



PARTNERSHIP
TO ADVANCE
COMBUSTION
ENGINES

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ACE141: Advanced Ignition System Fundamentals

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FY21 DOE Vehicle Technologies Office Annual Merit Review, June 21-24, 2021



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Overview

Timeline

- PACE start: Q3, FY19
- PACE end: Q4, FY23 (46% complete)
- Focus and objectives of individual tasks will be continuously adjusted
- Overall PACE work plan discussed in **ACE 138**

Budget

Task	Description	FY20	FY21
A.M.03 PI: Scarcelli	Advanced Ignition Modeling Tools	400k*	370k*
A.E.03 PI: Rockstroh	Fundamental Ignition Experiments	380k	342k
S.E.03.01 PI: Ekoto	Advanced Ignition to Enable Alternative Combustion Modes	420k	420k

*Listed funding also supports research presented in **ACE 142**

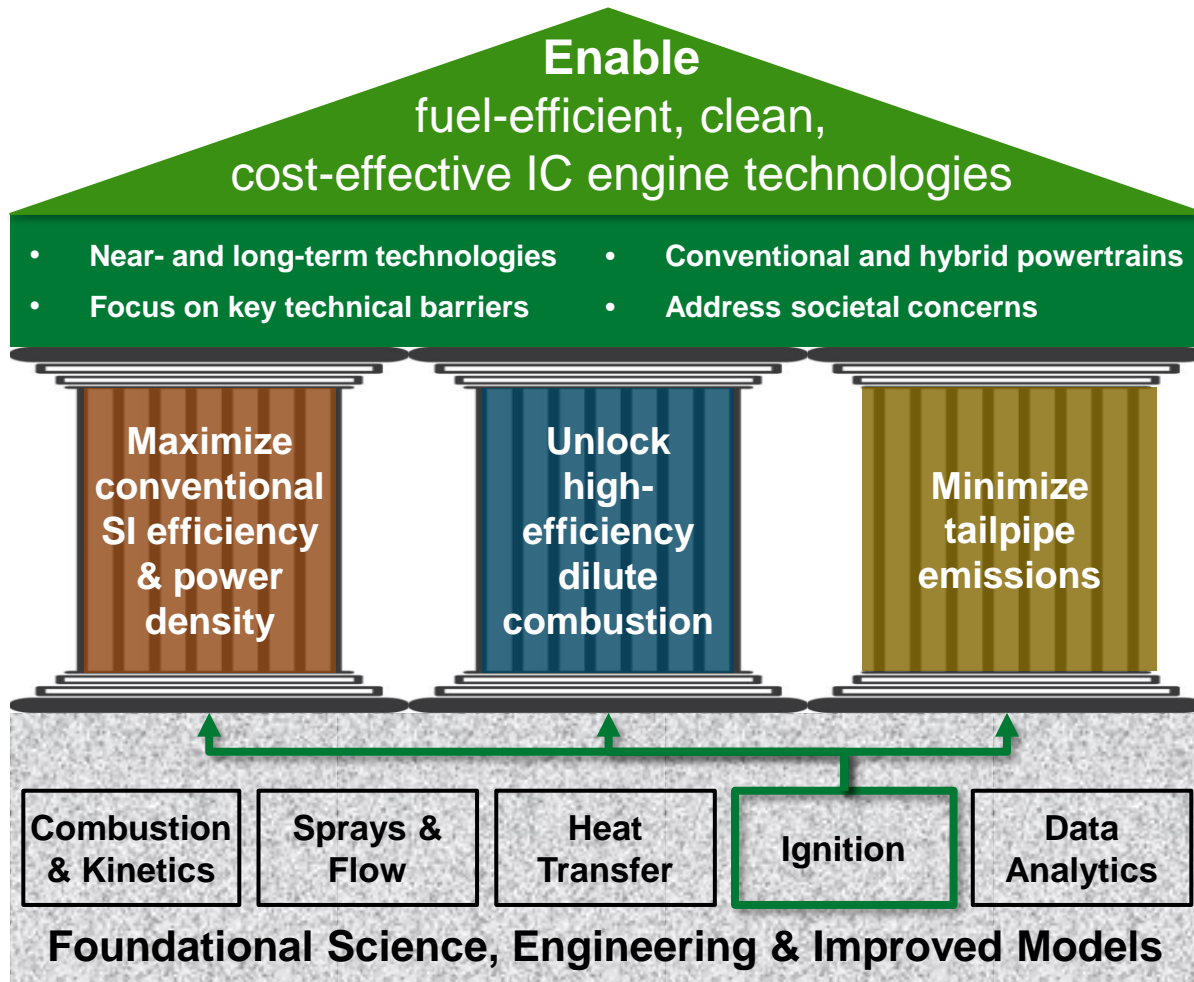
Barriers

- Addresses PACE Major Outcomes 6 and feeds directly into Major Outcomes 4, 5, & 8
 - More robust ignition systems for part-load dilute[†]
 - Technologies to reduced combustion variability at boosted high-load[†]
- [†]ACEC TT Roadmap

Partners

- **PACE is a DOE-funded consortium of 5 National Laboratories working towards a common goal (ACE 138)**
 - Kinetics (**Wagnon, ACE 139**)
 - Ignition modeling (**Scarcelli, ACE 142**)
 - Cold-start modeling/experiments (**Edwards, ACE 145**)
- **Partners include:**
 - Plasma ignition collaboration with Tenneco and TPS
 - Plasma kinetics/physics with U. Auburn, U. Texas, Esgee Tech.
 - Pre-chamber research with CMT-Motores, Mahle Powertrain
 - Pre-chamber modeling – Gamma Technologies

Relevance



Overall Relevance of PACE: (ACE 138, McNenly)

PACE combines unique experiments with world-class DOE computing and machine learning expertise to speed discovery of knowledge, improve engine design tools, and enable market-competitive powertrain solutions with potential for best-in-class lifecycle emissions

Major Outcome 6

Develop viable advanced igniters and control methods that expand existing dilution limits and enable stable catalyst heating operation

Success measure

Prototype igniters and control strategies ignition control methods enable stable ignition for EGR dilution rates of up to 40% or air dilution rates of up to 50% with no adverse impact on pollutant emissions relative to the stock OEM configuration.

*Demonstrate ignition system can maintain stable combustion at high exhaust heat flux conditions seen during cold start.
ACEC 3 bar/1300 rpm* test point*

https://www.energy.gov/sites/prod/files/2018/03/f49/ACEC_TT_Roadmap_2018.pdf

Milestones

- **Task A.M.03: Advanced Ignition Modeling Tools**

Date	PI	Milestone	Status
FY22 Q2	Scarcelli	Model LTP flammability limits with a combination of plasma and CFD simulations	50% Complete
FY22 Q4	Scarcelli	Develop engineering models for pre-chamber	25% Complete
FY22 Q4	Scarcelli	Develop pulsed plasma ignition models to include O3 generation	25% Complete

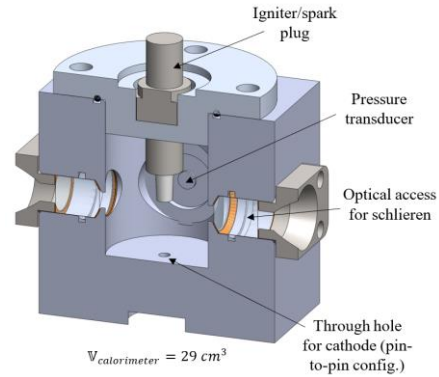
- **Task A.E.03: Fundamental Ignition Experiments**

Date	PI	Milestone	Status
FY21 Q4	Rockstroh	Demonstrate stable operation 40% EGR dilution with PC ignition for ACEC 1300 rpm, 3 bar BMEP	75% Complete
FY22 Q3	Rockstroh	Demonstrate comparable PC performance for cold-start protocol relative to conventional SI	0% Complete
FY22 Q3	Rockstroh	Develop 1-D model PC mixing and jet-exit momentum model – New task	25% Complete

- **Task S.E.03.01: Advanced Ignition to Enable Alternative Combustion Modes**

Date	PI	Milestone	Status
FY21 Q1	Ekoto	Improved SACI cyclic stability w/ O ₃ addition for EGR dilute charge at ACEC 1300 rpm, 3 bar BMEP	75% Complete
FY21 Q1	Ekoto	Demonstrate LTP plasma ignition 40%+ EGR tolerance under stoichiometric conditions	100% Complete
FY22 Q3	Ekoto	Demonstrate improved performance with BDI cold-start protocol relative to conventional SI	0% Complete
FY20 Q3	Ekoto	Passive PC engine testing with conventional igniter and BDI	50% Complete

Facilities:



Crossflow Facility

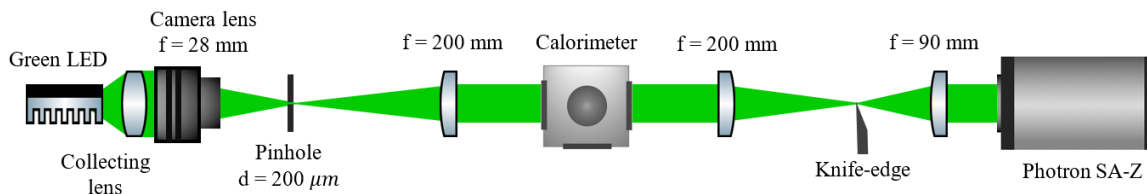


Static Ignition Tester

- Initial Press/Temp: 10 bar (30 bar discharge only)/373 K
- Oxidizer Stream: Air/CO₂/N₂/H₂O
- Gaseous & Liquid Fuels

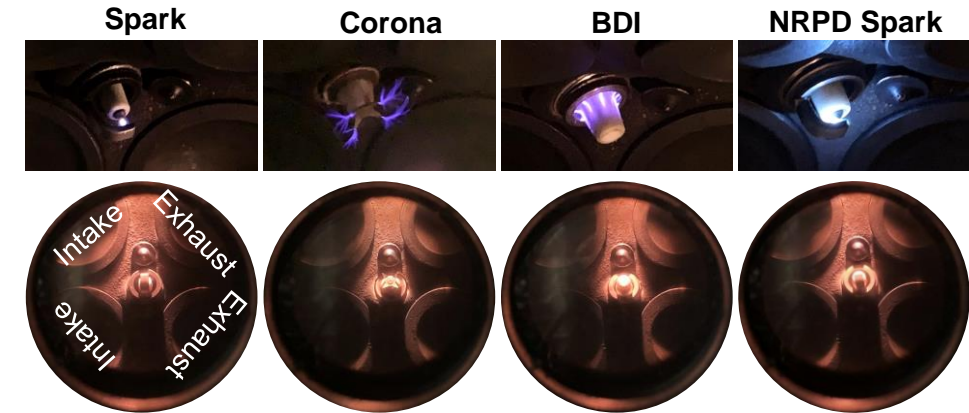
Diagnostics:

- Heat release & Calorimetry – not simultaneously
- High-frequency voltage/current monitoring
- High-speed schlieren/intensified imaging – 60+ kHz



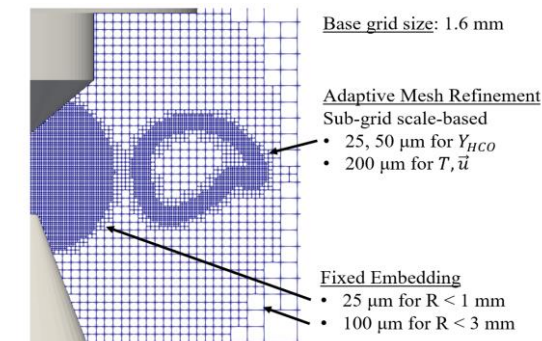
Non-equilibrium Plasma Igniters:

