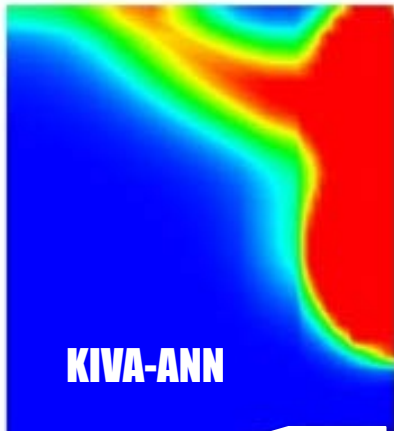
- 7900 species needed for the elementary reaction mechanism for 2-methyl alkanes (Sarathy *et al.* 2010)
- 2M-10M fluid cells for full 3D cylinder model (2010, CERFACS/IFP)

## Fully-coupled computation cost: 42,000 Pflop

- If the fastest computer in the world was ideally utilized:
  - **30 hrs on Jaguar (ORNL)** – 240,000 core 1.76 Pflop/s  
(Number 1 on Top500 supercomputer list)
- **60 years on a workstation** – six core AMD Opteron 100 Gflop/s

Combustion chemistry computational cost is the biggest barrier to complete physics-based simulation suitable for engine design.

# We seek to bring the most physically accurate combustion models for the lowest cost



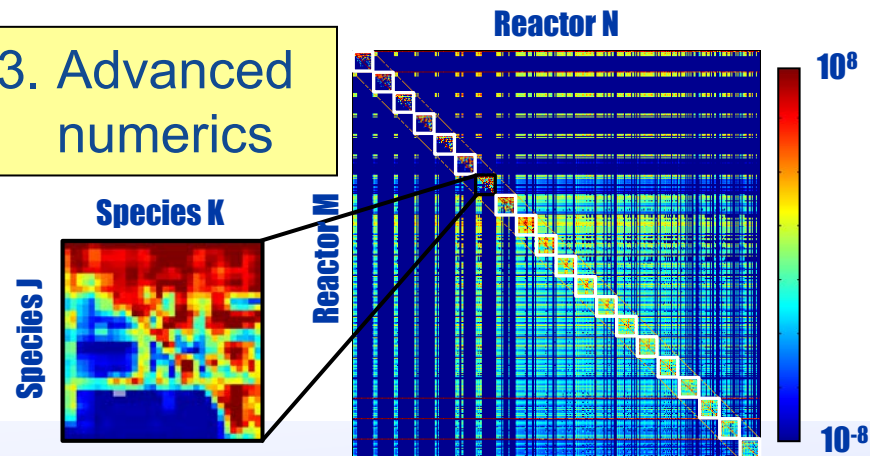
2. New computing architecture



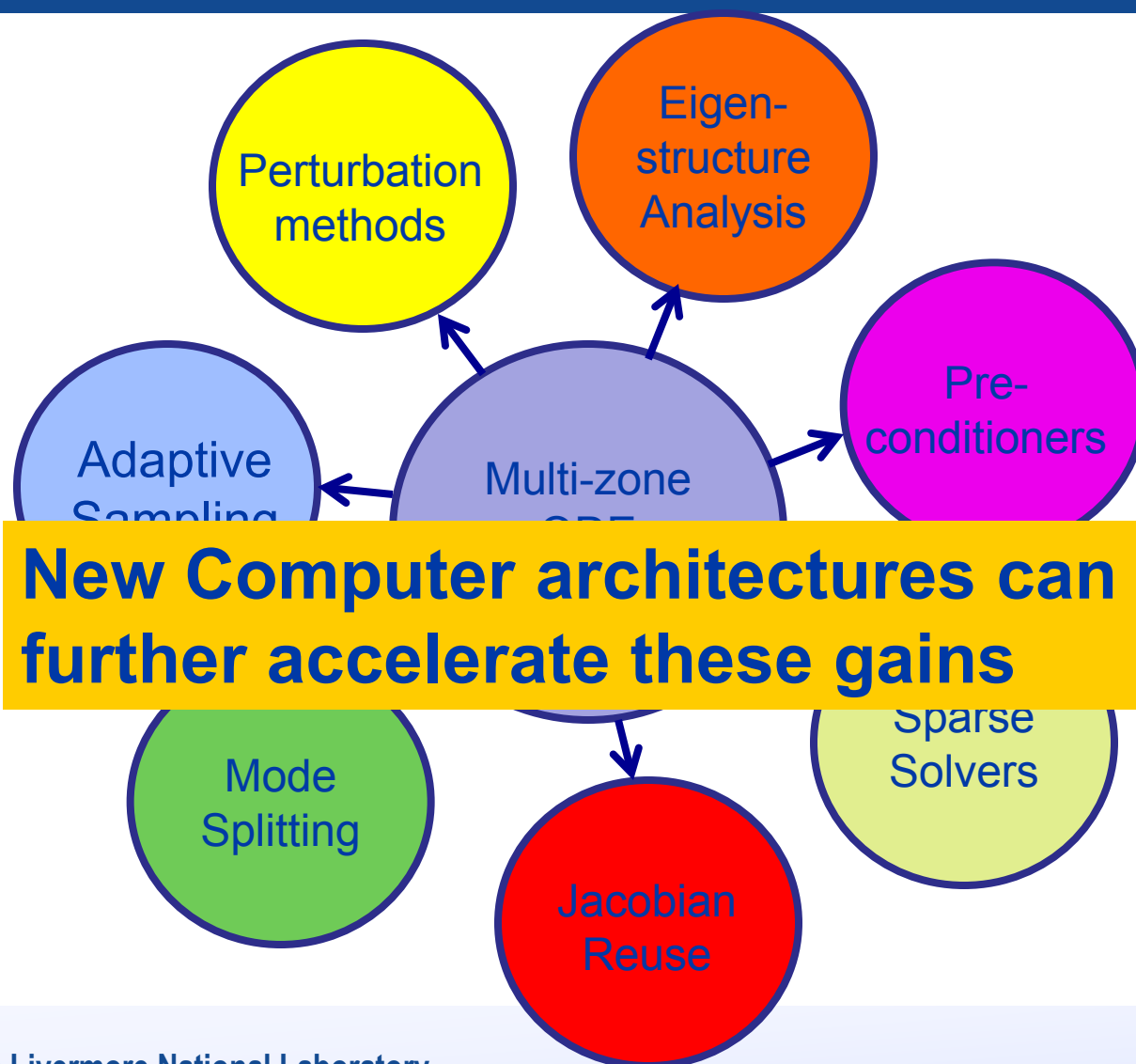
NVIDIA GTX480

1. Lower-cost models:
- Reduced Mechanisms
  - ANN Ignition Integral

3. Advanced numerics



