



SOLAR ENERGY
TECHNOLOGIES OFFICE
U.S. Department Of Energy

ENERGISE Webinar:

Solar to the Max: Innovations in Distribution Grid Planning and Operations

Robust Distributed State Estimator for Interconnected
Transmission and Distribution Networks

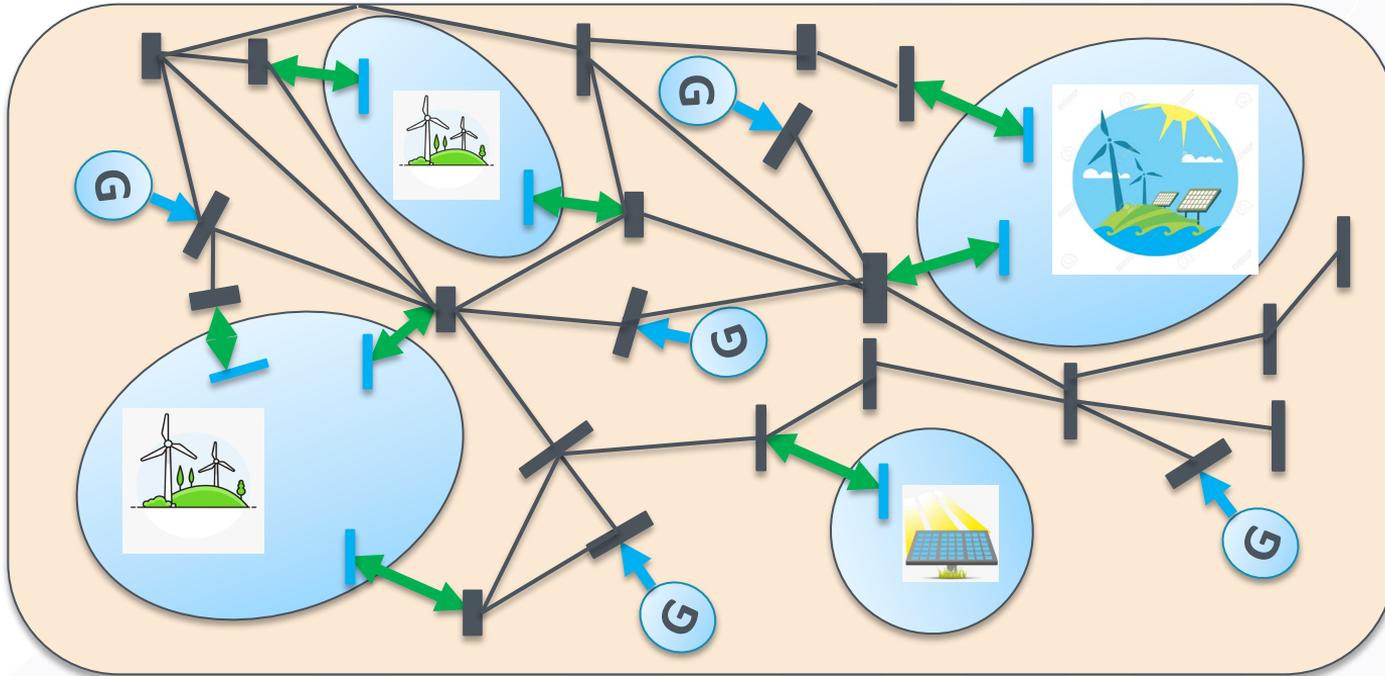
Northeastern University

DE-EE0008005

June 25, 2021

Principal Investigator: Ali Abur (NEU); Sub-contractor: Jianzhong Tong (PJM)
Other Contributors: Andre Langner, David Kelle, Ramtin Khalili (PhD students @NEU)

The goal: develop a state estimator for monitoring transmission and distribution systems simultaneously.



TRANSMISSION SYSTEMS

Established real-time monitoring
and control practices

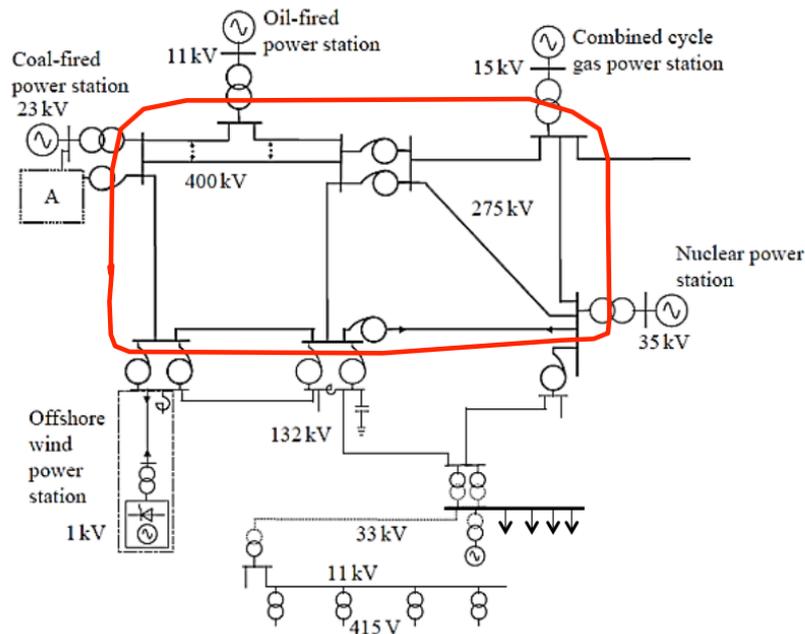
SCADA measurements

Monitored by SE introduced by

Schweppe in 1970

Balanced operation, + seq. model

Transmission Systems (230 – 750 kV)



DISTRIBUTION SYSTEMS

Radial / Meshed networks

Lack of real-time measurements

Distribution Management Systems (DMS)

Smart Grids

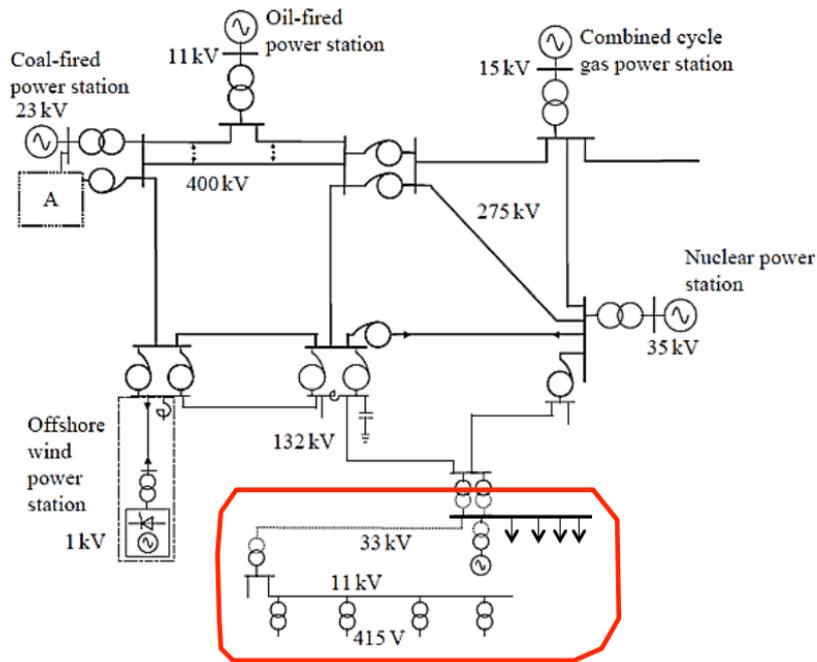
Distributed Generation (DG)

Advanced Measurement Infrastructure

(AMI)

Advanced DMS

Distribution Systems (13 - 33 kV)

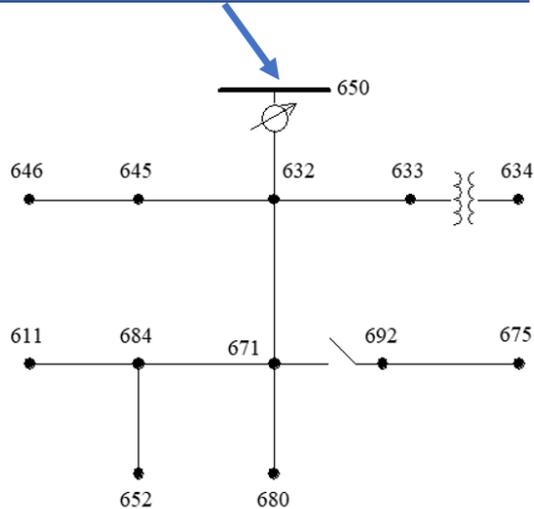


- Challenges / Innovations:

- **3-Phase SE formulation / Choice of a reference**
- Unbalanced operation / Mixed-phase SE
- System size / Scalable solution
- Uneven areas / Optimal system partitioning
- Bad measurements / Robust estimator