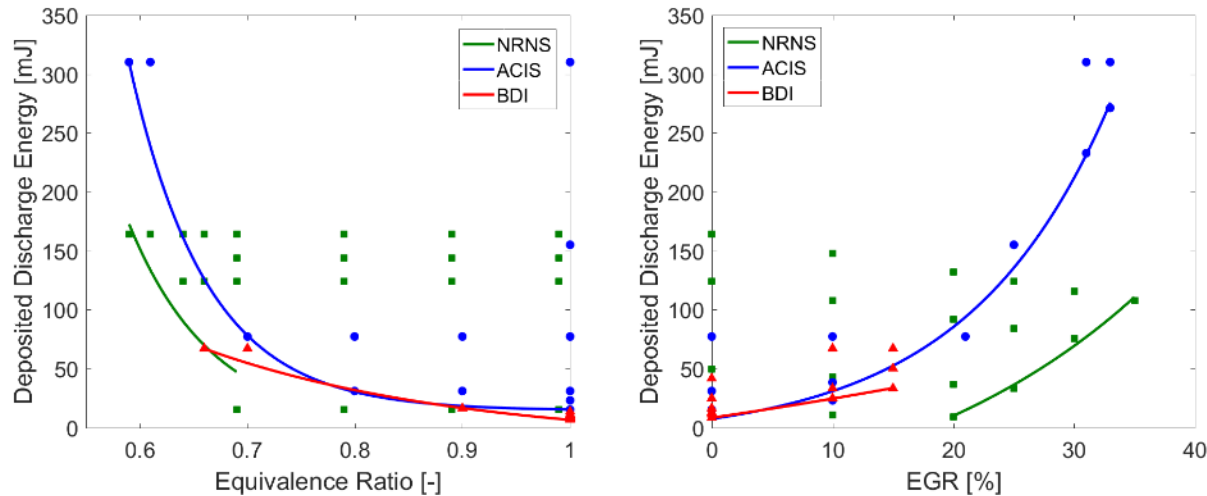
- Specific focus on nanosecond repetitive pulses (NRPD)
- Combination of high-energy **streamer** and **spark** discharges



Non-equilibrium Plasma Ignition Modeling :

- VizGlow non-equilibrium plasma discharge simulations
- Source term modeling with coupling to CONVERGE CFD



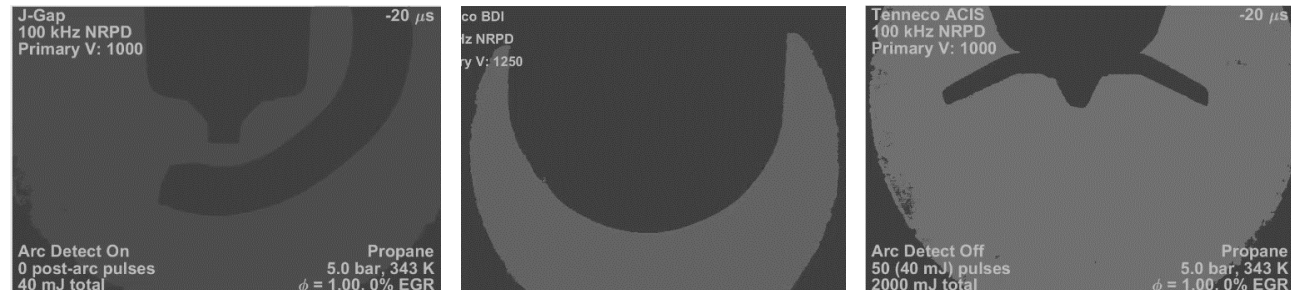


Complementary schlieren imaging reveals ignition physics

- Early ignition kernel supported by additional discharges
 - Spark igniters supply expansion energy
 - Streamers form on ignition kernel – kernel grows along streamer front
- Excess discharge energy disrupts ignition due to localized extinction

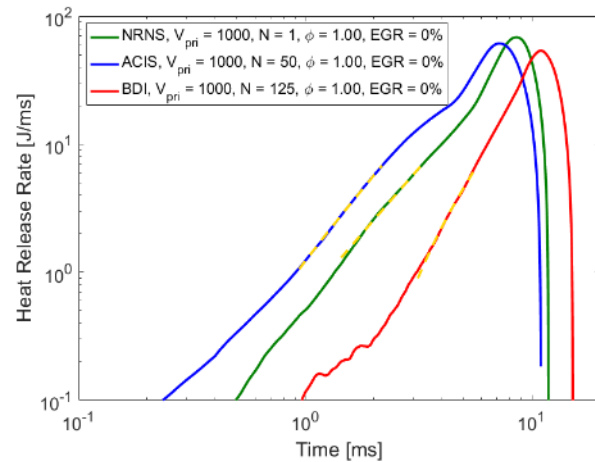
Dilution ignition limits measured for multiple spark and non-equilibrium plasma igniters

- Baseline spark ignition lean limit: $\phi = 0.59$ (93 mJ)
- Nanosecond spark igniters improve lean and dilution ignition limits
 - Greater extension for EGR dilution
- Spark igniters also use a lot less energy
 - Calorimetry performed to measure deposited energy (see Backup 1)
 - Streamer & spark energy use more consistent



Need to characterization growth rates via heat release data

- Large differences in flame development
 - Does not always correlate with ignition limits

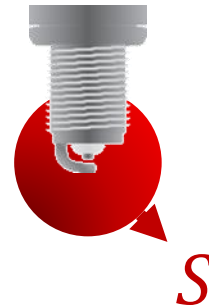


- Only interested in first 10% of heat release period

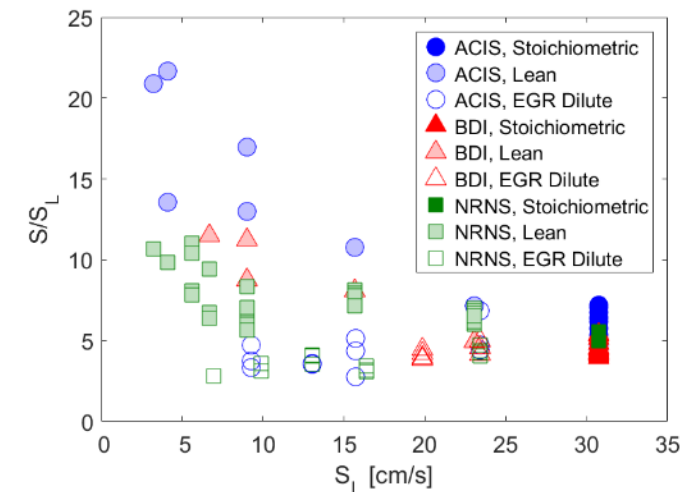
$$\dot{Q}_{Work} = 4\pi LHV \cdot Y_{fuel} \rho S^3 (t - t_0)^2 - \dot{Q}_{Heat Loss}$$

Unknowns

- Fit applied using the heat release data to get S and t_0
- Values well-match with imaging data of kernel growth

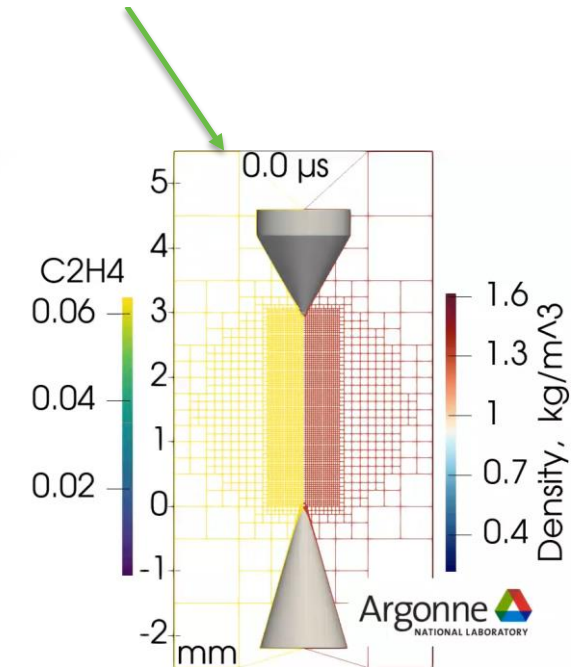
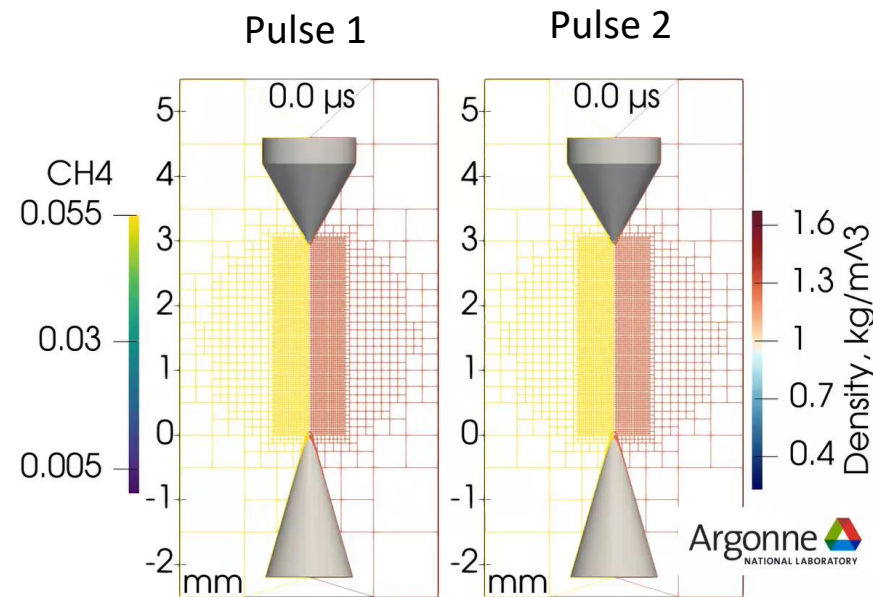
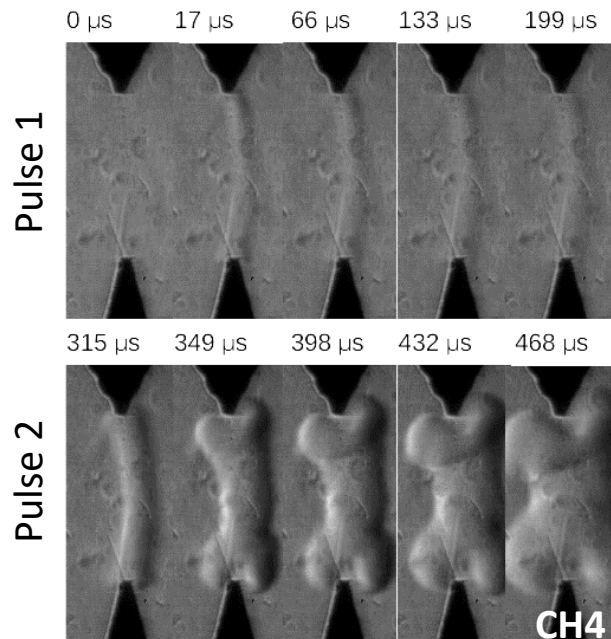
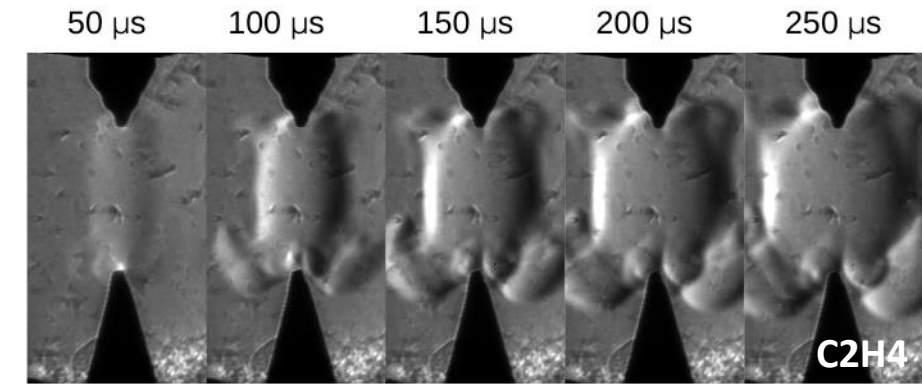