# Opportunities for 1000x speedup in computational chemistry cost through applied mathematics



# We seek to bring the most physically accurate combustion models for the lowest cost



2. New computing architecture

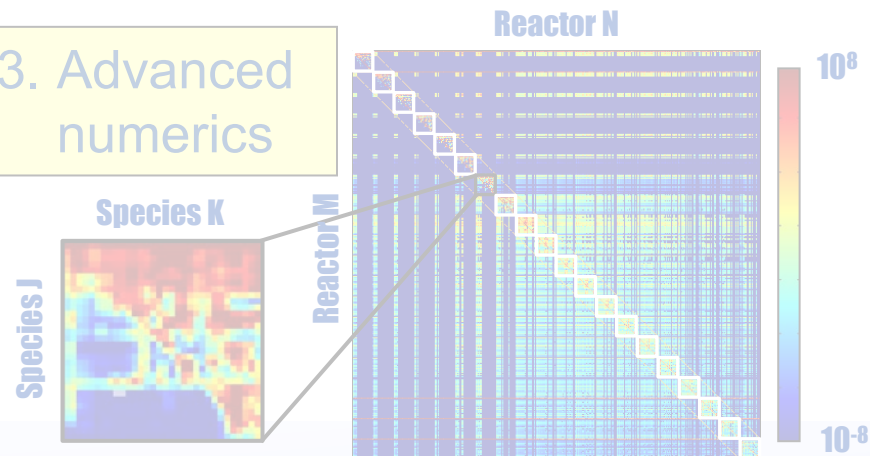


NVIDIA GTX480

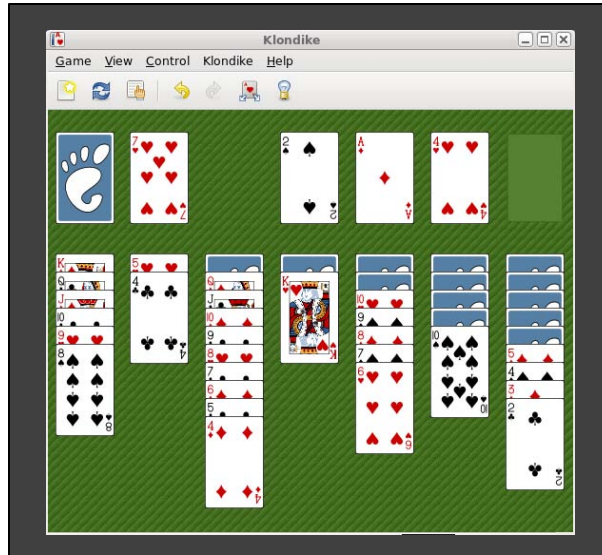
1. Low-cost models:

- Mechanism Reduction
- ANN Ignition Integral

3. Advanced numerics



# General Purpose Graphical Processing Units (GPGPUs) bring Tflop/s computing power to the desktop

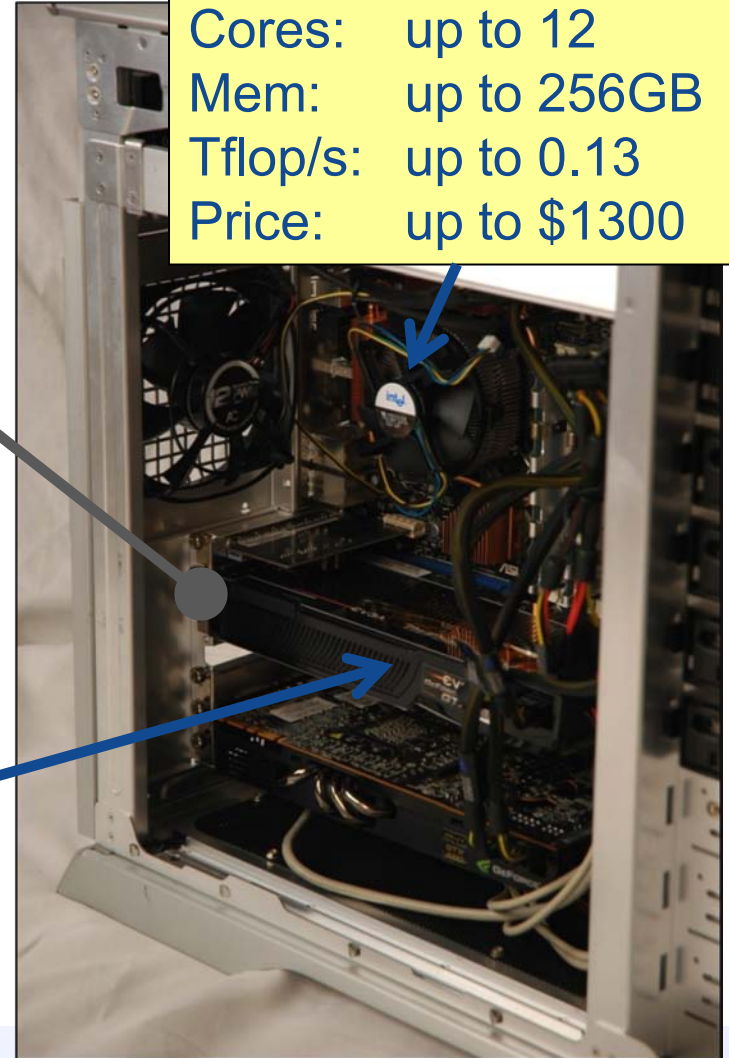


Originally used for  
graphics intensive  
applications:

video games

CPU: Intel/AMD  
Cores: up to 12  
Mem: up to 256GB  
Tflop/s: up to 0.13  
Price: up to \$1300

GPU: NVIDIA GTX 480  
Cores: 480  
Mem: 1.5 GB  
Tflop/s: 1.35  
Price: \$500



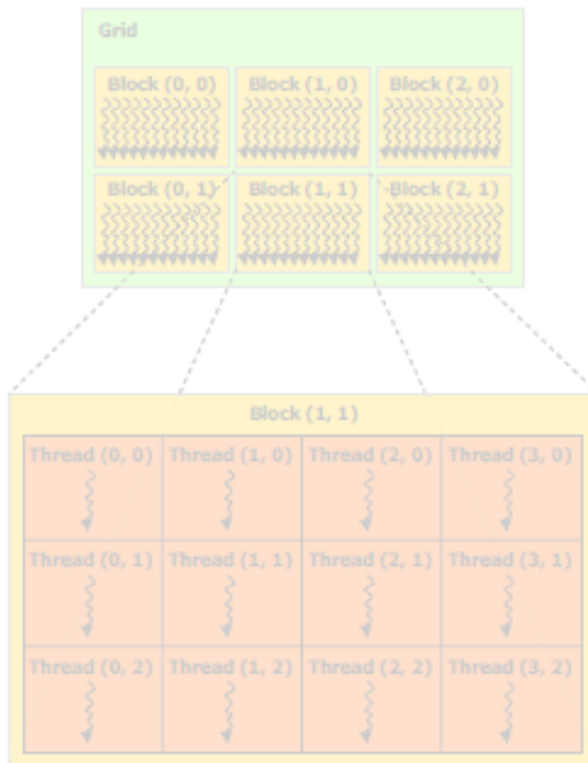
# NVIDIA's Compute Unified Device Architecture (CUDA) has made computational science on the GPU viable