CHOICE OF A REFERENCE BUS

$$\theta_{650}^a = 0^\circ \quad \theta_{650}^b = -120^\circ \quad \theta_{650}^c = 120^\circ$$



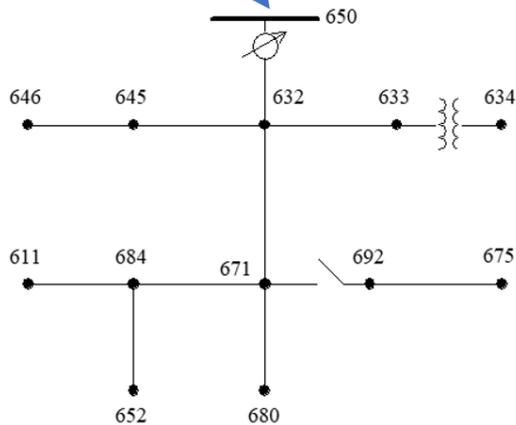
**DEFAULT PRACTICE:
Approach I**

Assume a balanced voltage bus exists

Set the phase angles to 0, 120,-120

Approach II: USE OF A SINGLE-PHASE REFERENCE

$$\theta_{650}^a = 0^\circ \quad \theta_{650}^b = \hat{\theta}_{650}^b \quad \theta_{650}^c = \hat{\theta}_{650}^c$$



Approach II

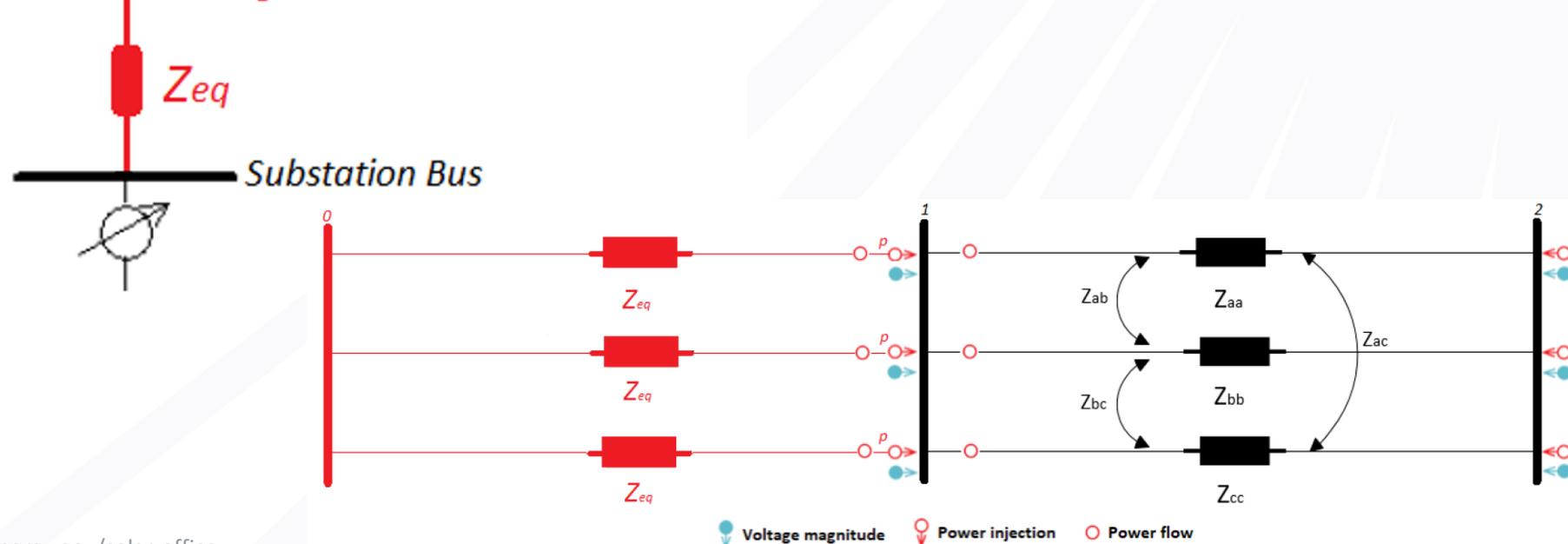
Fix only one phase angle
Estimate the rest of the phases

Approach III: USE OF 3-PHASE BALANCED VIRTUAL BUS

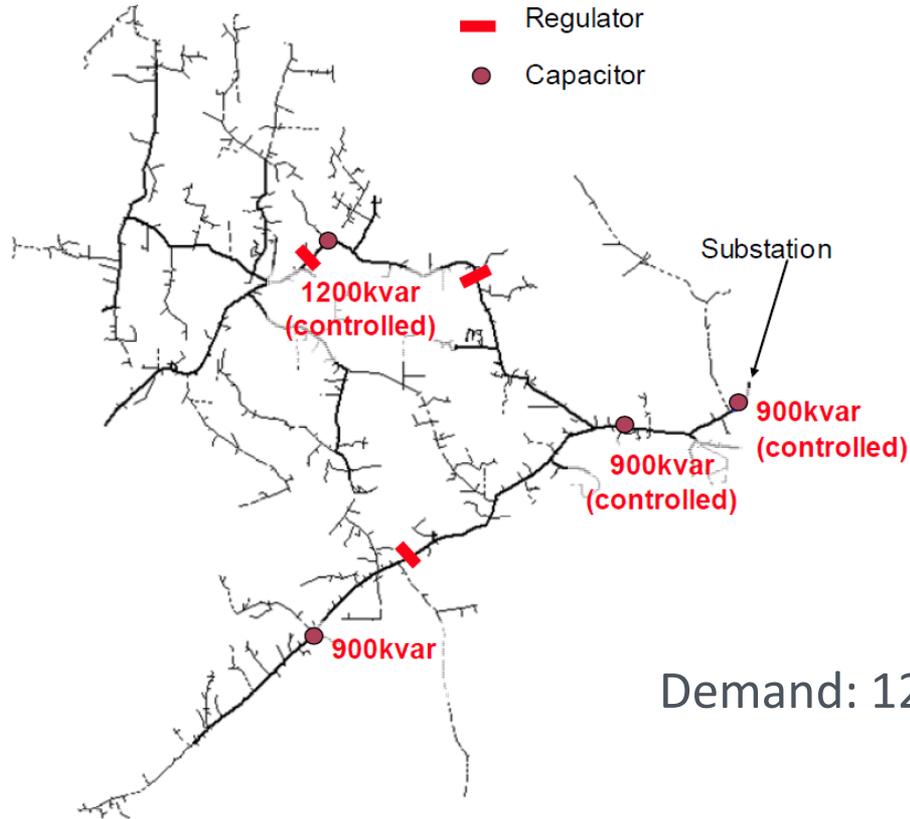
Andre L. Langner and A. Abur, "Formulation of Three-Phase State Estimation Problem Using a Virtual Reference," *IEEE Transactions on Power Systems*, vol. 36, no. 1, pp. 214-223, Jan. 2021.