- Large differences in flame propagation rate for lean ignition
 - Lean ignition readily accelerated by additional discharge energy – More so for streamer igniters
 - Dilute ignition not dependent on added discharge energy or discharge type



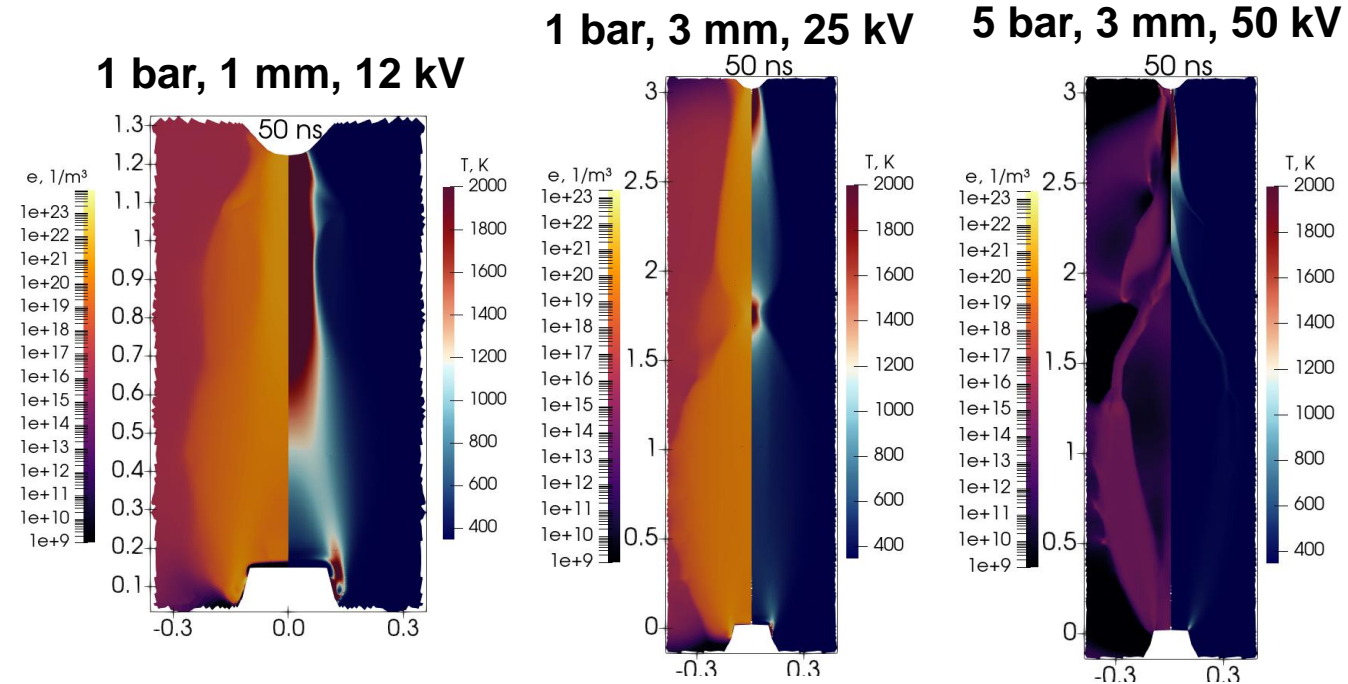
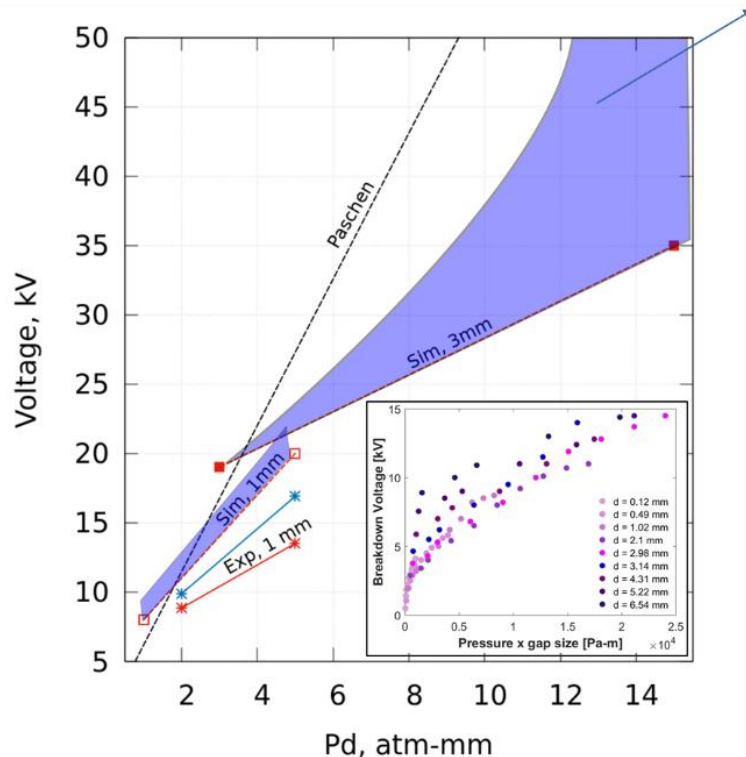
Streamer igniters seem best suited for lean combustion strategies

- Ignition initialized via VizGlow discharge simulation outputs
 - Used to create a temporally & spatially resolved energy source term: S_{LTP} (See Backup Slide 3)
 - S_{LTP} converted to a User Defined Function & used to initialize flame kernel
- LTP ignition simulations qualitatively match experiments
 - Methane-air ($\phi=1$) required at least two pulses
 - Ethylene-air ($\phi=1$) ignited with a single pulse
- Simplified discharge models under development



CONVERGE CFD

- Development of predictive for streamer-arc transition capability
 - Major design constraint for streamer igniters
 - VizGlow simulations correlated to experiments at a wide range of pressure/gap-size/voltage

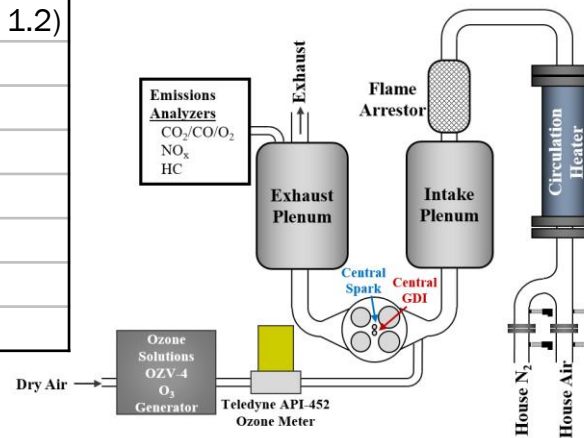


- Simulations capture previous experimental observations, and provide additional detail
 - Streamer widths decrease with pressure
 - Branching increases with pressure
 - Gas heating decreases with pressure
 - Breakdown voltage increases with pressure and gap size but the rate of change decreases

Homogeneous lean/dilute w/ plasma & passive PC (SNL):

- EGR (N₂ only) and air dilution sweeps
- Heat release, emissions, and ignition imaging
- **2 streamer & 3 spark-type plasma igniters evaluated**
- Passive pre-chamber with either spark or plasma igniters
- Multiple tip geometries (hole area, tangential angle)

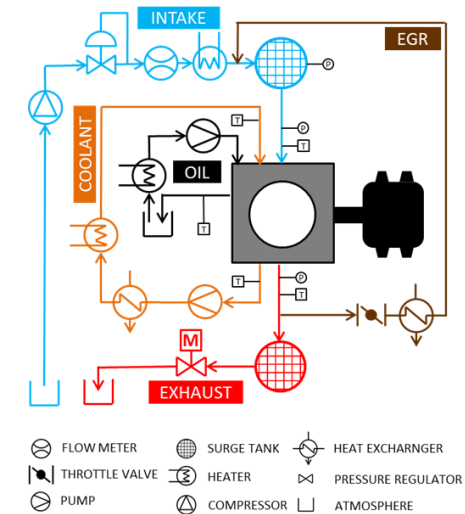
SG2 Central DI/SI	
Injector	8-hole solenoid (HDEV 1.2)
Stroke/Bore	1.11
CR	13 (12.6 w/ PC)
Displacement [L]	0.55
Intake press. [bar]	0.5 – 0.7
Engine Speed [rpm]	1300
EGR [%]	0 – 27%
IMEP [bar]	3.5



Homogeneous dilute w/ active/passive PC (ANL):

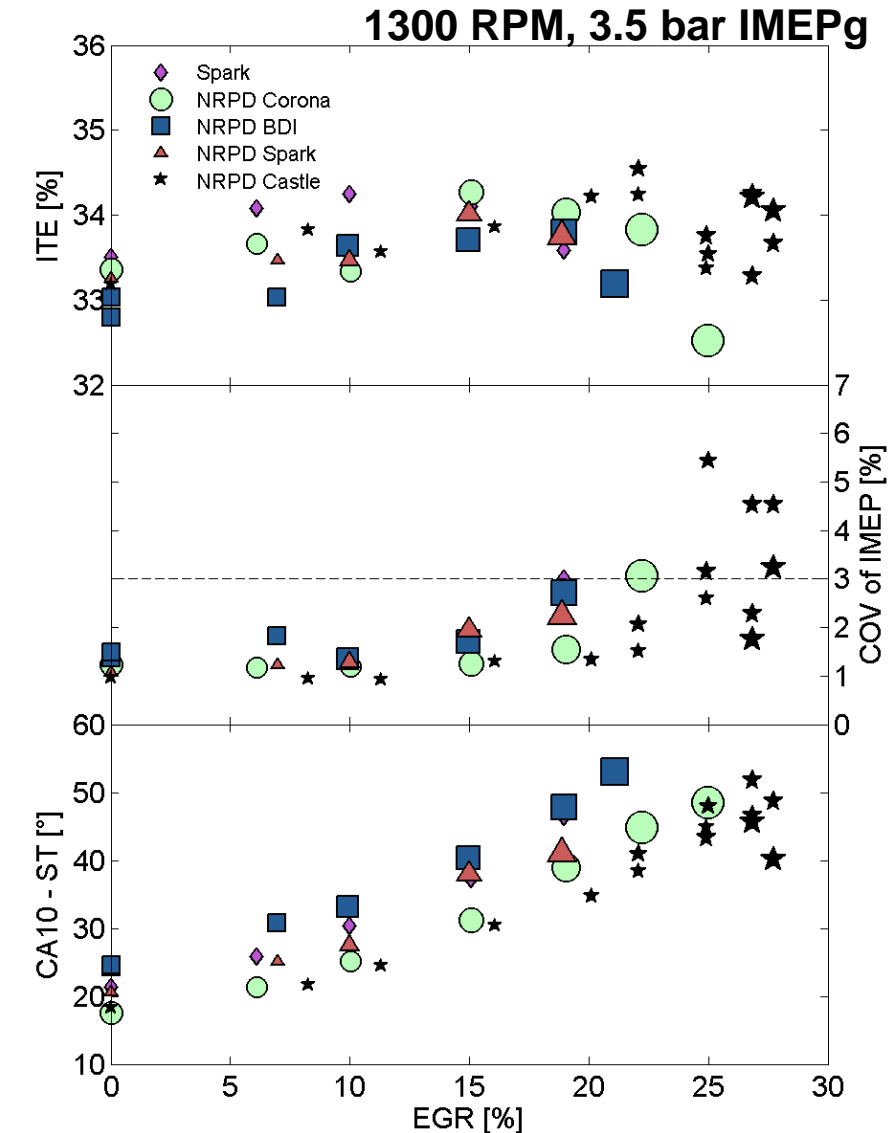
- EGR dilution sweeps
- Heat release and emissions measurements
- Instrumented pre-chamber
- Single tip geometries (4-hole)
- **Companion modeling of PC residuals & jet momentum**
- **Active PC: premixed fuel/air vapor**

EcoBoost Central DI/SI	
Injector	6-hole solenoid
Stroke/Bore	1.13
CR	11.3 (10.9 w/ PC)
Displacement [L]	0.63
Intake press. [bar]	0.5 – 0.7
Engine Speed [rpm]	1300, 1500
EGR [%]	0 – 32%
IMEP [bar]	3.5, 5.0



