



# Distribution System State Estimator

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U.S. DEPARTMENT OF  
**ENERGY**

Energy Efficiency &  
Renewable Energy



**Robust Distributed State Estimator for  
Interconnected Transmission and  
Distribution Networks  
Northeastern University**

May 16, 2019

# Motivation

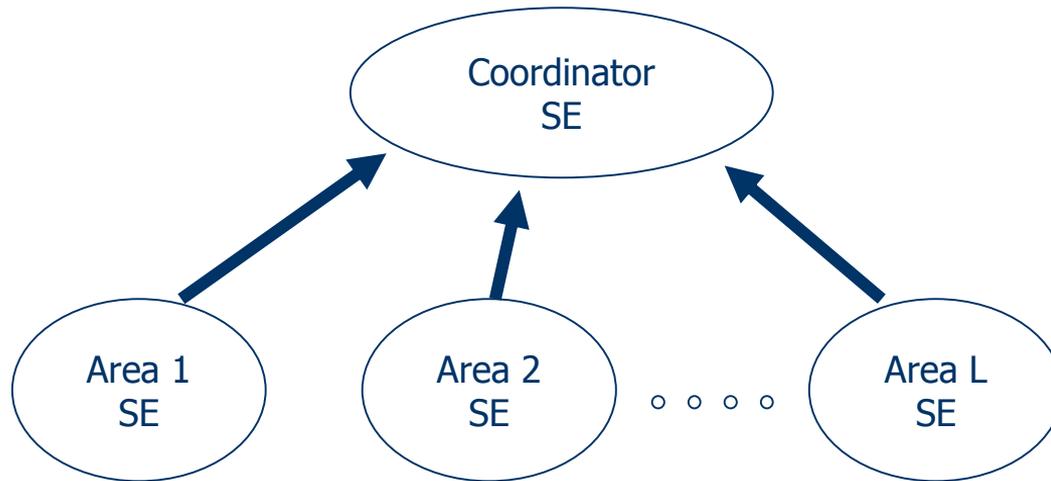
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- Computational burden: finding a scalable solution which will remain viable as the network size increases.
- Robustness: maintain the ability to detect and remove bad data, thus provide an unbiased state estimate both for the distribution and transmission system states.
- Stitching the transmission and distribution system real-time models, by combined estimation of transmission and distribution system states.

# Multi-area SE

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- Each area SE estimates its own state.
- Coordinator SE
  - merges the solutions, and
  - processes bad data for boundary measurements.



# Properties

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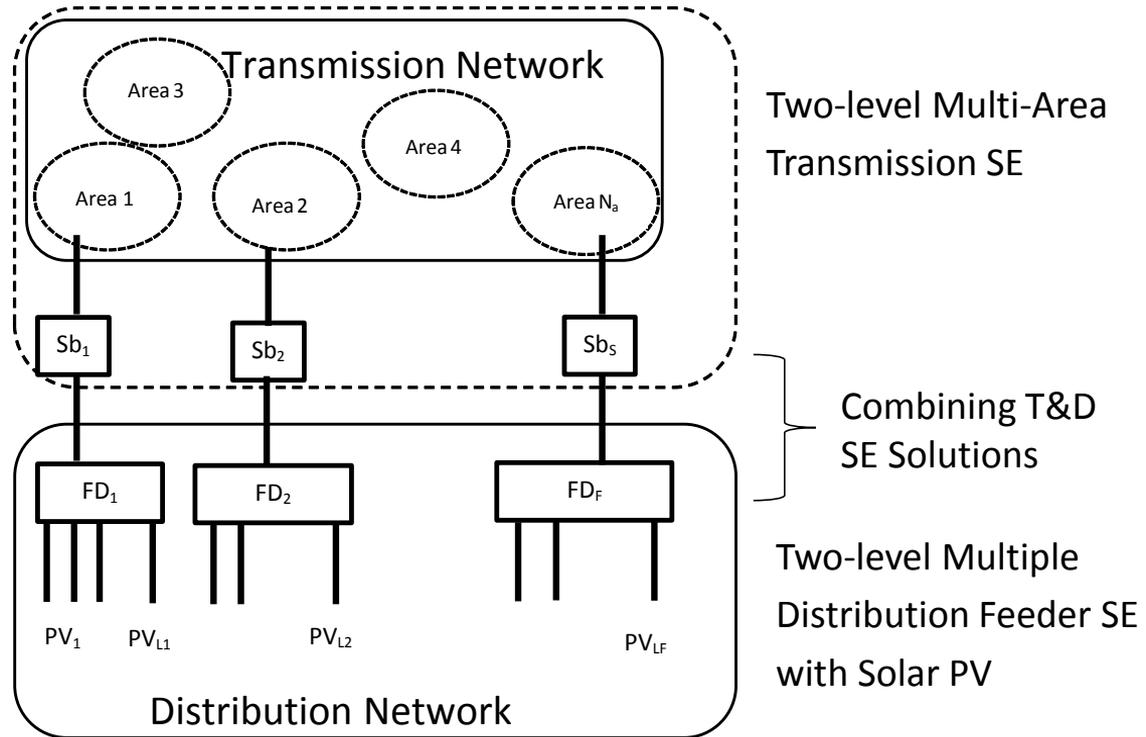
- No boundary measurements are discarded.
- All detectable / identifiable bad data are detected and identified.
- PMU measurements are effectively used, but not required for this scheme to work.
- Areas do not share network data (internal system details) or intermediate iteration results. They only provide boundary network model and measurements and their estimated states to the coordinator.
- Applicable to both single phase [positive seq.] and three-phase SE, areas representing either transmission control areas or distribution system feeders which may or may not be configured radially.