- **GPUs are now programmed with a simple extension to the C language:**
  - New Fermi line offers full C++ support.
  - NVIDIA currently provides free compilers, debuggers and code profilers for all platforms (Linux, Mac and Windows).
  - 3rd party wrappers for most languages (Python, FORTRAN, etc.).
- **Best algorithms have high arithmetic intensity (i.e. many mathematical operations per memory access):**
  - Researchers performing N-body simulations were early adopters (molecular dynamics and astrophysics).
  - Routinely reached +100x speedup.
- **Computational science on the GPUs was in the news recently:**
  - Georgia Tech Research Institute used GPUs to crack passwords.
  - Recommend 12-character random passwords to beat today's GPUs.



# GPU architecture and memory controllers require fine-scale parallelism for best performance

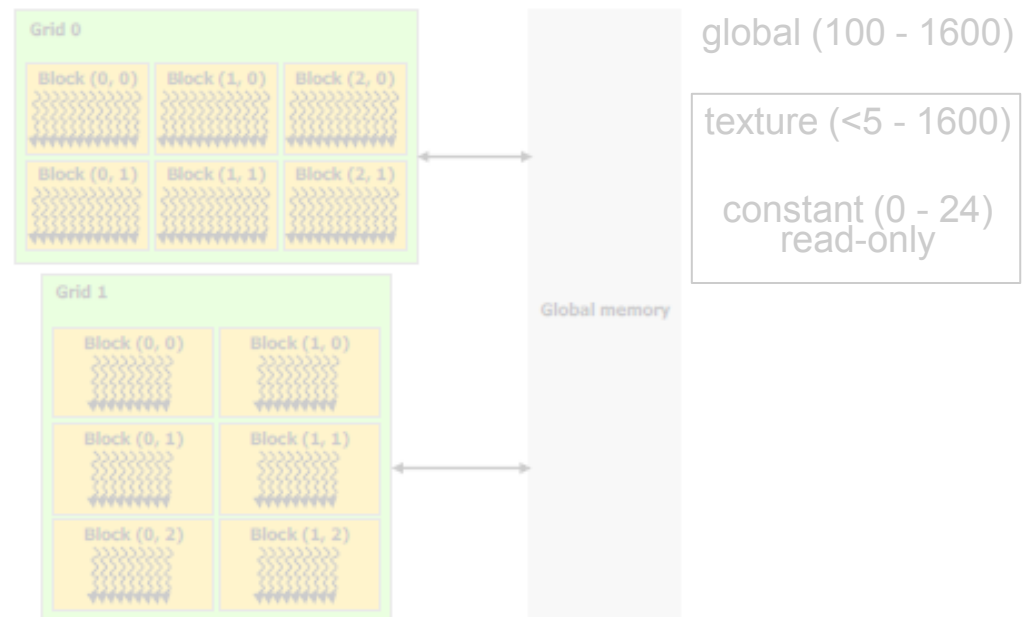
Each function (kernel) executes N times for N threads organized in a compute grid of independent thread blocks:



- Images from NVIDIA's [CUDA C Programming Guide Version 3.1](#), 2010.

Mem  
Threa

**Optimal GPU algorithms are designed to exploit the fast shared memory**

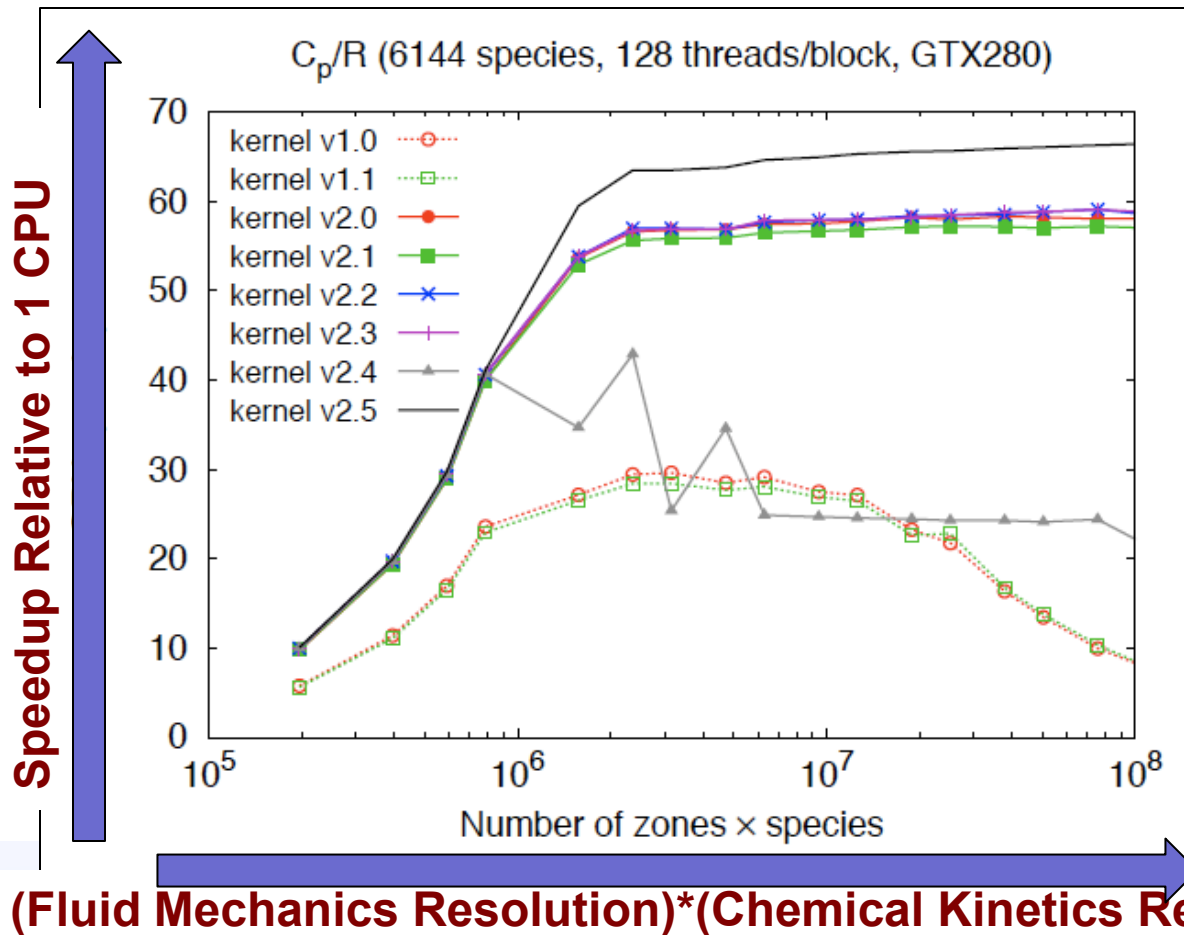


# Evaluation of thermodynamic properties highlights the algorithm design considerations for the GPU

$$\frac{C_p}{R} = \begin{cases} a_1 + a_2\eta + a_3\eta^2 + a_4\eta^3 + a_5\eta^4 & \text{if } \eta \leq \eta_m \\ a_8 + a_9\eta + a_{10}\eta^2 + a_{11}\eta^3 + a_{12}\eta^4 & \text{if } \eta > \eta_m \end{cases}$$