Additional lean-stratified work with ozone addition at SNL (see Backup slide 4)

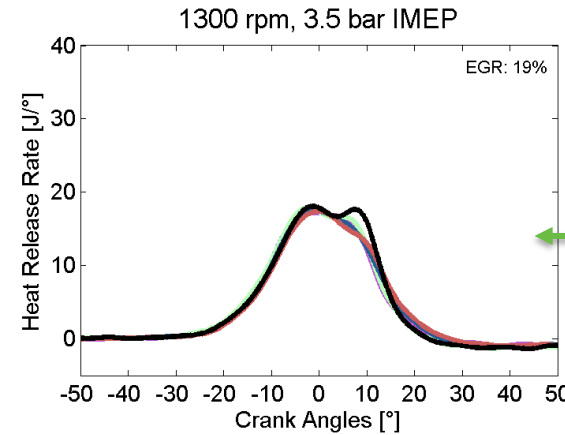
- **FY20: Demonstrated RF corona & NRPD spark extended lean limits and increased ITE relative to spark**
 - Spark: $\phi = 0.73$, ITE: 32.5%
 - ACIS: $\phi = 0.68$, ITE: 33.8%
 - NRPD Spark: $\phi = 0.65$, ITE: 34.4%
- **NRPD igniters further extend lean limits increase ITE**
 - Peak ITE: 36.0% (NRPD Castle), 35.7% (NRPD Corona)
 - Strongest NO_x reduction with NRPD castle (71% reduction)
 - Corona igniter limited by arcing but still had fastest early burn rates – consistent with static cell measurements
- **Little difference in igniter type on dilution limits or peak efficiency – confirms static-cell experiments**
 - Marginal benefit with NRPD Castle igniter but requires high energies that result in rapid electrode erosion
 - Corona igniter limited by increased arc propensity with higher dilution rates that restricted applied voltage that could be used



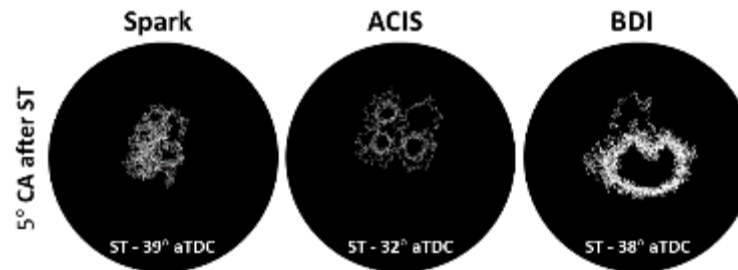
Accomplishment: Homogeneous Plasma Ignition

S.E.03.01

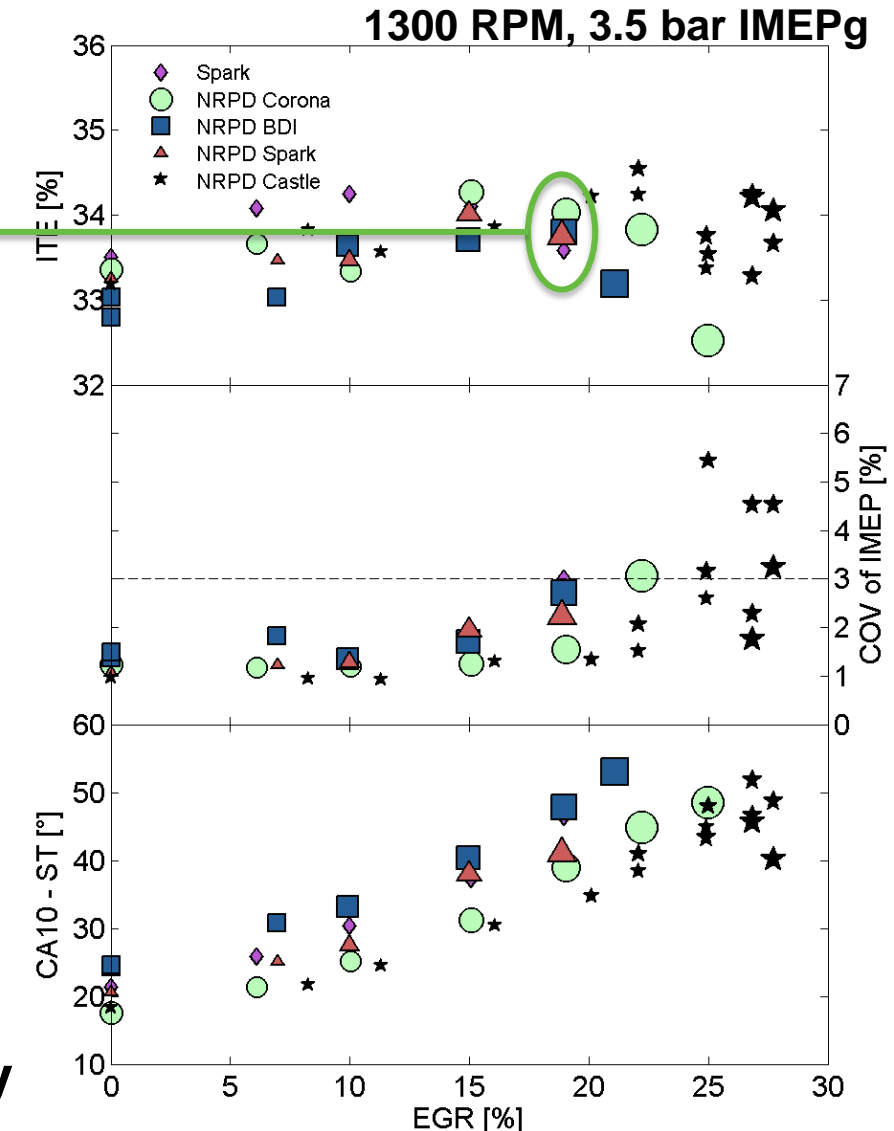
- Auto-ignition inhibited by slow early flame development
 - Exception is NRPD Castle igniter
 - Auto-ignition phasing highly variable



- Imaging reveals better stability due to more repeatable early flame development for plasma igniters
 - Corona stability limited by arc propensity w/ increase dilution
 - BDI stability limited by poor discharge energy deposition



Given high discharge energies, plasma igniters likely cannot do better with current engine platform

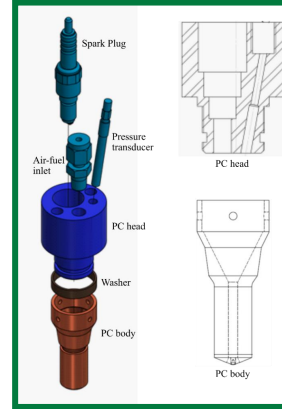


Accomplishment: Pre-Chamber Engine Ignition Testing

A.E.03

- ANL developed active pre-chamber

- Funnel-throat concept
- Pre-vaporized air/fuel
- 3% of clearance volume
- 4-nozzles – no swirl
- Working with Tier 1s for production concepts

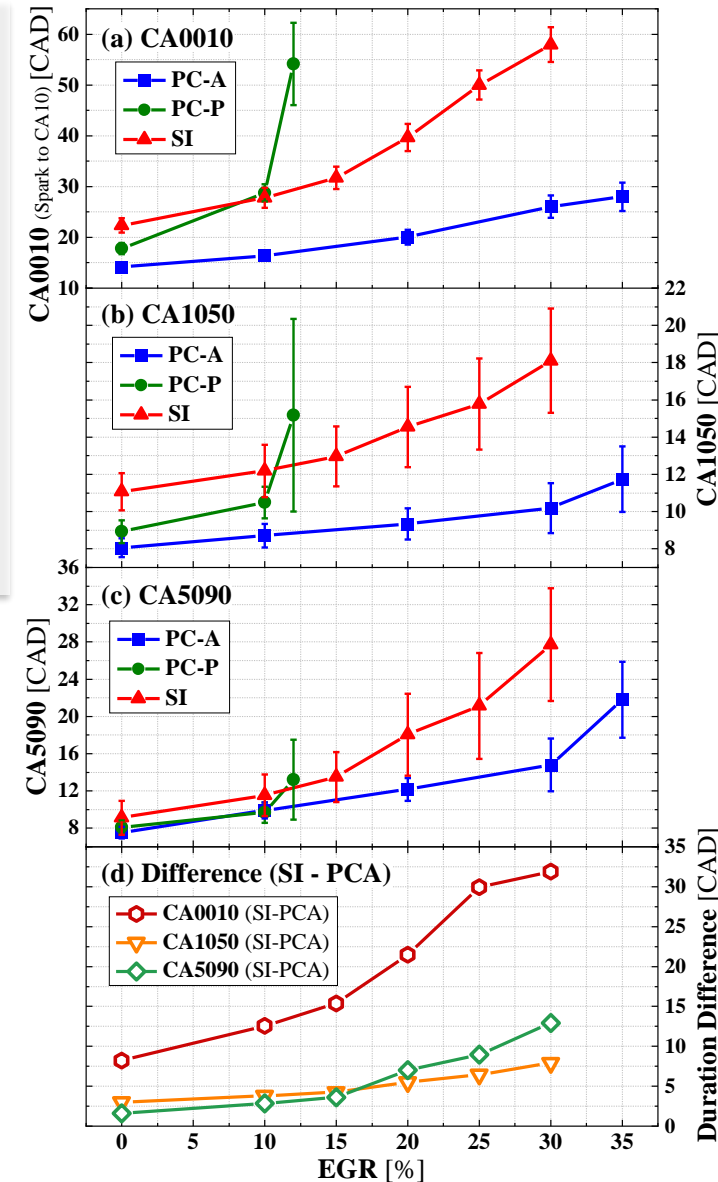
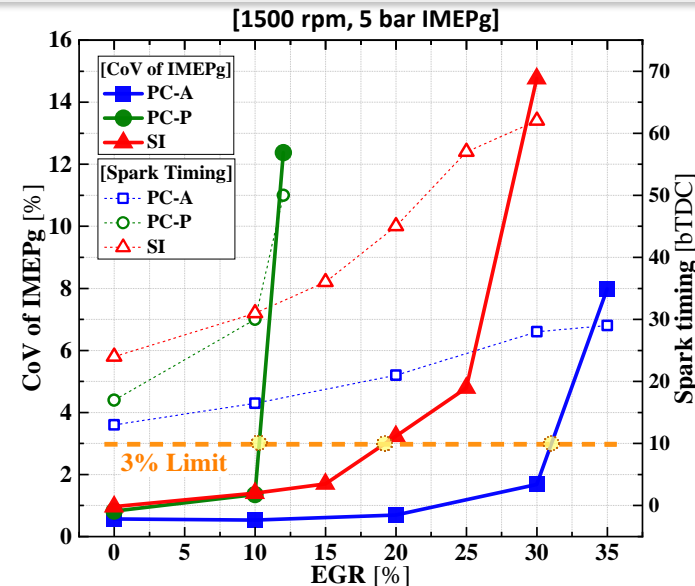
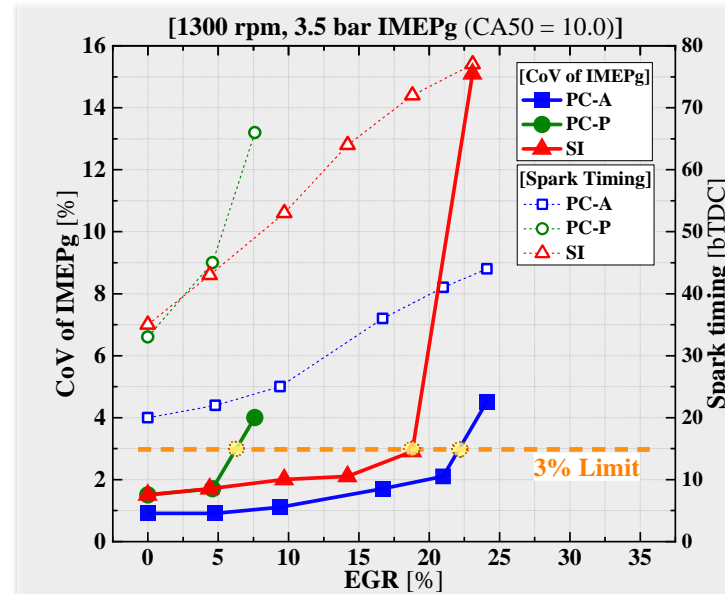