$$V_0^a = V_0^b = V_0^c$$

$$0 \quad \theta_0^a = 0, \theta_0^b = -120, \theta_0^c = 120$$



8500 NODE DISTRIBUTION SYSTEM



Demand: 12.04 MW and 1.44 MVar

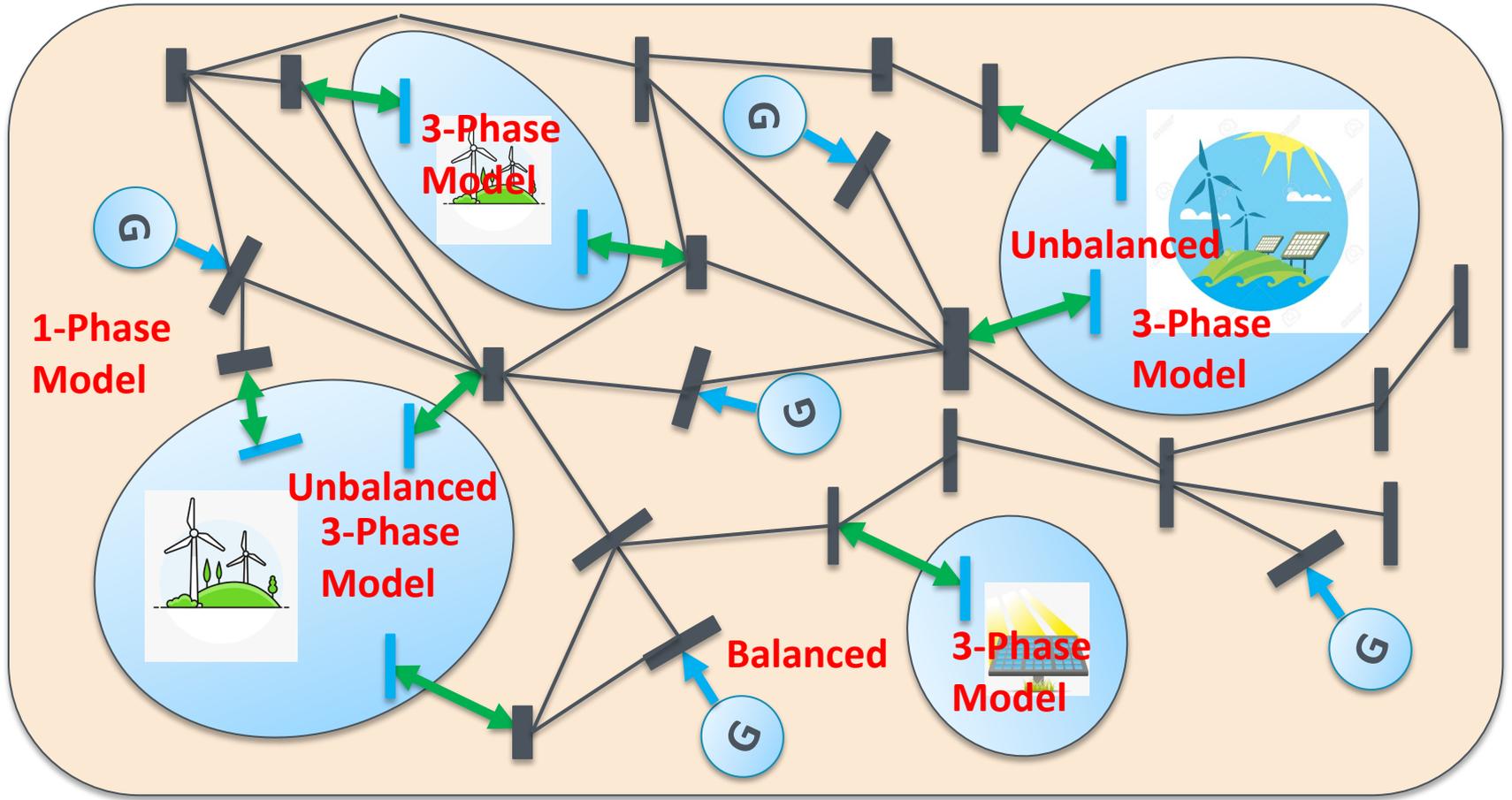
IEEE 8500-NODE DISTRIBUTION SYSTEM

True States	App. I	App. II	App. III
-2.8597°	-2.8597°	-2.8597°	-2.8626°
-122.7995°	-122.8597°	15.7623°	-122.8008°
117.1093°	117.1403°	292.0141°	117.1023°

App.	No Iterations	J-index	Processing Time (s)
I	9	0.0644	26.1323
II	14	0.0609	39.8192
III	9	0.0507	29.4274

■ Challenges / Innovations:

- 3-Phase SE formulation / Choice of a reference
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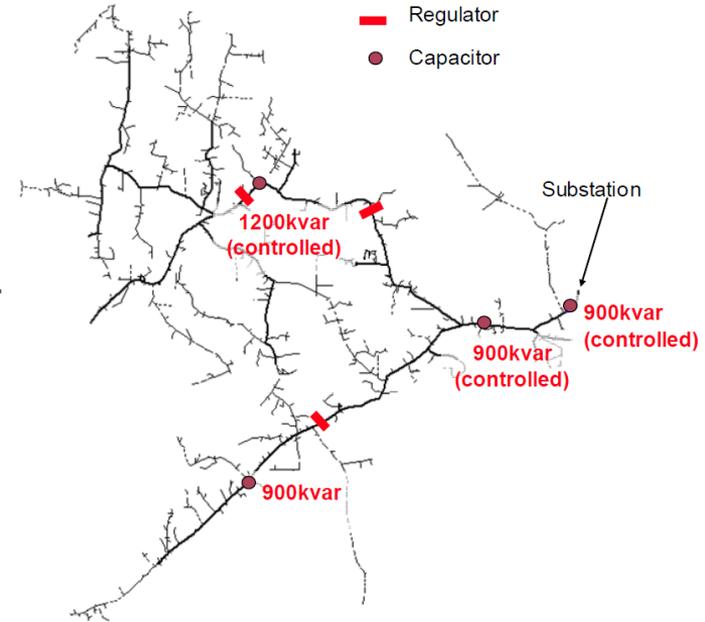


MODELING CHALLENGES: Mixed-phase line sections; Unbalanced DS

Network Data and Measurements

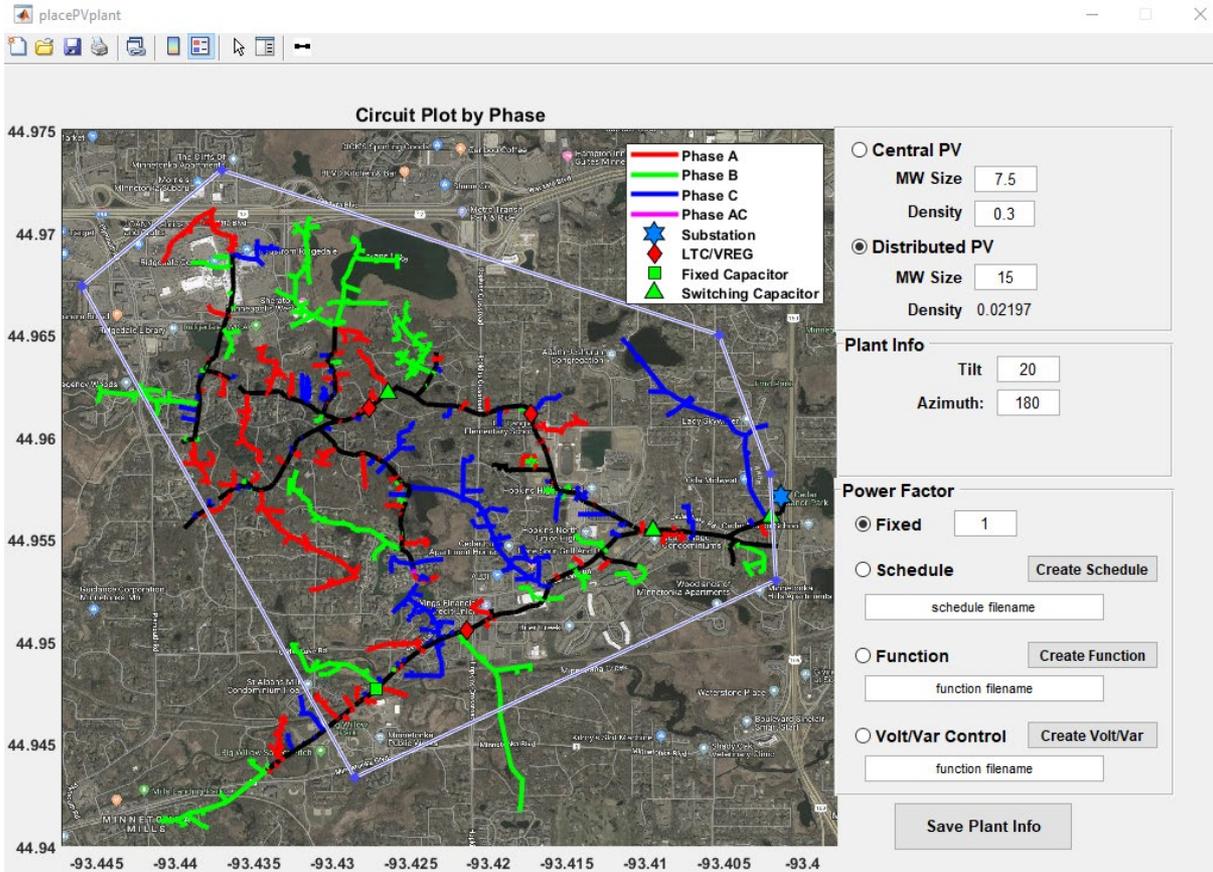
8500 Node System

- GridPV was used to insert solar PVs in the feeder
- Many different scenarios are simulated
- Validation for accuracy and bad data detection



Example Scenario

Solar PVs : 15 MW



State Estimation Results

MSE Values - Scenario 1

Case	V	θ	Combined
Perfect Meas.	2.84×10^{-29}	6.99×10^{-20}	3.49×10^{-20}
Gaussian Noise	2.71×10^{-11}	3.34×10^{-5}	1.67×10^{-5}