← Low Temperature Polynomial (T<1000K)

← High Temperature Polynomial (T>1000K)



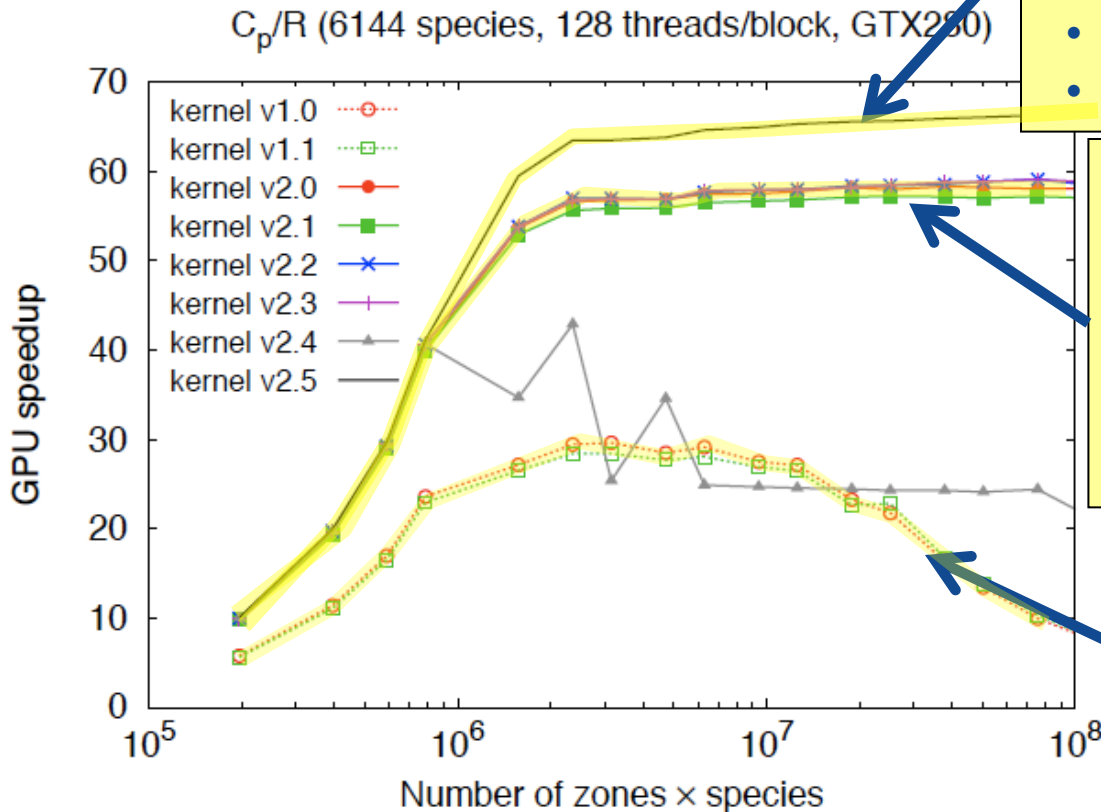


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## Further optimization

- 65x speedup
- Every thread calculates both temperature branches.
- Only assignment is conditional.
- No thread divergence.



## GPU specific coding

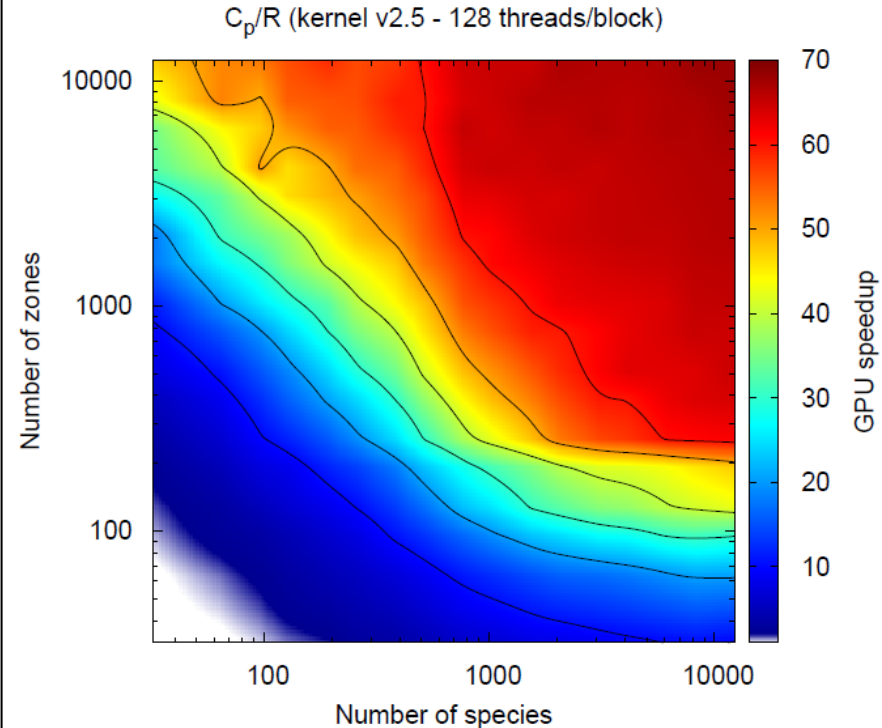
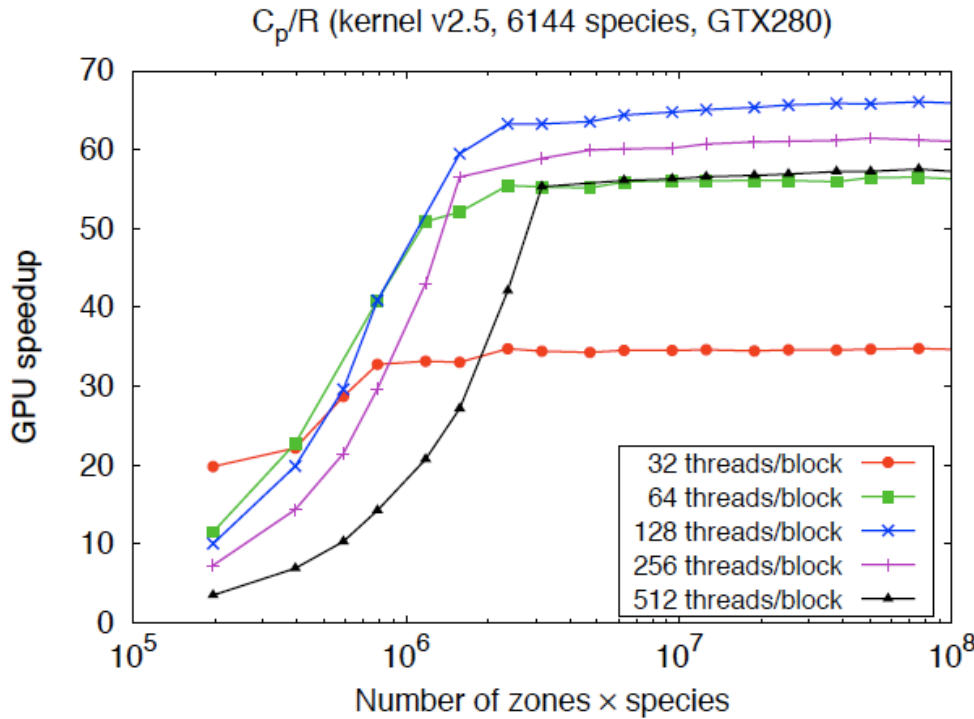
- Load  $a_i$  in shared memory
- Peak speedup 55x with no size limit on performance
- Load strategies and variable reuse have minor impact