- ACEC TT low-load (3.5 bar / 1300 rpm):
18% EGR SI baseline

- 7% EGR tolerance for Passive PC (PC-P)
- 22% EGR tolerance for Active PC (PC-A)

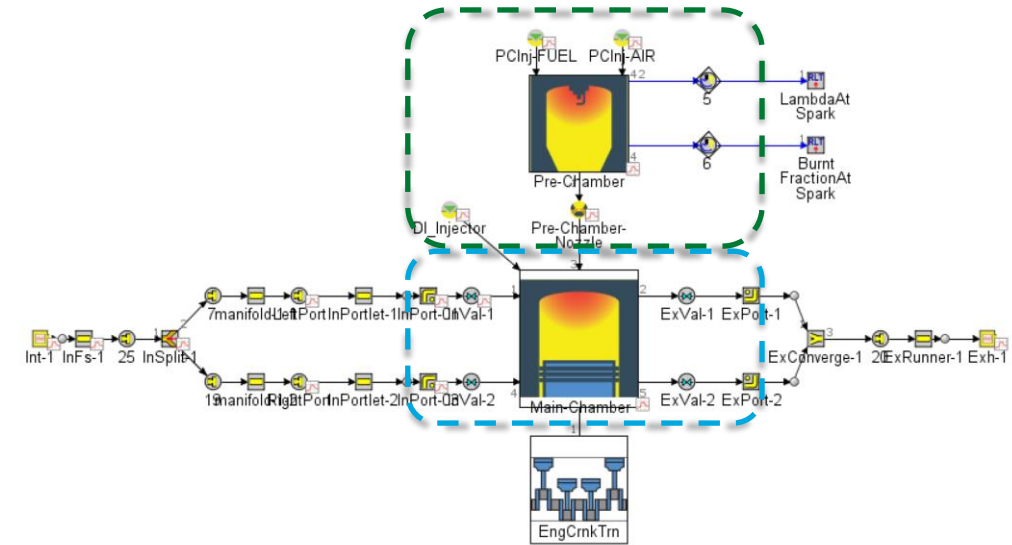
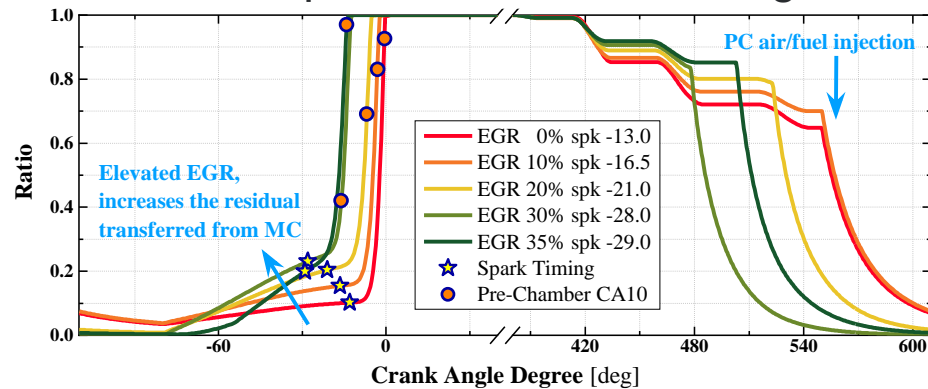
- Moderate load/speed (5 bar / 1500 rpm):
19% EGR SI baseline

- 10% EGR tolerance for PC-P
- 32% EGR tolerance for PC-A
- Close to EGR tolerance goal



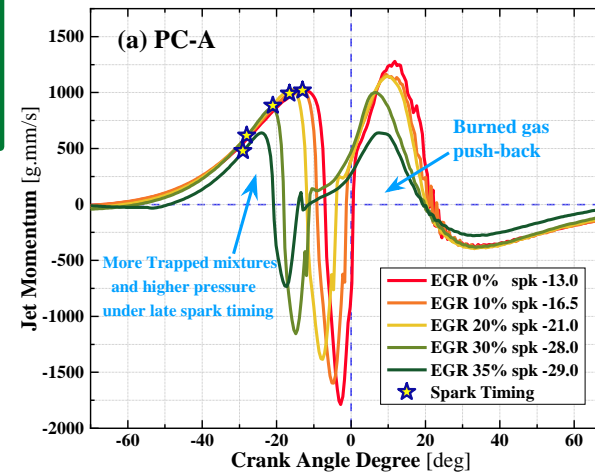
- **GT Power Model MC to PC gas exchange**

- 1D gas exchange solved via energy & mass conservation using measured PC and MC pressure data
- Estimates pre-chamber residual gas fraction at spark timing



- **Pre-chamber combustion**

- Genetic optimization of Wiebe function anchor angle, burn rate & exponent using experiment data
- Estimates jet-exit momentum



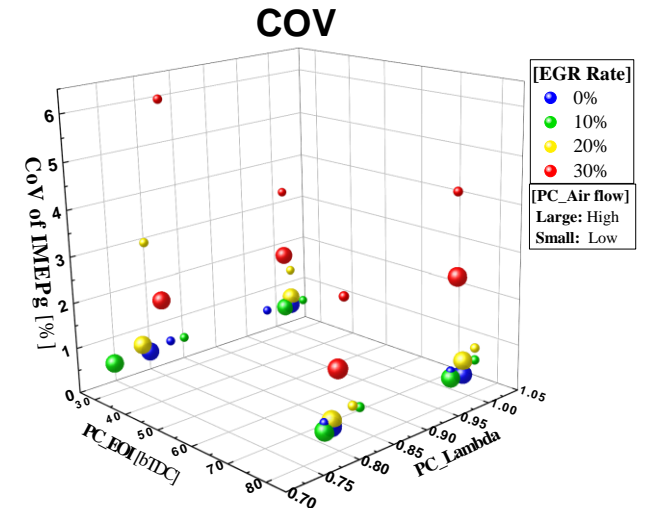
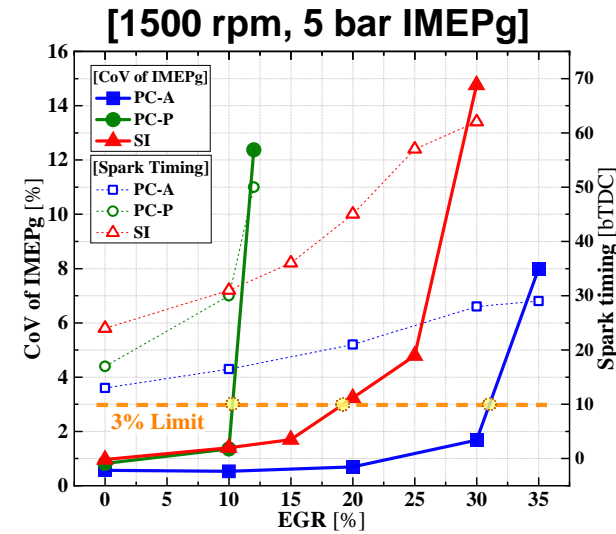
- **Main Chamber combustion**

- Imposed burn rate from experiment data & Three Pressure Analysis
- Start of combustion set by PC 50% MFB point
- Refinement ongoing

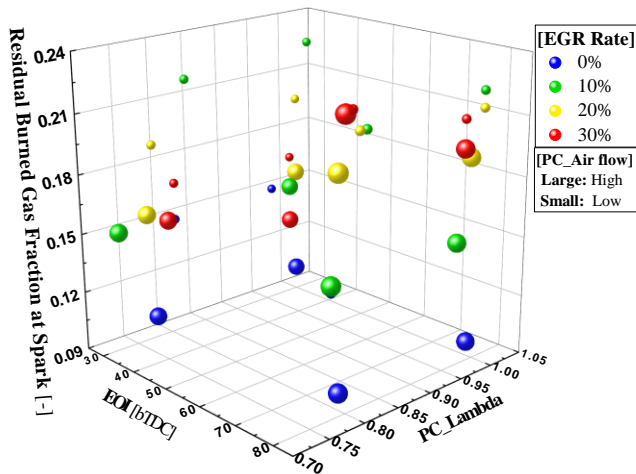
PC-A injection control parameters (λ_{PC} , EOI_{PC} , and m_{PC}) investigated to identify influence on different PC and MC combustion properties

MC Combustion CoV

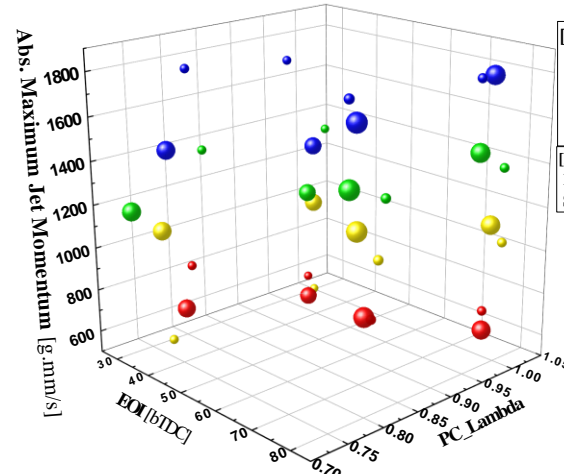
- Higher m_{PC} improves stability
- Rich PC mixtures produce good stability regardless of EOI_{PC}
- Stoichiometric PC mixtures only stable for late EOI_{PC}



PC Residual Gas Fraction



Max Jet Momentum



PC Residual Gas Fraction:

- Improved scavenging with increased m_{PC}
- Reduced residuals with late EOI_{PC}