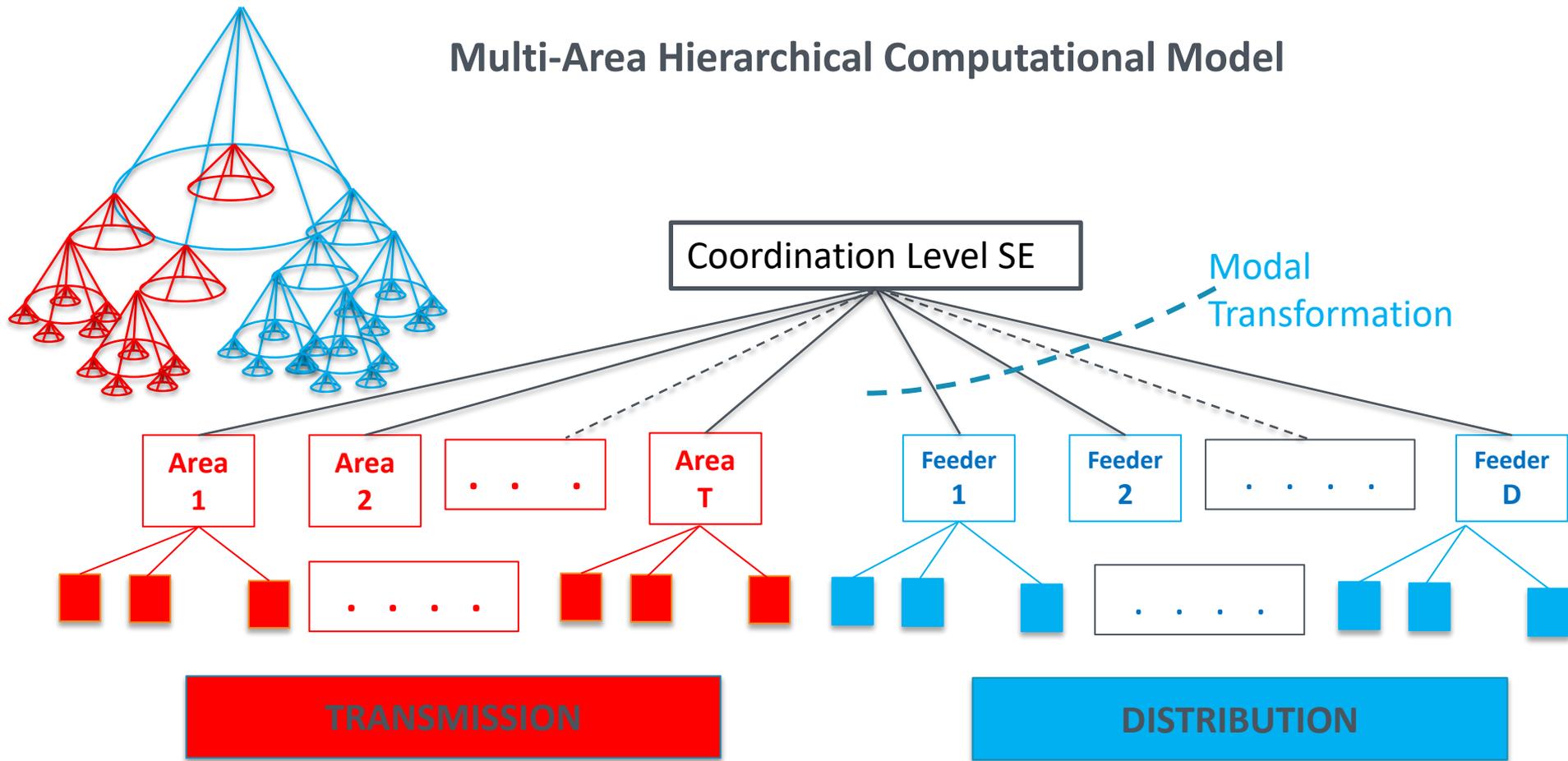
J-index, Convergence, and mean of diag. of G inverse - Scenario 1

Case	J	Iterations	$\text{mean}(\text{diag}(G^{-1}))$
Perfect Meas.	5.83×10^{-13}	4	0.0018
Gaussian Noise	37.98	5	0.0018

■ Challenges / Innovations:

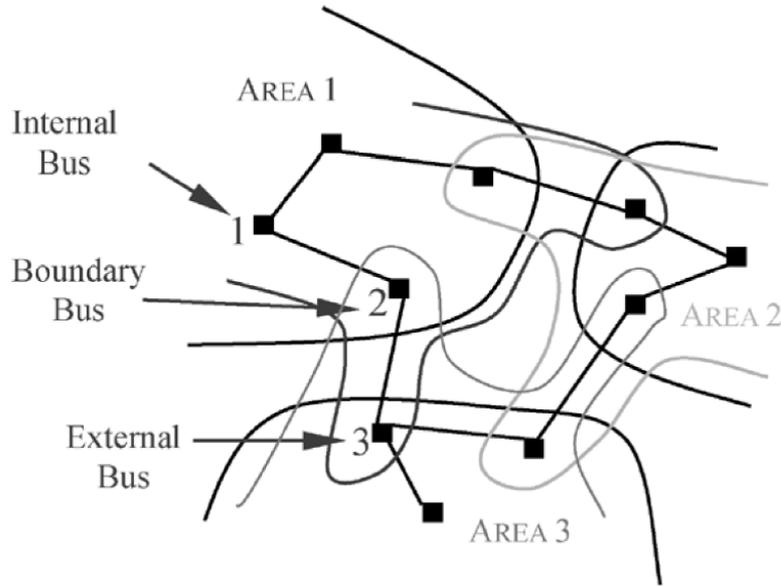
- 3-Phase SE formulation / Choice of a reference
- **Unbalanced operation / Mixed-phase SE**
- **System size / Scalable solution**
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Multi-Area Hierarchical Computational Model



Multi-area State Estimation

Zhao and Abur (2005) Multiarea State Estimation Using Synchronized Phasor Measurements



Partition the network into non-overlapping areas

Identification of buses:

- Internal
- Boundary
- External

Two-Level Computation Framework

Ren and Abur (2018) Obtaining Partial Solutions for Divergent State Estimation Problems in Large Power Systems

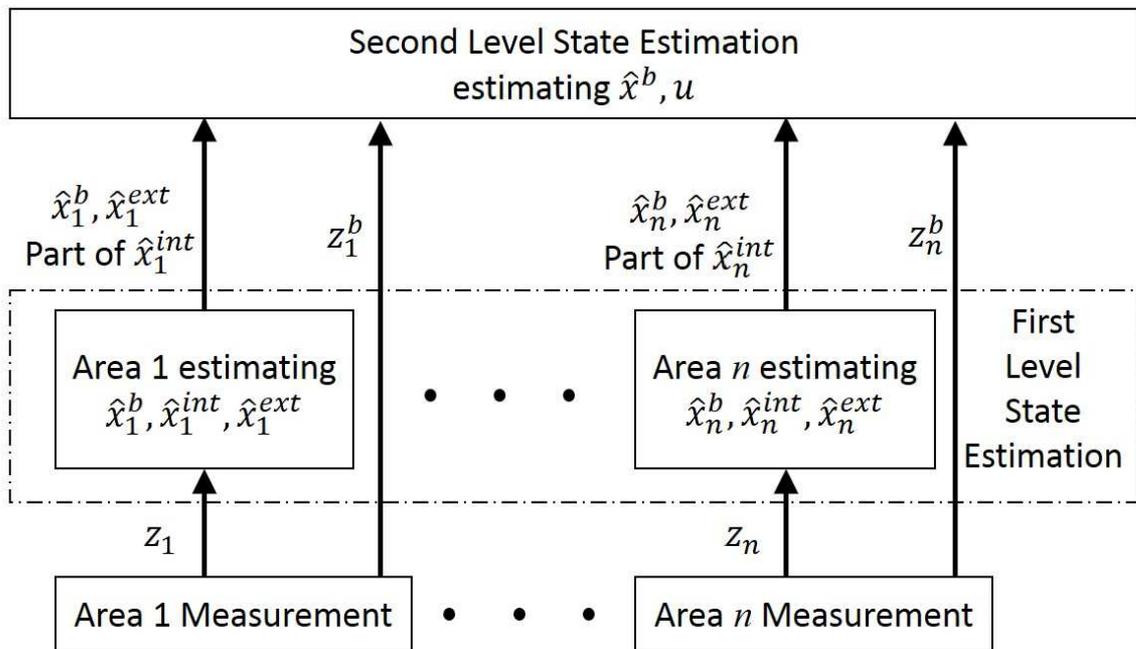
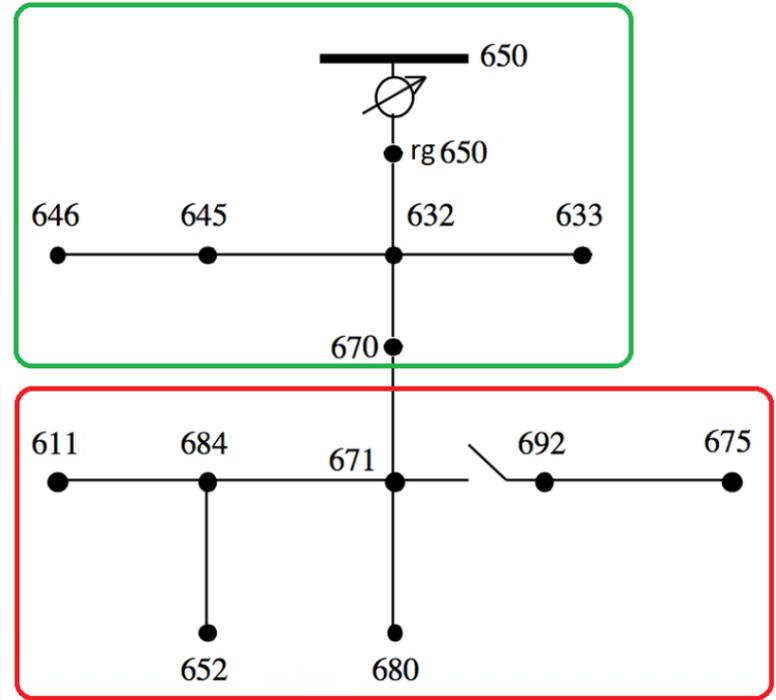
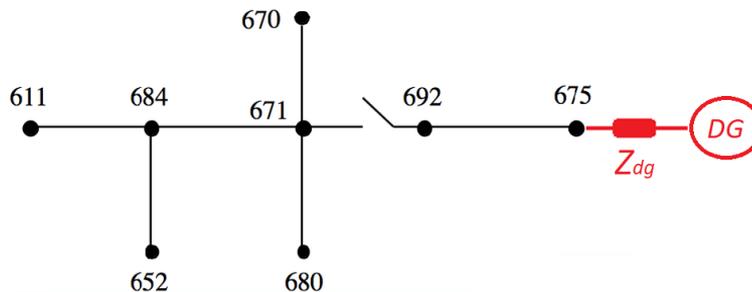
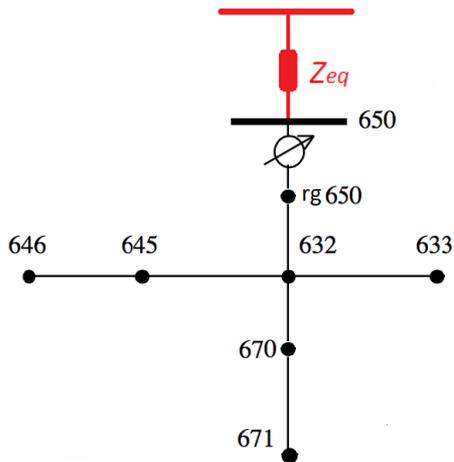