## Conventional CPU coding

- No shared memory
- Peak speedup limited to less than 30x

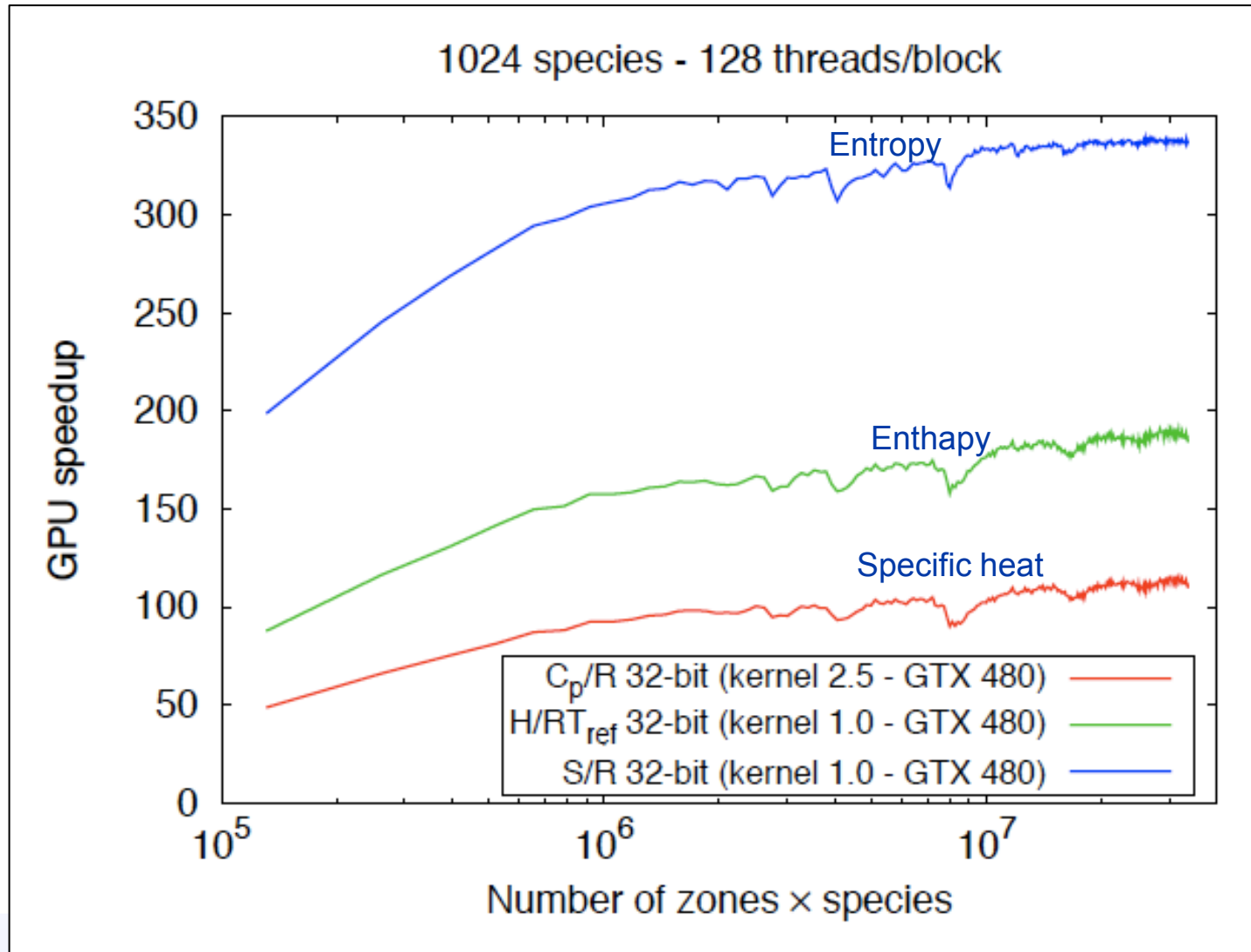


# Peak GPU performance is a balance between shared memory reuse and multiprocessor occupancy



- More threads per block: produces greater shared memory reuse between cooperating threads.
- Fewer threads per block: allows more independent blocks to be placed on a multiprocessor effectively hiding memory latency.

# Enthalpy and entropy calculations have greater speedup, benefiting from more arithmetic operations per memory access



# GPUs are a growth area for bringing scientific computing capability to the desktop

- 64 bit “no-fun” GPU’s being developed for scientific computing
- Democratizing architecture for large-scale computing:
  - Enable greater physics for engineering design
- Puts greater emphasis on programming and numerical methods for effective utilization