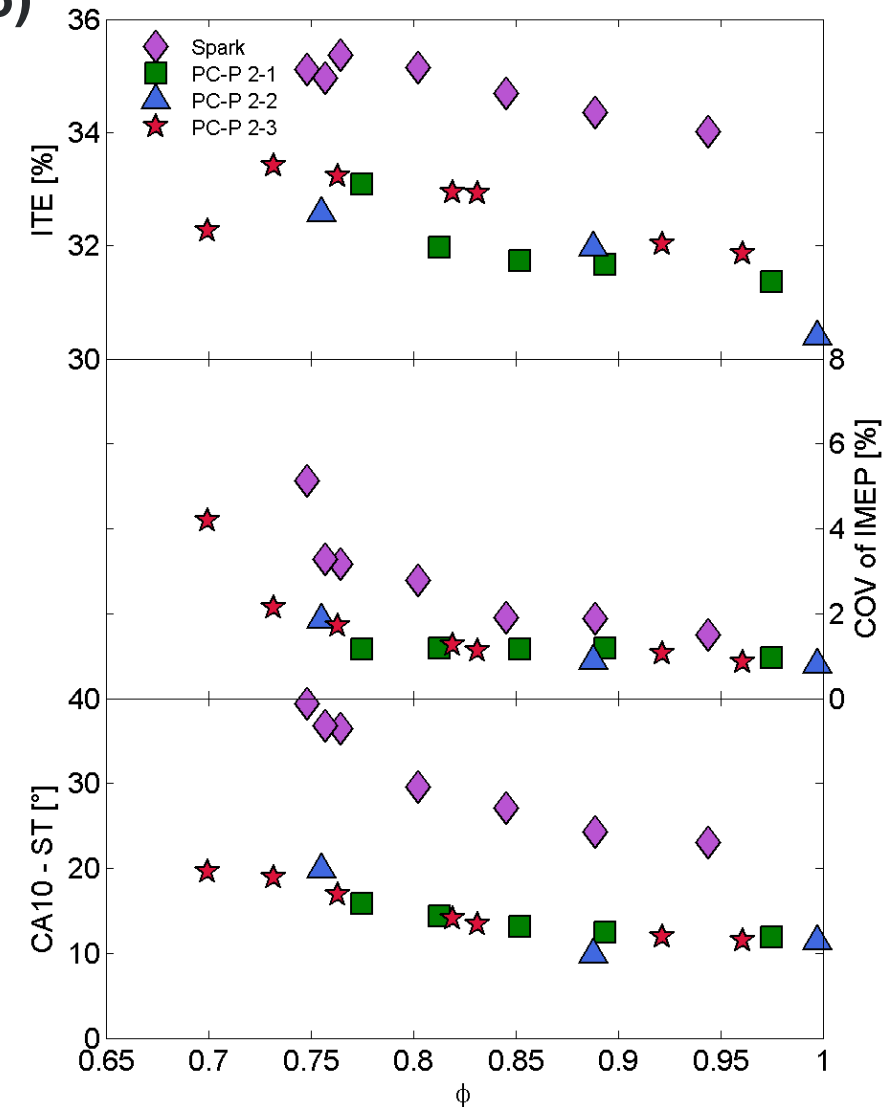
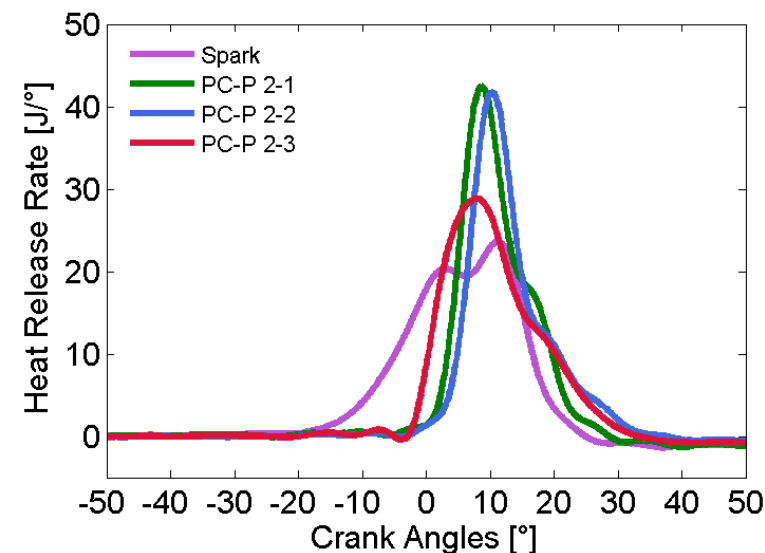
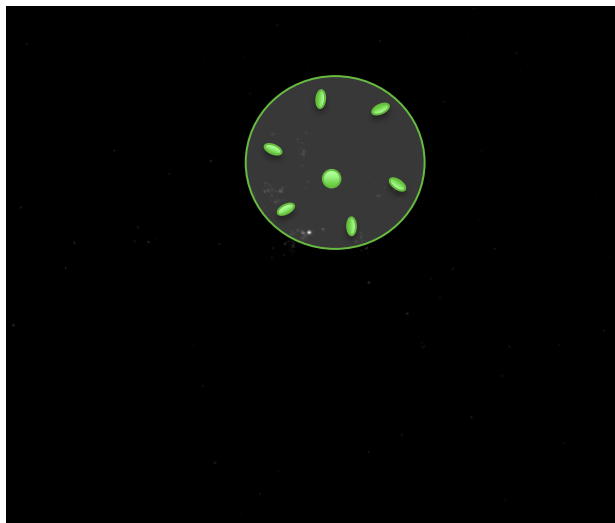
Jet Momentum:

- Late EOI_{PC} reduces jet momentum
- Higher jet momentum with lower λ_{PC}

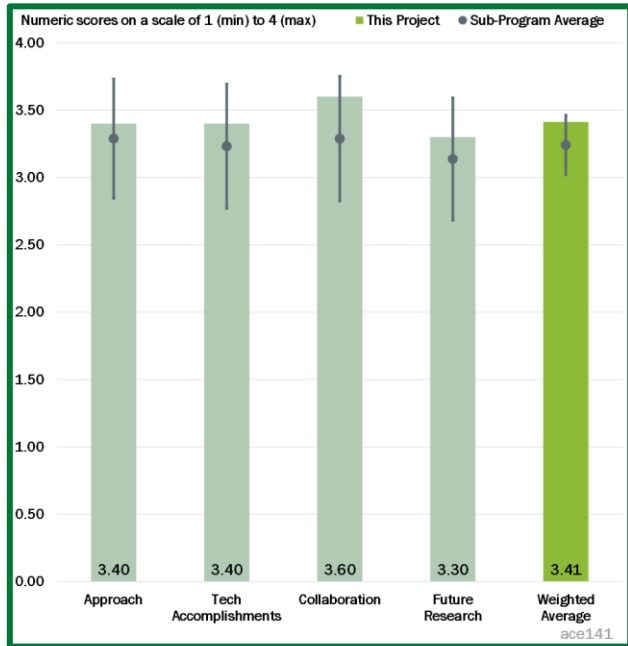
- 1D modeling needed to link jet exit momentum and energy to MC combustion (see future work)

- **Similar passive PC with 6 x tangential nozzles (See Backup 5)**

- All PC demonstrated improved lean limit relative to SI
- PC-P 2-1: Added center hole nozzle, larger PC volume (2.0 cc)
 - Early central ignition followed by 2nd stage radial ignition
 - CMT simulations well-matched to the data
- PC-P 2-2: Same hole arrangement, smaller PC volume (1.7 cc)
 - Virtually identical ignition characteristics as PC-P 2-1
- PC-P 2-3: no center hole nozzle, smaller PC volume (1.7 cc)
 - Radial ignition followed by combustion in the core



Response to Reviewer Comments



Approach/Relevance

- **R3: ... effort is needed to understand the mechanisms [of the jet] ignition process ...**
 - **Agreed!** In FY21 we leveraged CFD and 1D engine models to evaluate different nozzle hole arrangements with select variants tested in thermodynamic/optical test engines. Imaging and heat release data are being used to identify ignition mechanisms and improve the predictive capability of the modeling approaches.
- **R4: ... can [you] narrow options to one ignitor path?**
 - We have already down-selected laser and rail plug igniters. Our current focus is on streamer, nanosecond spark, and active/passive pre-chamber igniters. These igniters have favorable features for advanced combustion concepts under consideration by various OEMs (e.g., high-tumble, mixed-mode). No igniter is optimal for every advanced combustion strategy.
- **R5: ... more measurements of ignition energy - primary and secondary - should be made and reported. / R2: ... compare results between new ignition systems and current ignition systems with equal energy input**
 - We agree this was lacking. As such we reported extensively the primary and deposited energy each plasma igniter.

Technical Accomplishments

- **R2: ... emphasize EGR tolerance at stoichiometric conditions / R4: ... pursue stoichiometric dilute combustion / R5: ... [results that extend] the EGR tolerance of stoichiometric gasoline combustion have not been met**
 - Stoichiometric dilute combustion research comprised roughly half of all work performed for plasma ignition, and more than half of work performed for pre-chamber related research. This includes evaluation of active pre-chamber igniters with air addition.

Collaboration and Coordination

- **R5: ... more collaboration with conventional ignition system suppliers is required to keep the project at a practical level**
 - For this project we worked closely with advanced ignition system suppliers with engagement of conventional ignition system suppliers reserved for for ACE 142.

Future Research

- **R3: ... looking forward to active pre-chamber research. Are catalyst heating conditions sufficiently represented in the future plans? / R5: More work on pre-chamber ignition and high-load ignition should be conducted as these are important to the OEMs.**
 - In FY21, we evaluated active pre-chambers at Argonne and passive pre-chamber igniters at Sandai. At both labs, the dilute ignition testing is nearly complete, and we will transition to evaluation of catalyst heating conditions in Q3/Q4. High-load ignition tests are planned for FY22.
- **R4: How do we leverage current understanding for electrode wear?**
 - While direct prediction of electrode wear is largely beyond our expertise and capability, predictive capability for arc propensity discussed here is essential for associated electrode wear calculations. We are accordingly working with modeling groups that specialize in wear prediction to ensure compatibility with our discharge prediction methods.

Collaboration and Coordination

- **PACE Coordination**

- Internal pre-chamber spark ignition modeling (*Scarcelli, ACE 141*)
- Ignition prediction at lean/dilute part-load and boosted high-load (*Ameen, ACE 146*)
- Associated auto-ignition characteristics from BDI generated ozone (*Wagnon, ACE 139*)
- Catalyst warm-up operation during cold-start (*Edwards, ACE 145*)

- **Connections to other DOE projects**

- **DE-EE0008874:** Development of a High-Fidelity LTP Model for Predictive Simulation Tools
PIs: Nick Tsolas (U. Auburn), Fabrizio Bissetti (U. Texas – Austin)
- **DE-SC0013824:** SBIR Phase IIB, Low-energy nanosecond pulsed ignition system
PI: Dan Singleton (Transient Plasma Systems Inc.)
- **HPC4Mfg (Round 5):** Modeling of Non-equilibrium Plasma for Automotive Applications
PI: Dan Singleton (Transient Plasma Systems Inc.)

- **External Collaborations**

- *Tenneco / Transient Plasma Systems Inc.:* Plasma igniter development and testing
- *Mahle Powertrain:* Integration of active pre-chamber igniter into PACE engine
- *Gamma Technologies:* Development of 1D pre-chamber ignition modules
- *CMT Motores:* Passive pre-chamber testing with plasma ignition
- *Esgee Technologies, U. Texas, U. Auburn:* High-fidelity plasma discharge modeling

Remaining Challenges and Barriers

- **Streamer plasma ignition works best for lean combustion, but is less effective at dilute conditions**
 - Most discharge energy (95%+) is reflected back to the pulse generator. Methods for improved energy deposition via improved impedance matching are needed.
 - Simplified methods for modeling streamer discharges are needed that capture the streamer growth using rules-based 1D growth and branching with minimal computational time
 - A comparative study of discharge voltage and insulator thickness for BDI is needed along with an evaluation of best-practice manufacturing methods and dielectric material properties.
- **NRPD BDI do not produce ozone concentrations observed during static-cell testing**
 - Temperature is the likely culprit, so lower intake temperature conditions need to be evaluated.
- **Equilibrium plasma from nanosecond sparks result in significant electrode erosion**
 - Electrode configurations that minimize applied voltage while maximizing deposition efficiency are needed
- **Pre-chamber ignition performs poorly at idle & cold-start conditions due to excess PC residual gases**
 - It is unclear what nozzle hole patterns work best for different conditions and importantly what works well across the load/speed map. Validated methods for rapid hole patternation evaluation are needed.
 - Improved ignitability of internal PC fuel/air/residual gas mixtures via high-energy ignition concepts need evaluation
 - Still unclear what turbulence model is best (WSR?, G-Eqn?, ECFM?) and how to treat heat transfer (e.g., conjugate heat transfer?)
 - Quantitative characterization of PC jet-exit products needed for better understanding of ignition mechanisms
 - PC heat losses are a major efficiency challenge. Thermo swing coatings are needed to minimize these losses

Future Work

- **Nanosecond pulse BDI ozone formation experiments**
 - Evaluate why engine generated ozone does not match static cell or modeling results
 - Switch to RF BDI if NRPD BDI continues to fail
- **Pre-chamber ignition**
 - Perform direct sampling within PC to evaluate 1D model performance
 - Implement/calibrate 1D jet-ignition combustion model that matches burn rates & observed combustion behavior
- **Catalyst light-off during cold-start experiments (PC and plasma)**
 - Demonstrate comparable or superior performance to baseline spark testing
 - ACEC TT Cold-Start Protocol
 - 1300 rpm, 2 bar IMEP, 20°C coolant & intake temperature
 - Exhaust Heat Flux: 3 – 10 kW/liter (stoichiometric)
- **High-load crossflow facility and engine testing: 80% peak load @ 2000 rpm**
 - Measure burn rates with varying crossflow velocities
 - Demonstrate improved high-load KLSA due to faster early burn rates with PC & NRPD plasma ignition
- **Reduced order plasma streamer modeling**
 - Develop simplified rules-based plasma streamer ignition model that can be implemented as a UDF in an engineering-level combustion solver

Summary

Relevance

- PACE goals speed discovery of knowledge, improve engine design tools, and enable market-competitive powertrain solutions with potential for best-in-class lifecycle emissions
- Tasks directly address USDRIVE research priority 1: Dilute Gasoline Combustion and priority 3: Low-Temperature Combustion (LTC)
 - Removes barriers to advanced ignition

Approach

- Experiment facilities developed to replicate relevant conditions at dilute, high-load, and cold-start; with companion diagnostics to identify relevant ignition phenomena
- High-fidelity discharge and ignition modeling capability developed to identify dominant ignition mechanisms that can then be used for reduced order model development
- Combination of thermodynamic and optical engine experiments performed using custom igniter hardware to evaluate ignition mechanisms and benchmark performance

Accomplishments

- Demonstrated that streamer igniters have low deposited-to-discharge energy efficiency due to poor impedance matching of the voltage pulse
- Developed a method to evaluate igniter induced early flame growth rates using heat release data – validated with flame kernel growth imaging

Accomplishments (Cont.)