Illustration on a Distribution System

- Multi-phase Solution
- Scalable to large networks
- Parallel processing

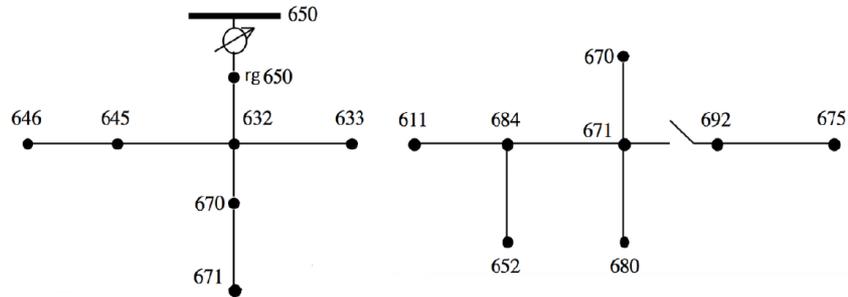


Use of a Virtual Bus

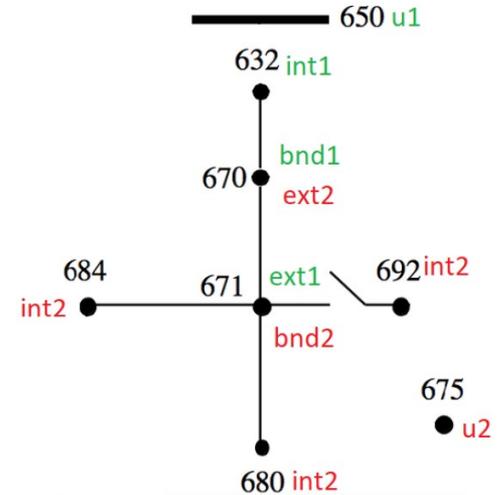


Two-stage Solution

Stage 1 – Individual areas



Stage 2 – Coordination



PJM Transmission Model Details

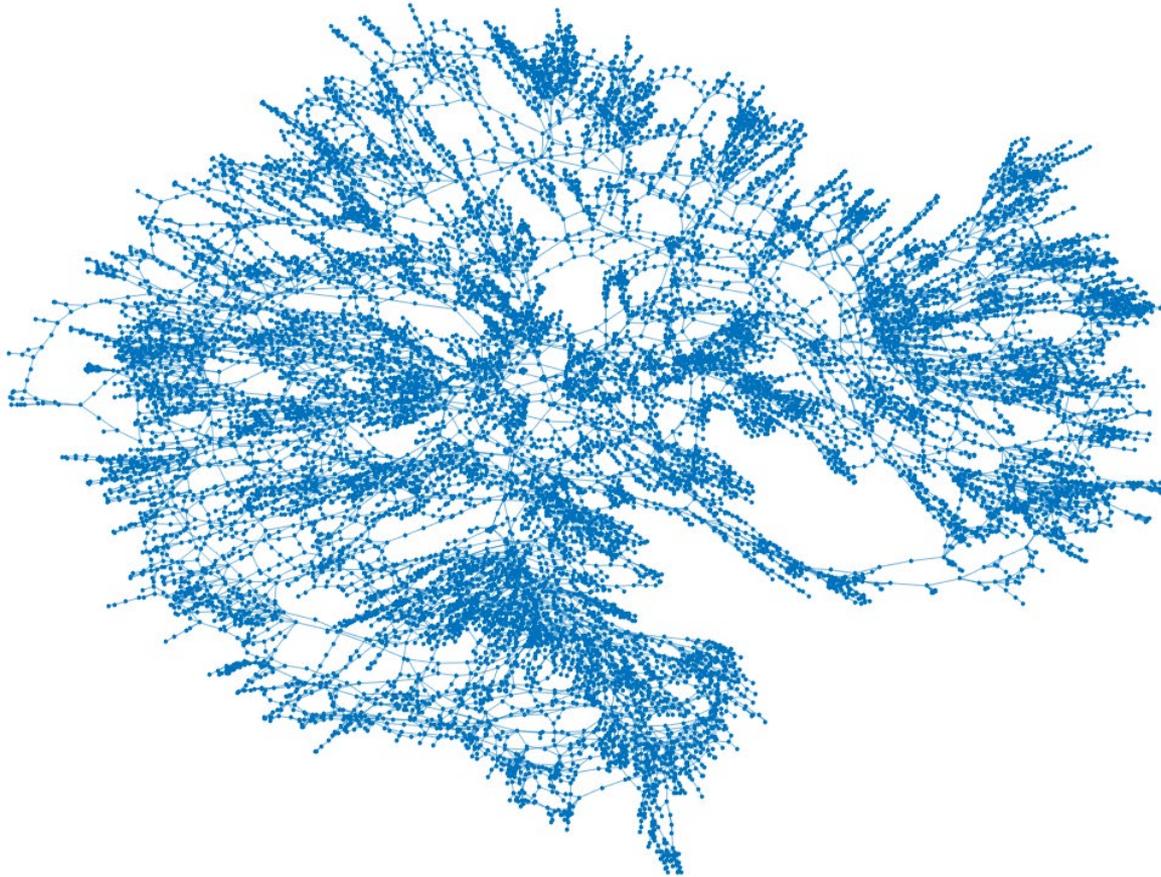
System Overview

Component	Number
buses:	14207
loads:	7598
on	7598
off	0
fixed	7594
dispatchable	4
generators:	2574
on	1001
off	1573
shunt elements:	1238
branches:	19248
areas:	2