# We seek to bring the most physically accurate combustion models for the lowest cost



2. New computing architecture

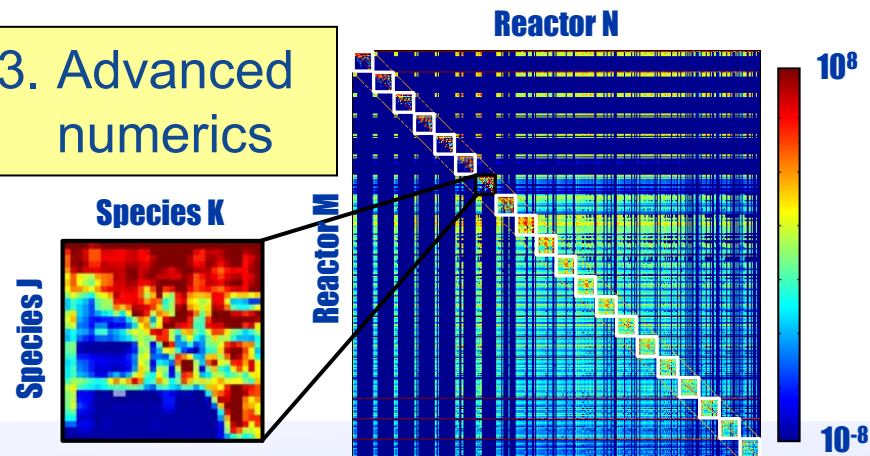


NVIDIA GTX480

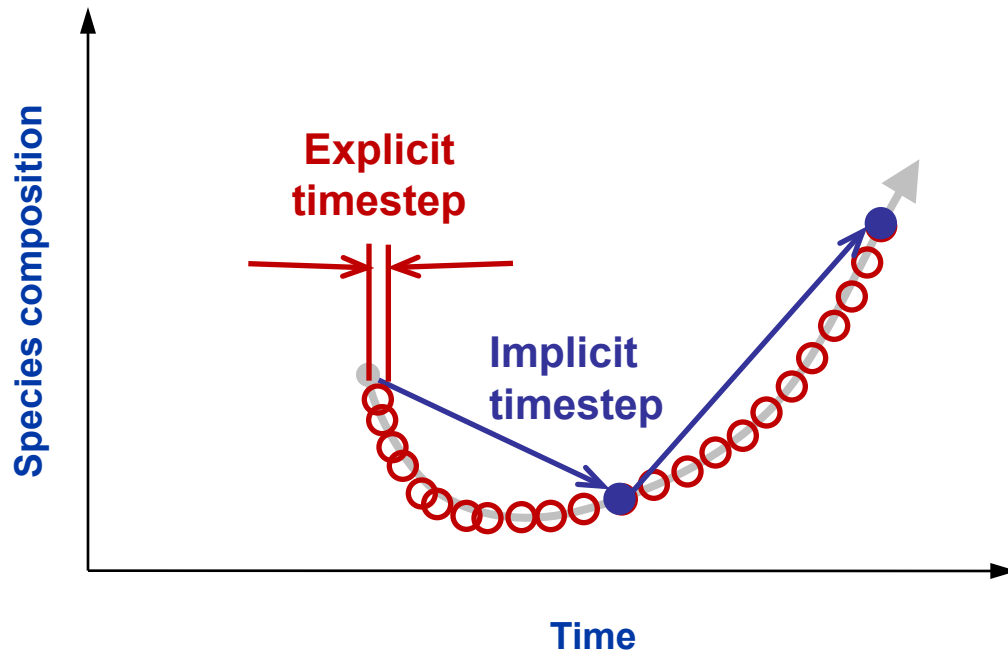
1. Low-cost models:

- Mechanism Reduction
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# Implicit methods are necessary to integrate the chemical time scales over an engine cycle



**Explicit Update**  
(lower cpu/step)

$$\begin{aligned}\frac{\partial x_1}{\partial t} &= f_1(t, x_1, \dots, x_N) \\ \frac{\partial x_2}{\partial t} &= f_2(t, x_1, \dots, x_N) \\ &\vdots \\ \frac{\partial x_N}{\partial t} &= f_N(t, x_1, \dots, x_N).\end{aligned}$$

**Implicit Update**  
(more trajectory data)

$$J = \begin{pmatrix} \frac{\partial f_1}{\partial x_1} & \frac{\partial f_1}{\partial x_2} & \dots & \frac{\partial f_1}{\partial x_N} \\ \frac{\partial f_2}{\partial x_1} & \frac{\partial f_2}{\partial x_2} & & \frac{\partial f_2}{\partial x_N} \\ \vdots & & \ddots & \vdots \\ \frac{\partial f_N}{\partial x_1} & \frac{\partial f_N}{\partial x_2} & \dots & \frac{\partial f_N}{\partial x_N} \end{pmatrix}$$

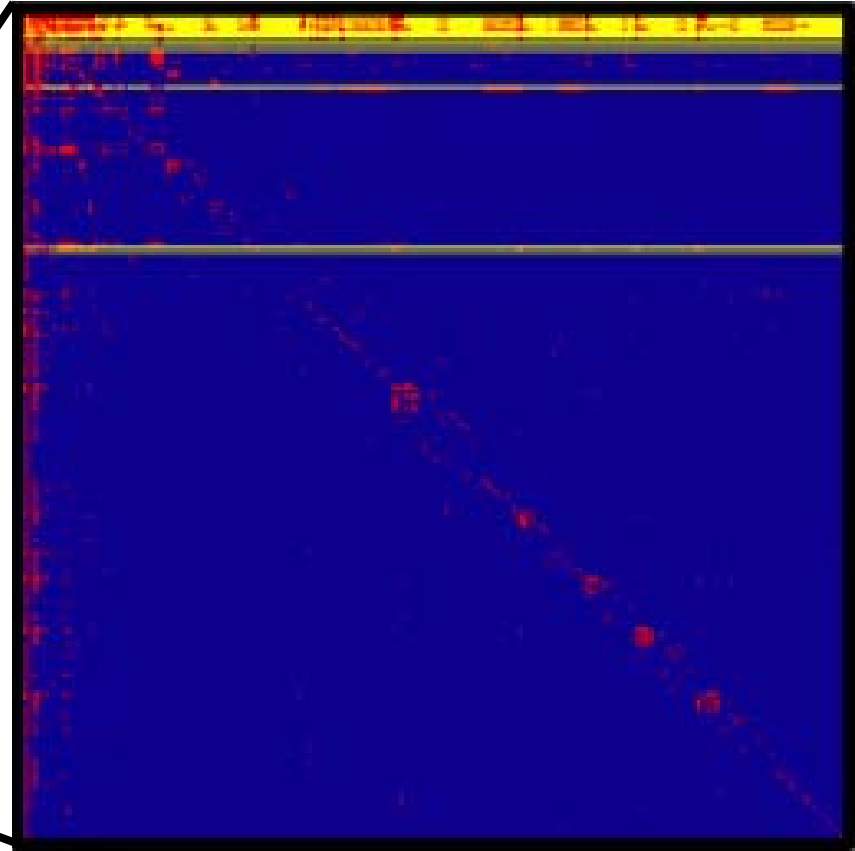
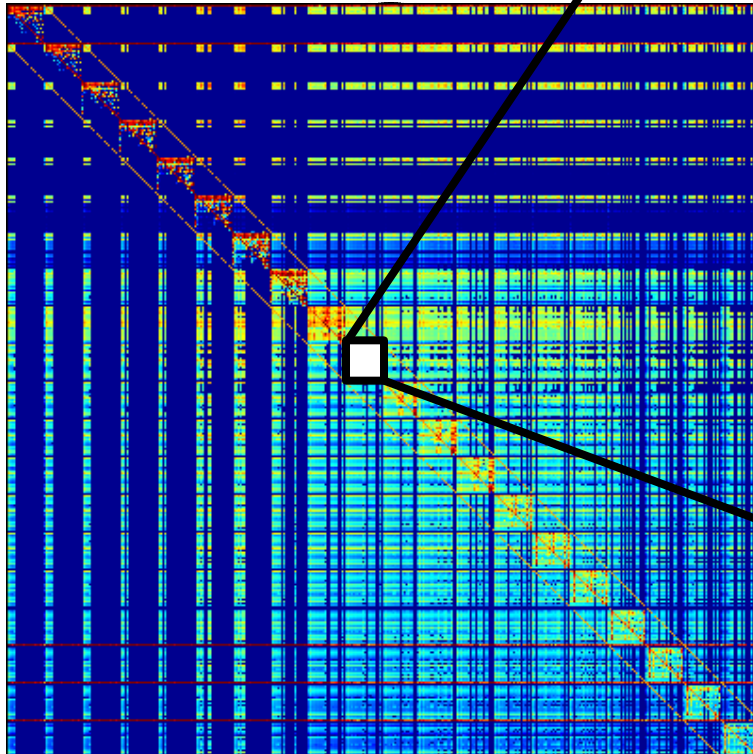
During ignition:

$$\Delta t \text{ (explicit)} = 10^{-12} \text{ to } 10^{-15} \text{ s}$$

$$\Delta t \text{ (implicit)} = 10^{-6} \text{ to } 10^{-8} \text{ s}$$

# Jacobian construction/solution is more than 95% of the simulation cost – a big speedup is possible with smart solvers

Block Diagonal Jacobian  
Multizone 10x-100x faster



Sparse Solver w/o 3<sup>rd</sup> body  
Single reacting zone +6x faster



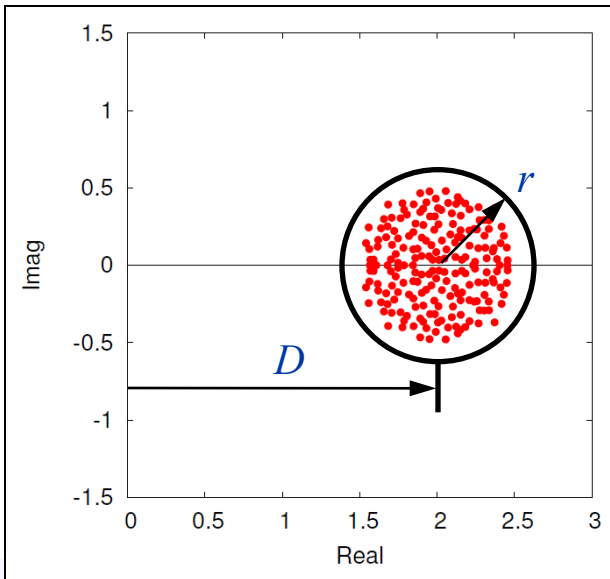
# Approximate Jacobians can be used to precondition iterative linear system solvers like GMRES

## Generalized Minimal RESiduals

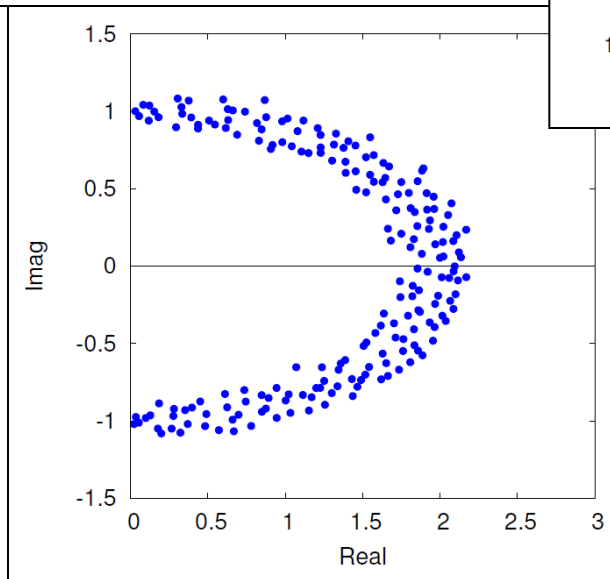
$$E^{(n)} = \frac{\|Ax^{(n)} - b\|_2}{\|b\|_2} \leq \Lambda^n \text{cond}(V)$$
$$\Lambda \approx \frac{r}{D}$$