- Successfully modeled multi-pulse streamer ignition using a combination of high-fidelity discharge simulations and a newly developed LTP energy source model
- Demonstrated increased dilution tolerance with active PC
- Used developed 1D PC gas exchange & ignition models to evaluate the influence of active PC parameters on engine performance
- Demonstrated improved lean ignition limit with passive PC relative to high-energy spark through nozzle hole optimization

Collaborations

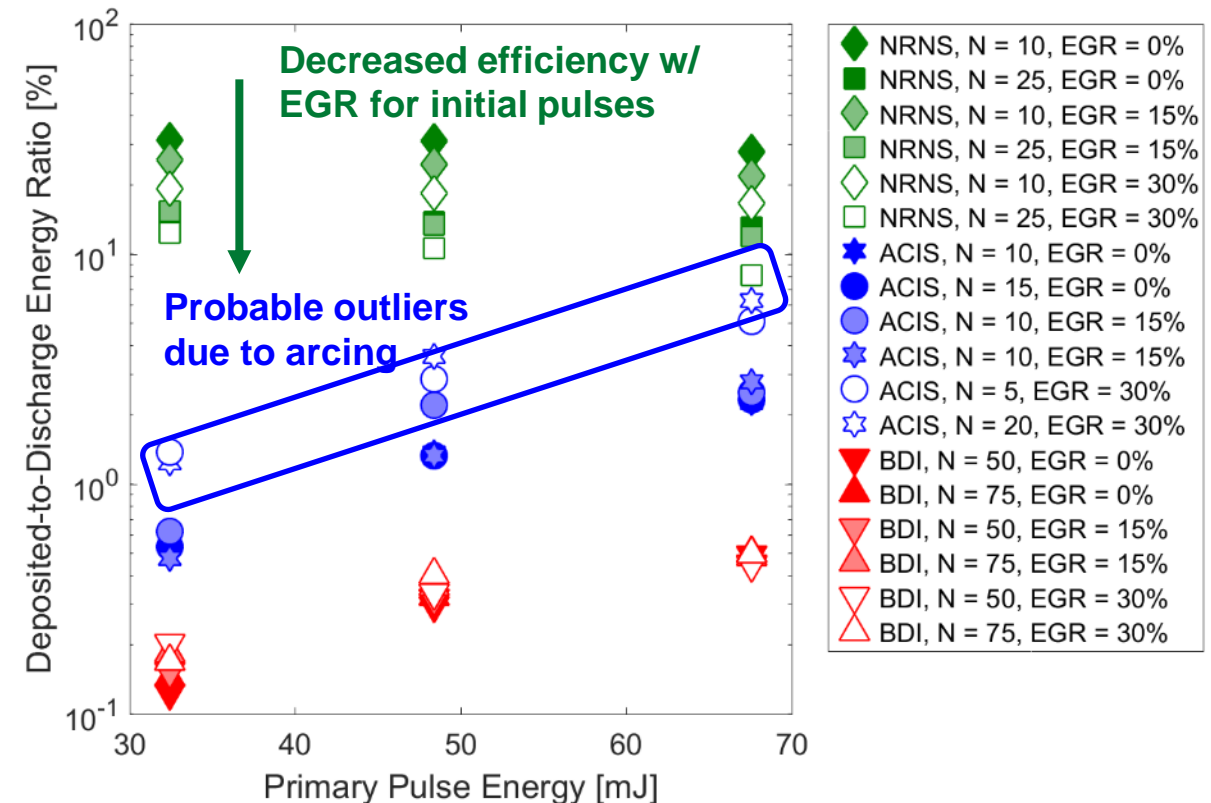
- PACE is a collaboration of 5 national laboratories; work plans are developed considering input from ACEC TT, code developers, and industry users
- PACE projects presented at AEC MOU program review meeting
- External collaborations with Tenneco, TPS, CMT, U. Auburn, U. Texas, and other university partners

Future Work

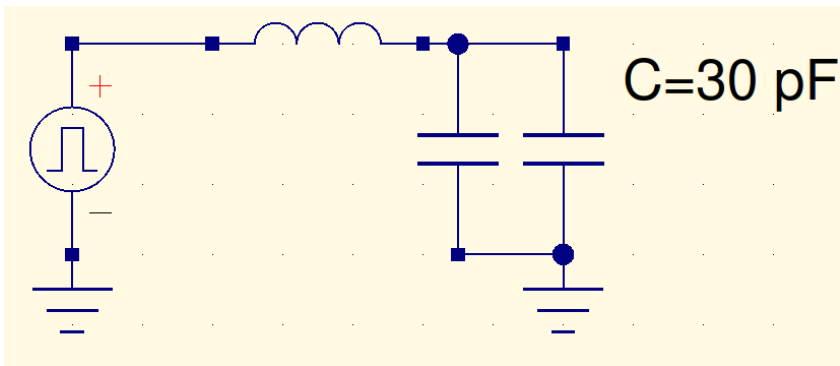
- Nanosecond pulse BDI ozone formation experiments
- Pre-chamber ignition 1D jet ignition mode development
- Catalyst light-off during cold-start experiments (PC and plasma)
- High-load crossflow facility and engine testing:
- Reduced order plasma streamer modeling

BACKUP SLIDES

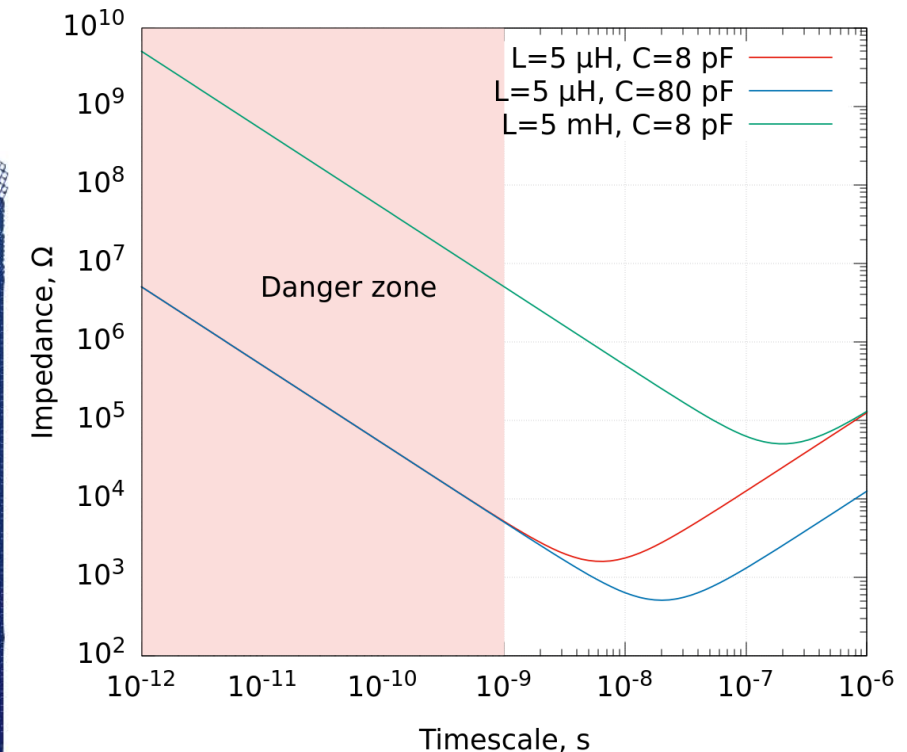
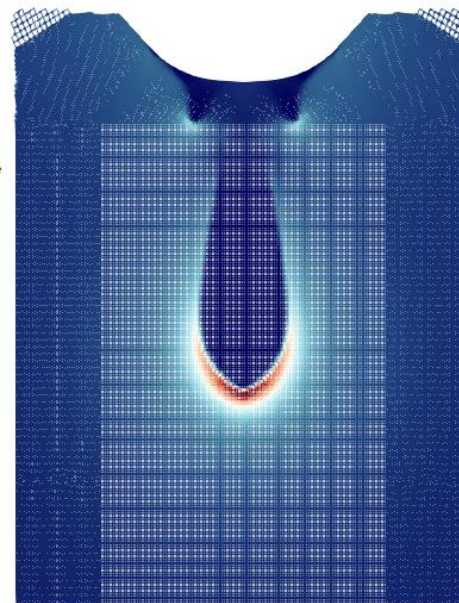
- **Measured energy deposition for nanosecond spark and streamer igniters**
 - Specified discharge energy with pressure-rise calorimetry used to measure deposited energy
 - Evaluated impact of **discharge number** and **EGR composition**
 - Inert mixtures only
- **Nanosecond spark energy deposition**
More efficient
 - Efficiency drops with successive pulses
 - EGR decreases deposition efficiency
- **Corona deposition efficiency drops by an order of magnitude (Max 5%)**
 - Linear increase with pulse voltage (i.e., energy)
 - Invariant to EGR
- **BDI deposition efficiency less than 1%**
 - Linear increase with pulse voltage (i.e., energy)
 - Invariant to EGR



- Circuit impedance (and thus current) controlled by adjusting upstream capacitance and inductance



- VizGlow simulations are run for a $2\mu\text{m}$ mesh in the streamer vicinity
 - Photoionization neglected
 - No fluid dynamics
 - No surface electron emission



• CONVERGE CFD setting

- No turbulence model
- AMR with a minimum 31.25 μm cell size
- Chemistry solved using Foundational Fuel Chemistry Model (FFCM-1) <http://nanoenergy.stanford.edu/ffcm1>
- Source term due to Low Temperature Plasma, S_{LTP} given by

$$B(t) = \left(1 + fl\left(\frac{t}{\tau_p} - 1\right) - fl\left(\frac{t}{\tau_p} - \hat{\tau}\right) \right) \times H\left(t - fl\left(\frac{t}{N\tau_p}\right)\right)$$

$$f(x, y, z) = e^{-\left(\frac{x^2 + y^2}{2\sigma_g^2} + \frac{(z - m(z))^2}{2\sigma_f^2}\right)}$$

where $m(z)$ results in heating close to z_a , z_c , and z_i via:

$$m(z) = \begin{cases} z_a & z \geq \alpha z_i \\ z_i & \alpha z_i < z < \beta z_i \\ z_c & z \leq \beta z_i \end{cases}$$

$$S_{LTP}(x, y, z, t) = AB(t) (f(x, y, z) + g(x, y)(h_a(z) + h_c(z)))$$

$$g(x, y) = e^{-\left(\frac{x^2 + y^2}{2\sigma_g^2}\right)}$$

where

$$h_a(z) = \begin{cases} 0 & z \geq z_a \\ a_a z^2 + b_a z + c_a & z_i \leq z \leq z_a \\ 0 & z \leq z_i \end{cases}$$

$$\begin{aligned} a_a &= 4(1 - H_a)/d_a \\ b_a &= 4(H_a(z_i + z_a) - z_i - z_a)/d_a \\ c_a &= (2z_i z_a(1 - 2H_a) + z_i^2 + z_a^2)/d_a \\ d_a &= z_i^2 - 2.0z_i z_a + z_a^2 \end{aligned}$$

$$h_c(z) = \begin{cases} 0 & z \leq z_c \\ a_c z^2 + b_c z + c_c & z_c \leq z \leq z_i \\ 0 & z \geq z_i \end{cases}$$