Generation and Loads

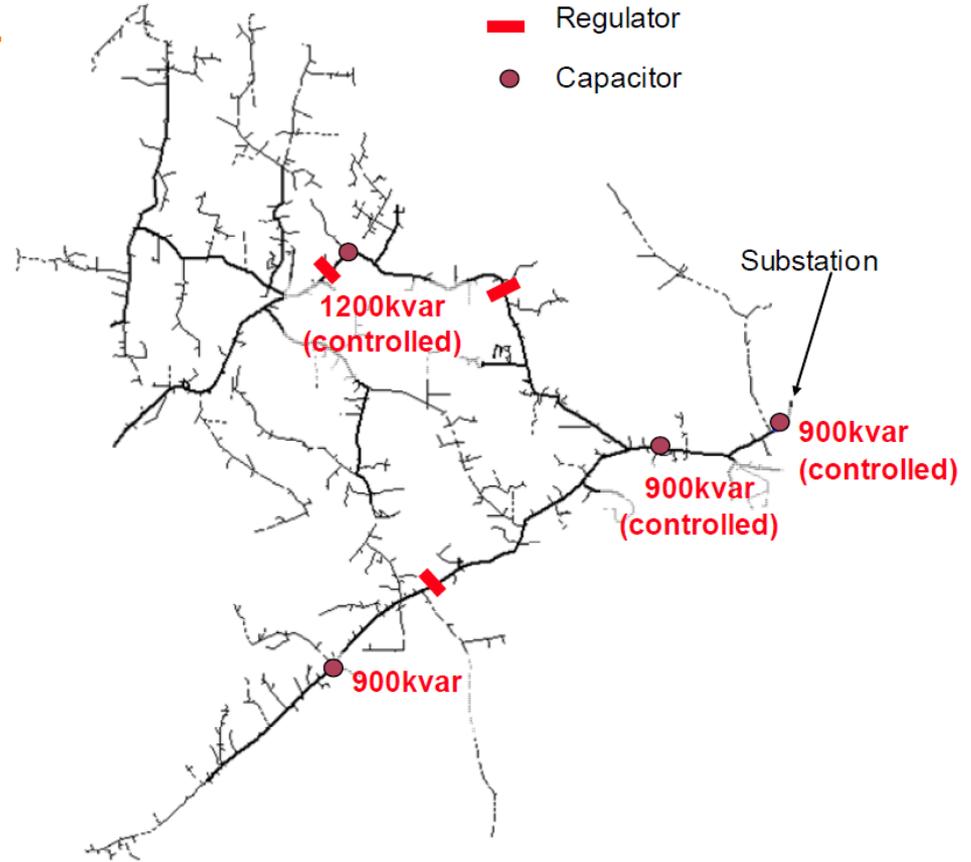
Type	Active (MW)	Reactive (MVar)
total dispatched loads:	217431.8	36528.6
fixed	217405.7	36600.6
dispatchable	26.1	-72.0
total curtailed loads:	0	292.0
total nominal loads:	217431.8	36820.6
on	217431.8	36820.6
off	0	0
fixed	217405.7	36600.6
dispatchable	26.1	220.0
on	26.1	220.0
off	0	0
total dispatched generation:	222850.5	17898.2

PJM Transmission System: ~16K substations



Distribution System

8500 node feeder
GridPV was used to insert
solar PVs in the feeder



Large-scale Testing Configuration

PJM Summer 2017 save case

16K Bus PJM
Transmission
System

Most sensitive
buses selected

Modified 8500-node Feeder -1

Modified 8500-node Feeder-2

Modified 8500-node Feeder-3

Modified 8500-node Feeder-4

Results

Table 22: Level 1 MAT SE MSE Values (Error-Free)

SE	V	θ	Combined
Area 1	2.659×10^{-12}	1.256×10^{-12}	2.084×10^{-12}
Area 2	2.055×10^{-10}	1.553×10^{-10}	1.823×10^{-10}
Area 3	6.525×10^{-11}	7.189×10^{-11}	6.860×10^{-11}

Only the first three areas are shown

Table 23: Level 2 SE Convergence (Error-Free)

SE	J	Iterations
Area 1	1.351×10^{-12}	15
Area 2	1.559×10^{-8}	4
Area 3	2.065×10^{-9}	5

Results

Table 25: Level 2 SE MSE Values (Error-Free)

SE	V	θ	Combined
MAT Coordinator	2.634×10^{-10}	2.479×10^{-10}	2.558×10^{-10}
MDF (Feeder I)	1.211×10^{-7}	1.865×10^{-6}	9.929×10^{-7}
MDF (Feeder II)	5.77×10^{-8}	4.762×10^{-7}	2.67×10^{-7}
MDF (Feeder III)	2.964×10^{-6}	8.653×10^{-5}	4.475×10^{-5}
MDF (Feeder IV)	6.912×10^{-9}	2.622×10^{-7}	1.311×10^{-7}

Table 26: Level 2 SE Convergence (Error-Free)

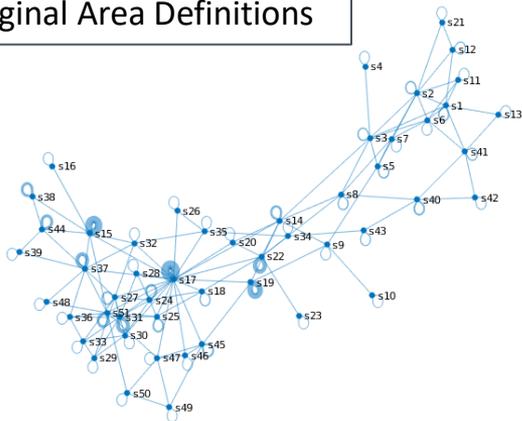
SE	J	Iterations
MAT Coordinator	7.735×10^{-15}	15
MDF (Feeder I)	1.804×10^{-4}	4
MDF (Feeder II)	7.062×10^{-8}	5
MDF (Feeder III)	1.402×10^{-4}	4
MDF (Feeder IV)	1.676×10^{-5}	4

■ Challenges / Innovations:

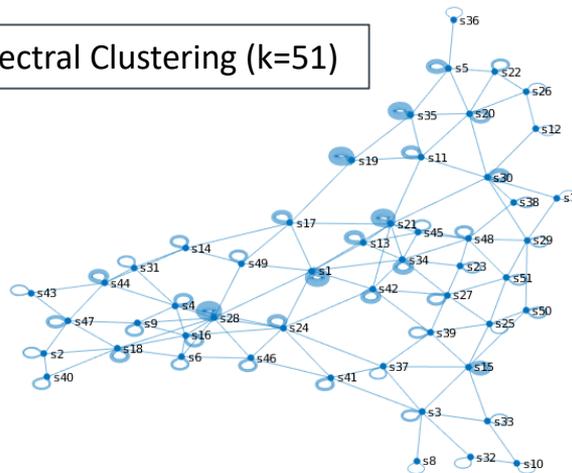
- 3-Phase SE formulation / Choice of a reference
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Partitioning Results

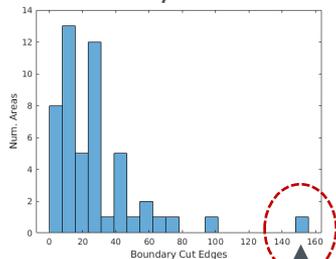
Case 1: Original Area Definitions



Case 2: Spectral Clustering (k=51)