## Eigenvalue Spectra (200 x 200)

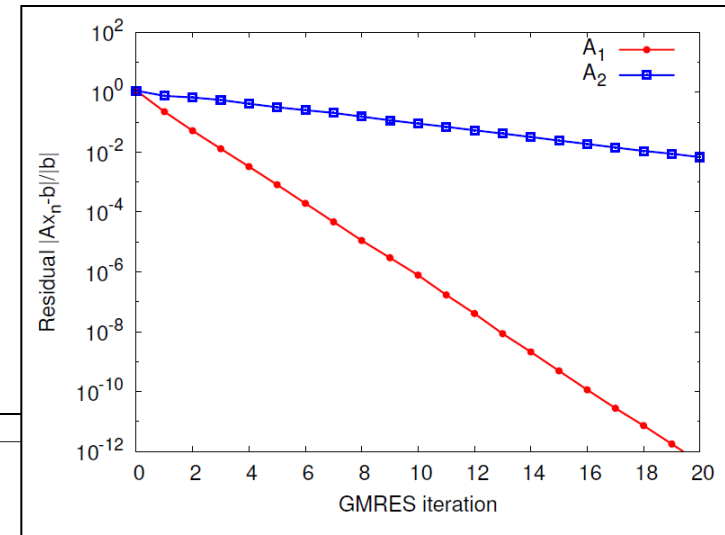
**A<sub>1</sub>: fast convergence**



**A<sub>2</sub>: slow convergence**

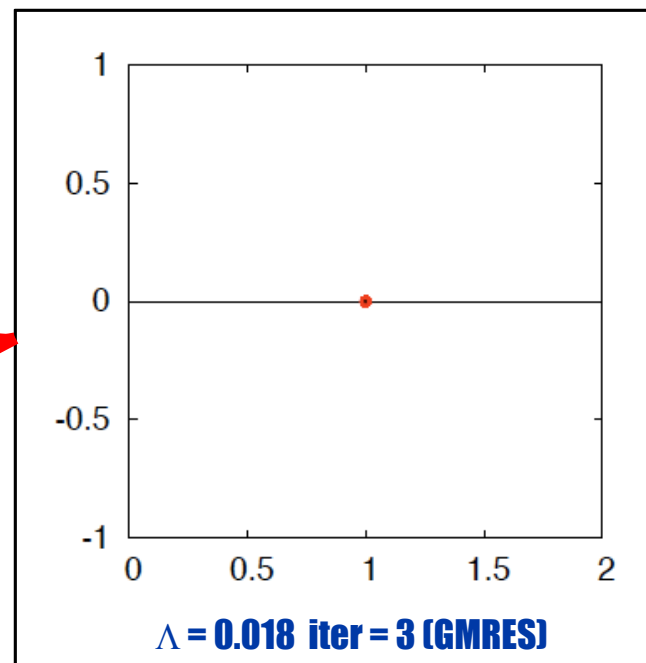
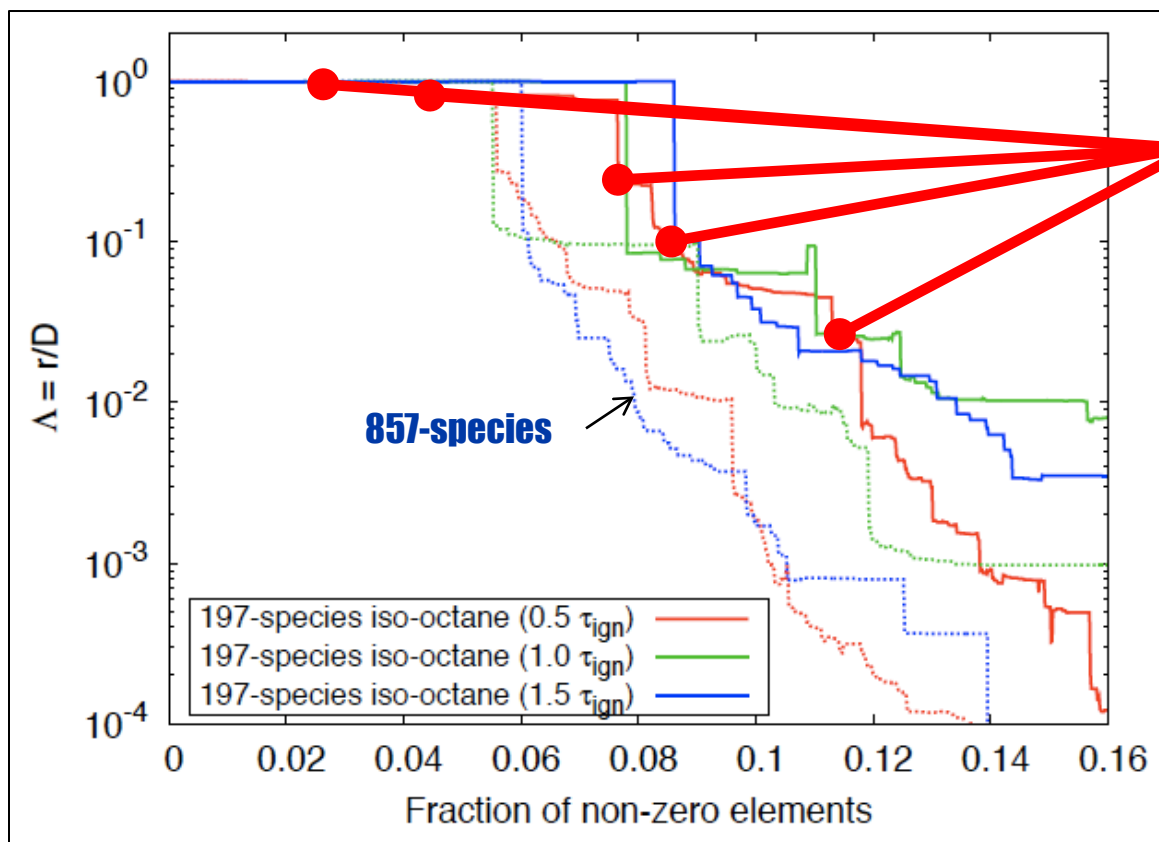


## GMRES Error





# Direct reaction sorting shows promise to be a general low-cost preconditioner for the Jacobian



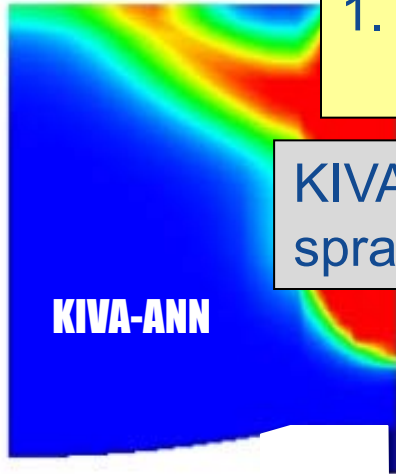
# Chemical mechanisms continue to evolve, adding more a more compounds that are present in real fuels

- Develop detailed chemical kinetic models for another series iso-alkanes:  
3-methyl alkanes
- Validation of 2-methyl alkanes mechanism with new data from shock tubes, jet-stirred reactors, and counterflow flames
- Develop detailed chemical kinetic models for alkyl aromatics:
- More accurate surrogates for gasoline and diesel
- Further develop mechanism reduction using functional group method

n-decylbenzene - Diesel Fuels



# Continued improvement of physical models and numerical methods will enable utilization of large mechanisms



1. Low-cost models

KIVA4+ANN and spray models

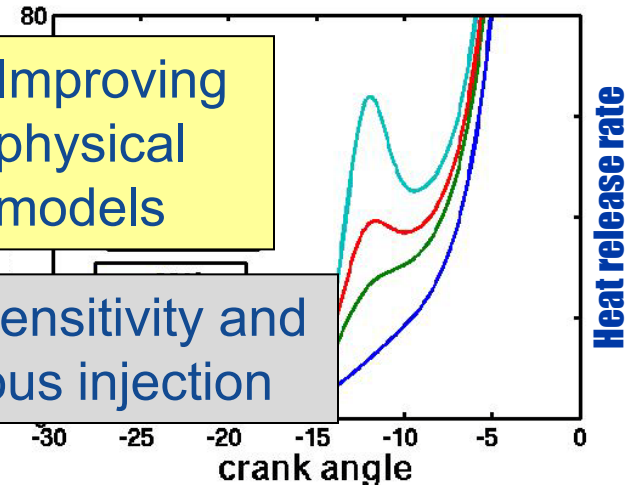
3. New computing architecture

GPU compute tiles for efficient species production rates

NVIDIA GTX480 image:  
[http://www.nvidia.com/object/product\\_geforce\\_gtx\\_480\\_us.html](http://www.nvidia.com/object/product_geforce_gtx_480_us.html)

2. Improving physical models

LTC sensitivity and gaseous injection



4. Advanced numerics

Combine reaction sort with 2x2 sort