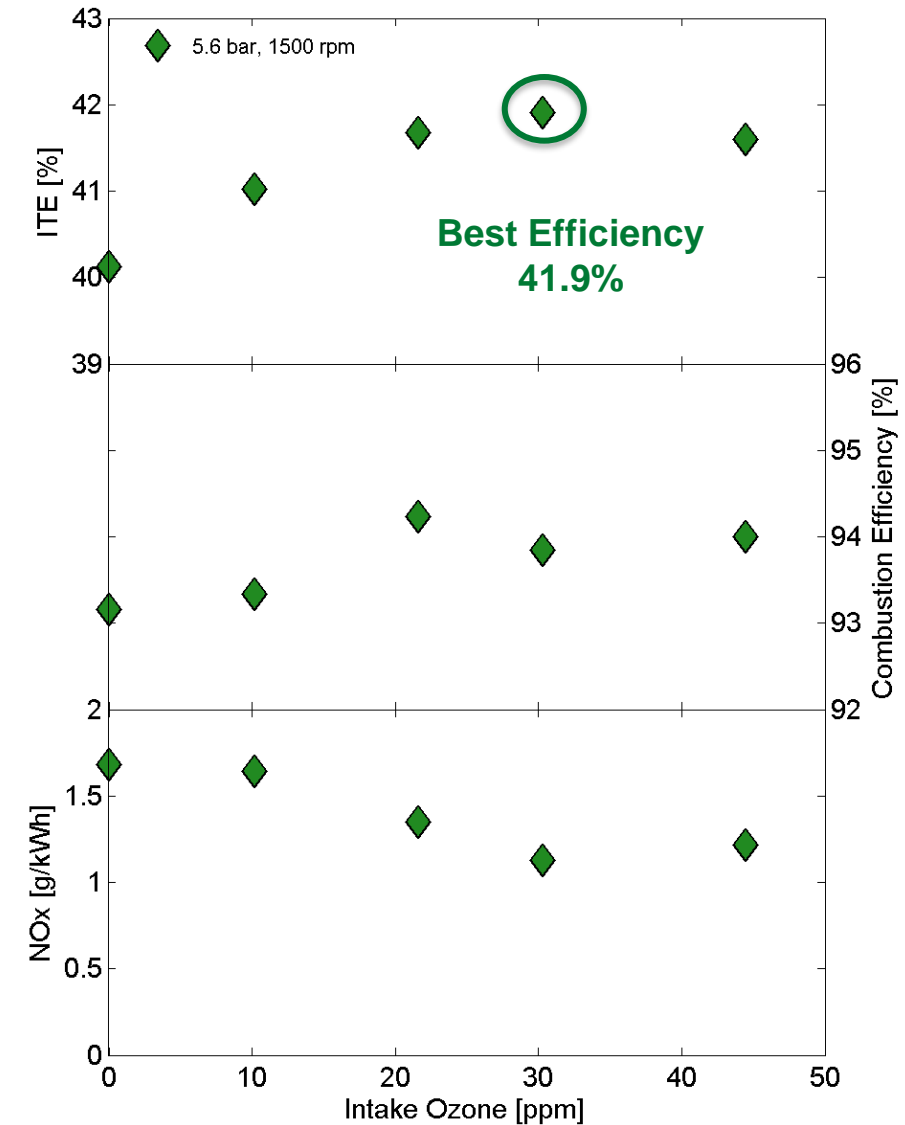
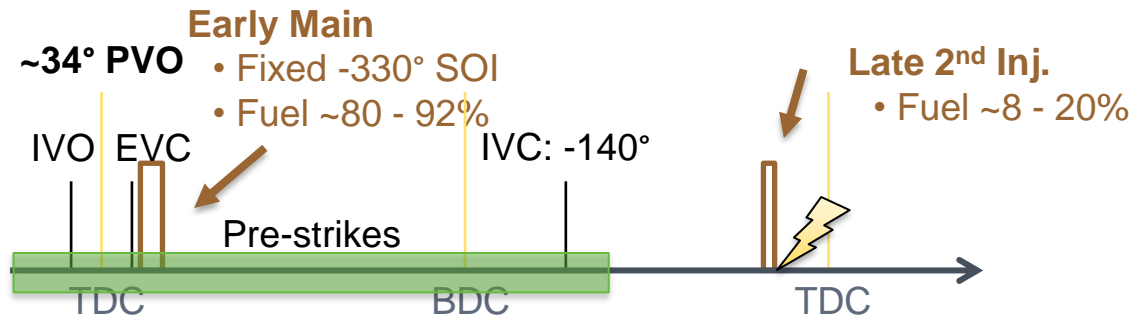
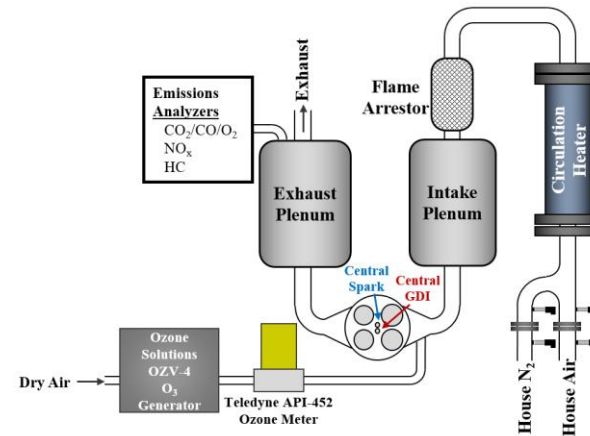
where

$$\begin{aligned} a_c &= 4(1 - H_c)/d_c \\ b_c &= 4(H_c(z_i + z_c) - z_i - z_c)/d_c \\ c_c &= (2z_i z_c(1 - 2H_c) + z_i^2 + z_c^2)/d_c \\ d_c &= z_i^2 - 2.0z_i z_c + z_c^2 \end{aligned}$$

O₃ Enhanced Mixed-Mode:

- Intake seeded ozone with conventional spark - baseline
- **BDI formed ozone and ignition - ongoing**
- Discharge and ignition imaging
- **Ozone absorption measurements**

SG2 Central DI/SI	
Injector	8-hole solenoid (HDEV 1.2)
Stroke/Bore	1.11
CR	13 (12.6 w/ PC)
Displacement [L]	0.55
Intake press. [bar]	1
Engine Speed [rpm]	800, 1300, 1500
phi	0.36, 0.48
Intake O ₃ [ppm]	0 - 110
IMEP [bar]	1.0, 3.5, 5.6

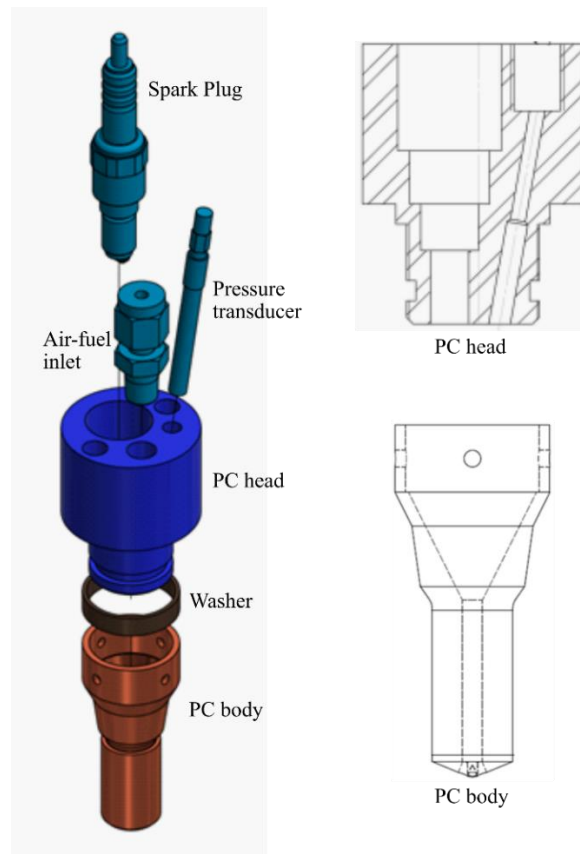


Technical Backup 5: Pre-chamber geometry

A.E.03
S.E.03.01

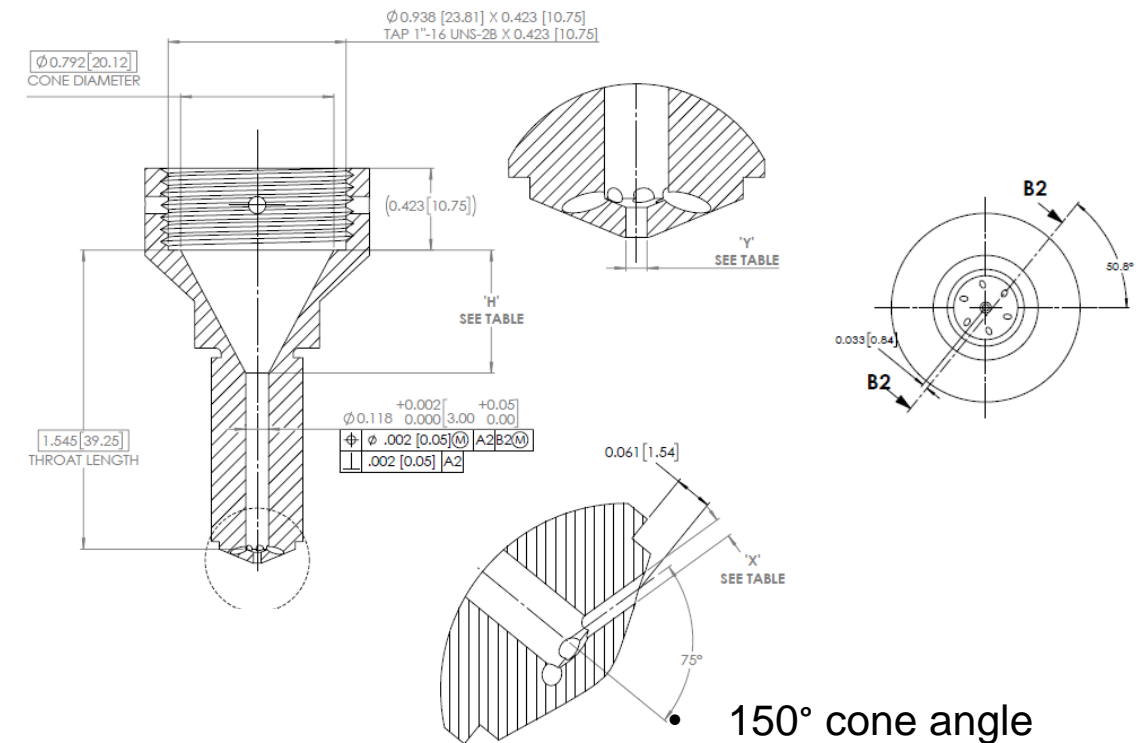
ANL

Igniter	Hole (#/diam. [mm])	PC Volume [cc]	Cone Angle [°]	Throat Diam. [mm]
ANL 1	4 / 2.0	2.0	80°	7.0



SNL

Igniter	Radial Hole (#/diam. [mm])	Center Hole (#/diam. [mm])	PC Volume [cc]
PC 2-1	6 / 0.8	1 / 1.0	2.0
PC 2-2	6 / 0.8	1 / 1.0	1.7
PC 2-3	6 / 1.2	1 / 1.0	1.7



- 150° cone angle
- 12.5° tangential angle
- Throat diameter: 3 mm