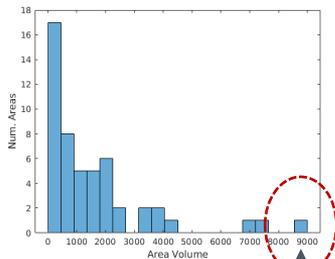


Boundary Branches



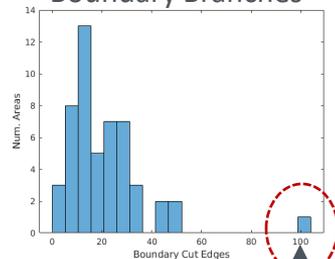
150

Internal Branches



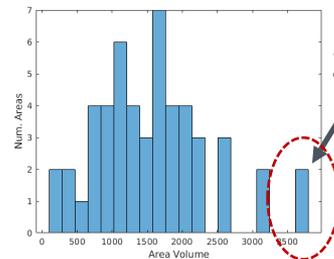
9000

Boundary Branches



100

Internal Branches

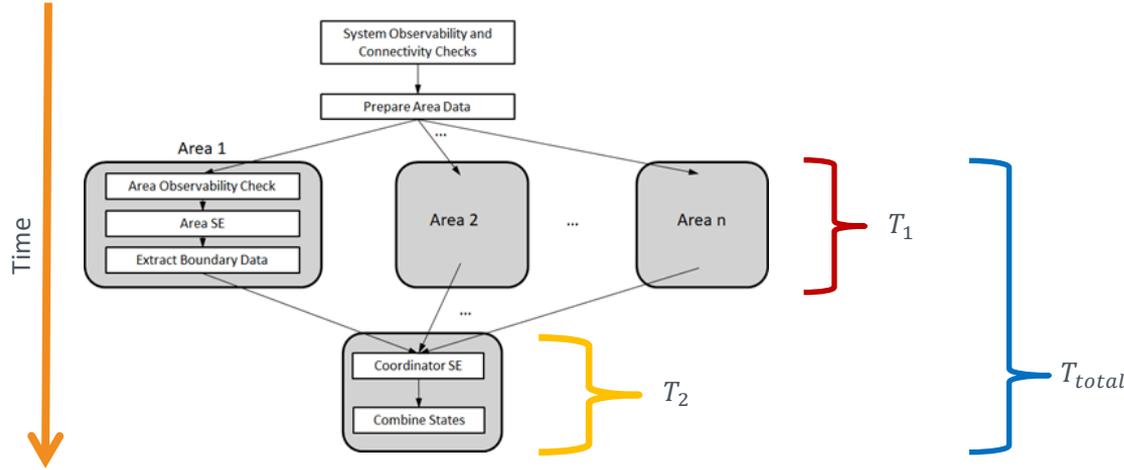


3750

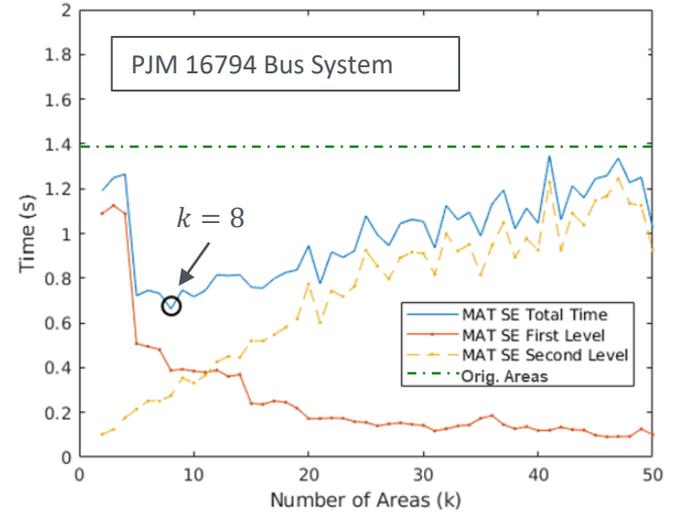
Timing Results

David Kelle and A. Abur, "Improving performance of multi-area state estimation using spectral clustering," *Proceedings of the 51st North American Power Symposium, 2019.*

Multi-Area State Estimation Algorithm Structure



Execution Time

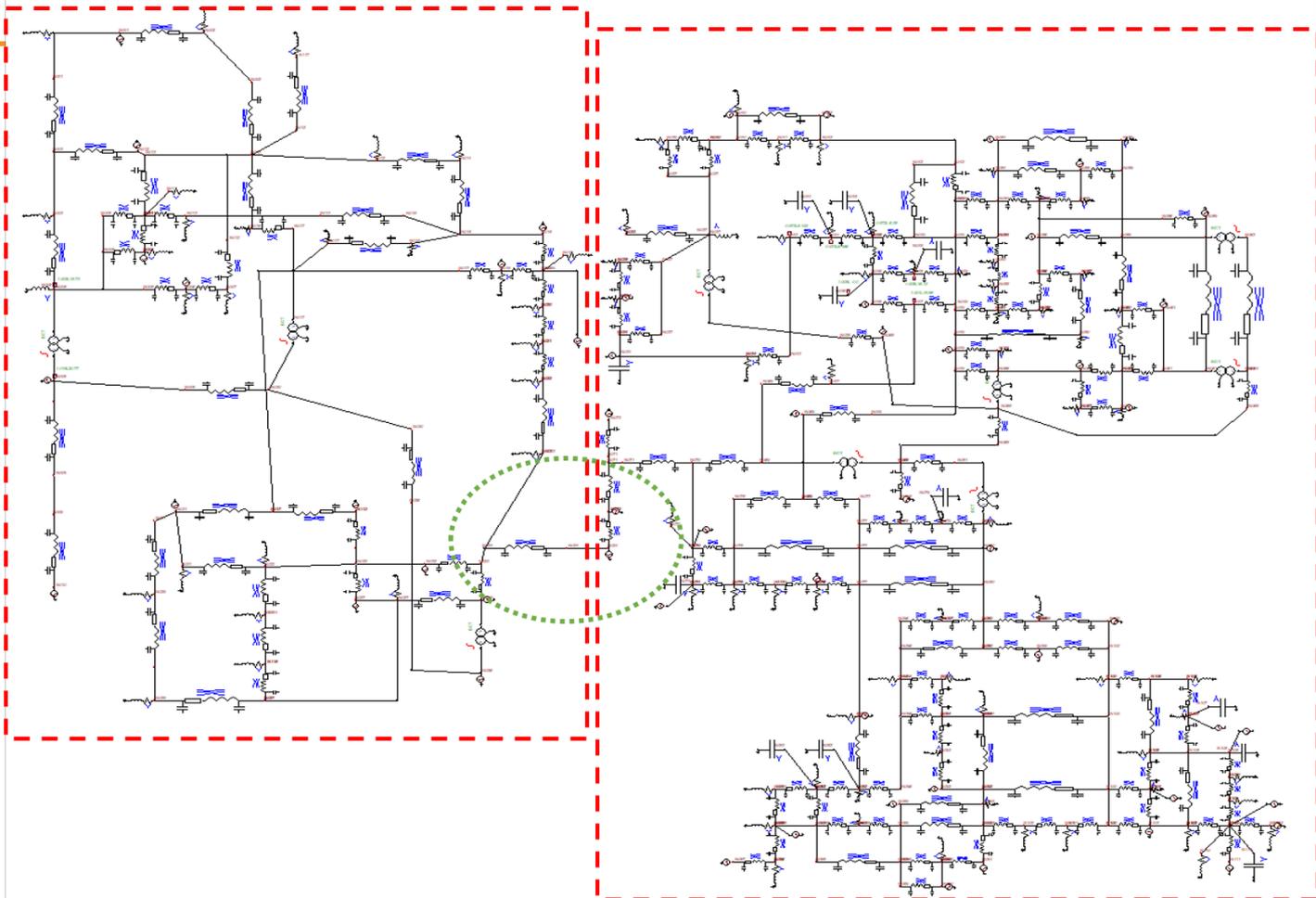


Case	k	Partition Results		Computation Time		
		$\sum r_j$	ϕ	T_1	T_2	T_{total}
Case 1	51	–	7.5465	0.2767	1.0841	1.3608
Case 2	51	12.0575	2.2864	0.1277	0.8658	0.9936
Case 3	8	1.6261	–	0.3876	0.2754	0.6630

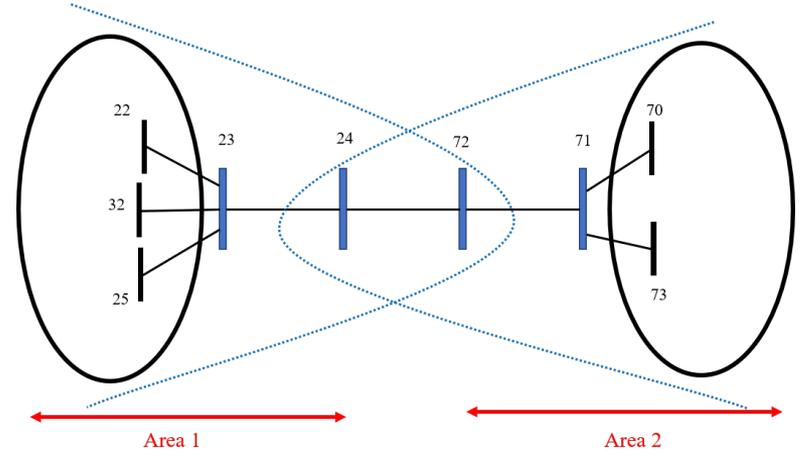
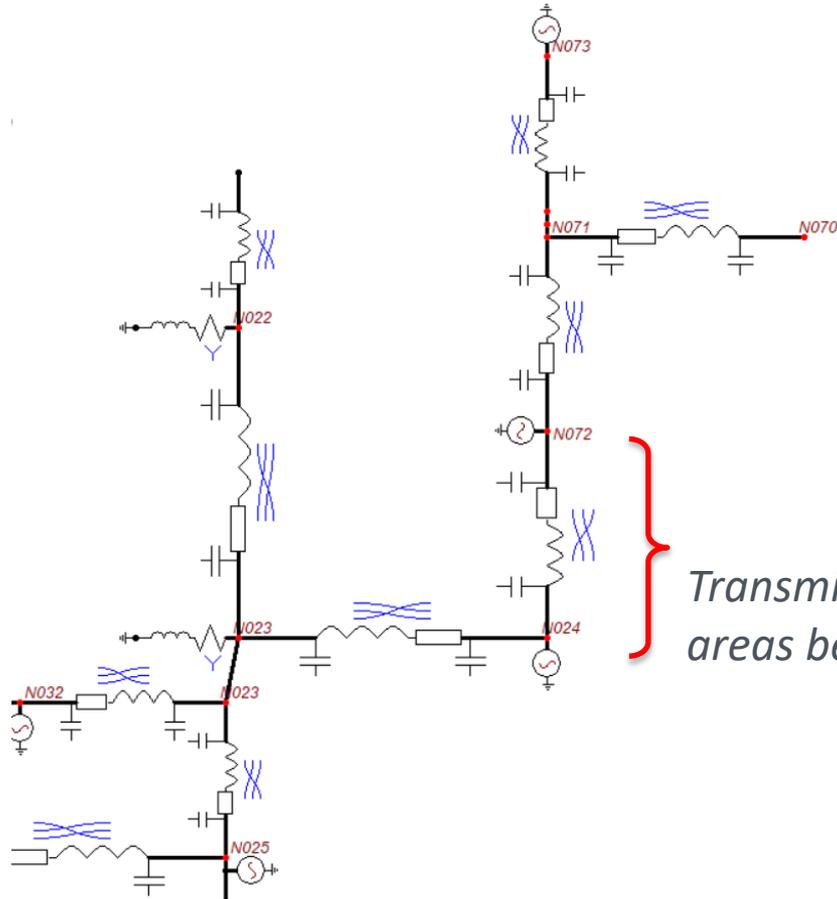
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- **Bad measurements / Robust estimator**

Detailed 3-Phase Model Using ATP



Boundary Configuration



Transmission Line that connects two areas between buses 24 and 72

Bad Data Testing

- Gross errors placed in the following locations:
 - Case 1: Interior of the transmission system (P_{23})
 - Case 2: Inner boundary of the transmission system (P_{24})
 - Case 3: Interior of the distribution system (P_{70})
 - Case 4: Inner boundary of the distribution system (P_{72})

Bad Data Results

Case 1:

Table 13: Bad Data Analysis Results: Case 1 – Area $\mathcal{G}_{(1,1)}$

Meas.	Original		Iteration 1	
	z_i	r_i^N	z_i	r_i^N
P_{23}	-0.02869	20.03	0.0503	0.001077
$P_{23,24}$	0.08247	19.90	–	0.0003111
$P_{23,25}$	-1.625	8.938	–	0.0003164
$P_{23,32}$	0.9308	8.022	–	0.0002817
$P_{22,23}$	-0.5328	6.084	–	0.0002382

BD Detected !

Bad Data Results

Case 2:

Table 14: Bad Data Analysis Results: Case 2 – MAT SE, Area $\mathcal{G}_{(1,1)}$

Meas.	Original	
	z_i	r_i^N
P_{24}	-0.02708	1.798
Q_{24}	-0.1242	1.798
$ V_{72} $	0.9800	1.798
$Q_{23,24}$	0.1090	0.5893
$Q_{8,30}$	0.2780	0.2514

Missed BD !

Table 15: Bad Data Analysis Results: Case 2 – Level 3 Coordinator

Meas.	Original		Iteration 1	
	z_i	r_i^N	z_i	r_i^N
P_{24}	-0.02708	20.03	-0.06711	0.01259
P_{72}	-0.1205	20.03	-	0.01259
$P_{23,24}$	0.08246	20.03	-	0.01259
$P_{71,72}$	0.1061	20.03	-	0.01259
$Q_{23,24}$	0.1089	11.95	-	0.007204

BD Detected !

Bad Data Results

Case 3:

Table 16: Bad Data Analysis Results: Case 3 – MDF SE, Area \mathcal{G}_2

Measurement	z_i	r_i^N
P_{70}^a	-0.7579	22.595
$P_{70,71}^a$	0.1739	9.241
$P_{71,70}^a$	-0.1735	9.132
$P_{69,70}^a$	1.0888	6.102
P_{74}^a	-0.6796	5.703

BD Detected !

Bad Data Results

Case 4:

Table 17: Bad Data Analysis Results: Case 4 – MDF SE, Area \mathcal{G}_2

Measurement	z_i	r_i^N
P_{72}^a	-0.1165	0.463
-	-	0.323
-	-	0.251

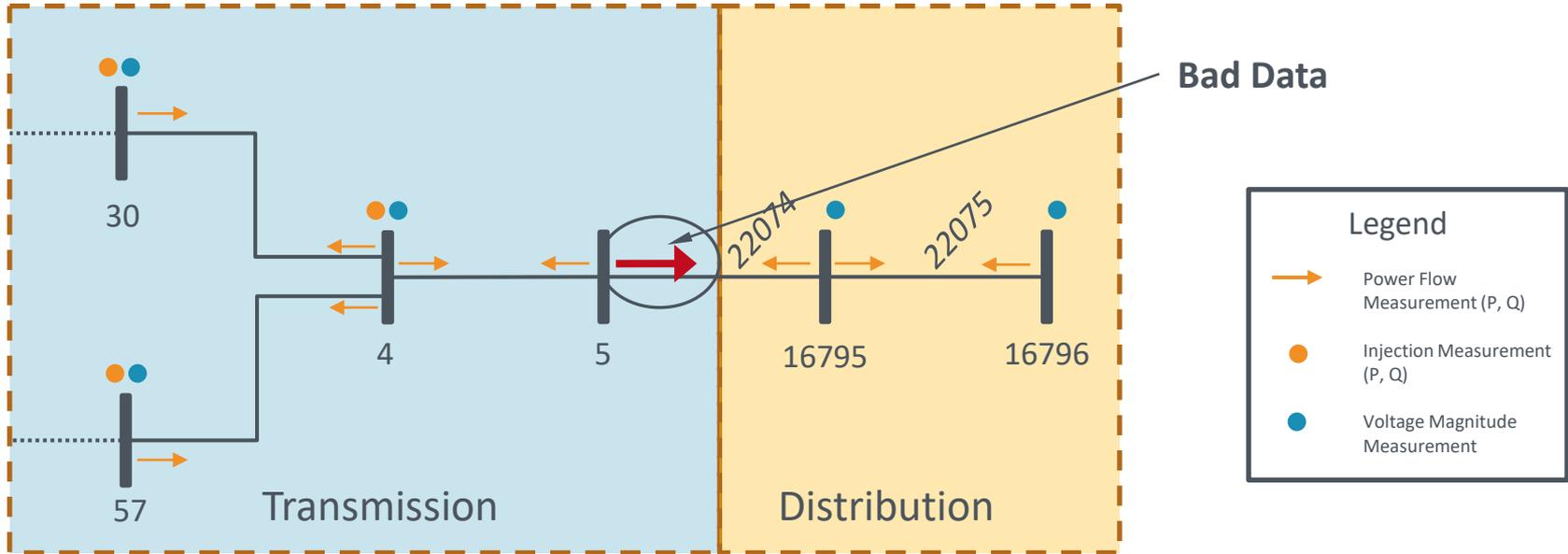
Missed BD !

Table 18: Bad Data Analysis Results: Case 4 – Level 3 Coordinator

Meas.	Original		Iteration 1	
	z_i	r_i^N	z_i	r_i^N
P_{72}	-0.08047	23.12	-0.1205	0.01215
P_{24}	-0.06708	23.12	-	0.01215
$P_{24,23}$	0.1061	8.777	-	0.006597
$P_{23,24}$	0.08246	8.755	-	0.004615
$P_{71,72}$	-0.08214	8.725	-	0.004595

BD Detected !

Large System: Gross error on the boundary



Bad Data Location	Level 1	Level 2	Level 3	Final MSE
$P_{5,16795}$	Not Detected	–	Corrected	1.92×10^{-7}

First Workshop at NEU – May 7, 2019 / NEU Campus



7 external speakers

- PNNL (2)
- NREL (2)
- U. California-R (1)
- ANL (1)
- ISO-NE (1)

3 NEU speakers

24 attendees

All presentations are posted
on workshop web page:

[http://www1.ece.neu.edu/~abur/
NEU_workshop/wkshop1.html](http://www1.ece.neu.edu/~abur/NEU_workshop/wkshop1.html)

Final Workshop at PJM – Changed to Virtual

- Date: October 30, 2020
- Location: virtual
- NEU speakers (3)
- External speakers (4):
 - National Renewable Energy Laboratory, Colorado (2)
 - Pacific Northwest National Laboratory, Washington (1)
 - University of California-Riverside (1)
- All presentations are posted on workshop web page:

http://www1.ece.neu.edu/~abur/NEU_workshop/wkshop2.html

Contributions

- A combined transmission and distribution system state estimator is developed. The estimator is scalable to very large-scale grids and can detect, identify and remove bad data.
- Some of the useful byproducts of the project include a novel formulation of multiphase state estimation using virtual reference buses, a decoupled modal domain state estimation, and an efficient partitioning algorithm for large scale power grids for improved multiarea state estimation.
- The developed combined state estimator is successfully implemented and tested using the large 16Kbus PJM transmission system and four copies of the IEEE 8500-node test feeders.