# Robustness

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- Conventional WLS SE followed by the largest normalized residual (LNR) – Plan to use a recently developed technique which drastically increases the computational speed of LNR test for very large scale systems.
- Alternative LAV SE: Plan to use a recently developed multi-copy multi-partition approach to address the scalability issue while maintaining robustness against bad data.

# Project Architecture



# Measurements

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- SCADA measurements
  - Active/Reactive power injections
  - Active/Reactive power flows
  - Voltage magnitude measurements
- Generated from OpenDSS
  - Three-phase power flow program
  - Developed by EPRI



# Weighted Least Squares Formulation

$$\min_{r_i} \sum_{i=1}^m W_{ii} r_i^2$$

$$\text{s.t. } z_i = h_i(x) + r_i, \quad i = 1, \dots, m.$$

Not Robust Against  
Bad Data, requires  
BD processing

$$r_i^N = \frac{|r_i|}{\sqrt{\Omega_{ii}}}, \quad i = 1, \dots, m.$$

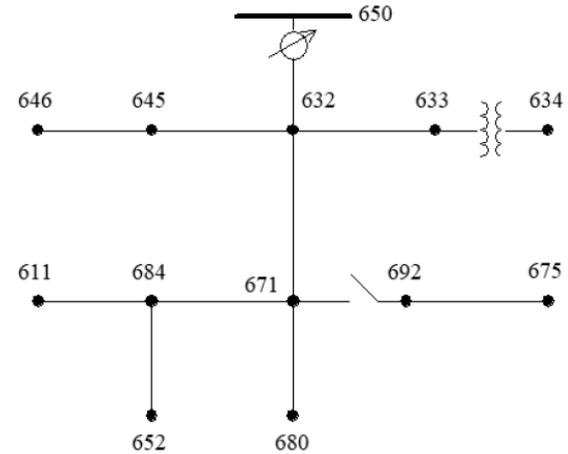
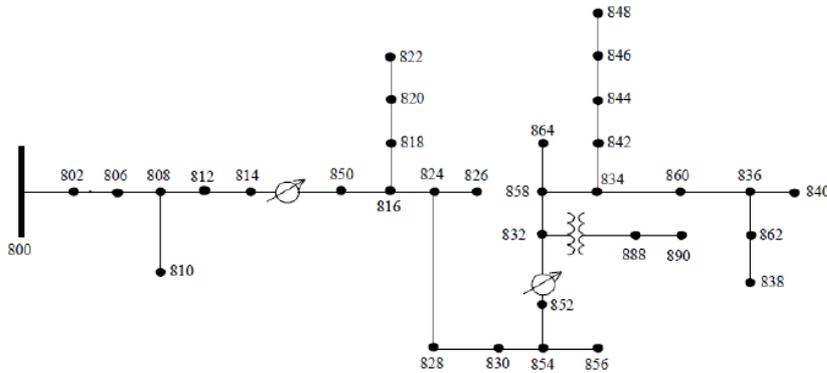
$$\Omega = R - H(H^T R^{-1} H)^{-1} H^T$$

$$r_i^N \geq 3, \quad i = 1, \dots, m.$$

# Distribution State Estimation

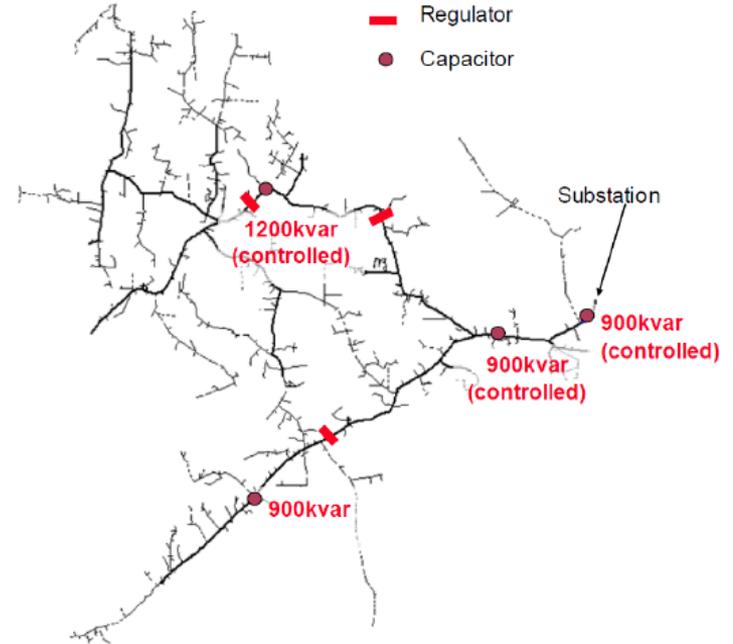
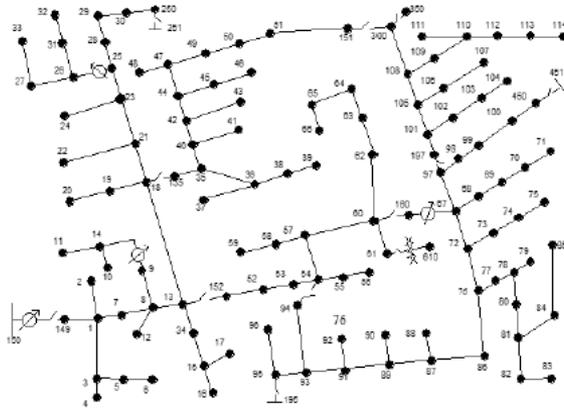
- IEEE Test Feeders

- 13 node feeder
- 34 node feeder



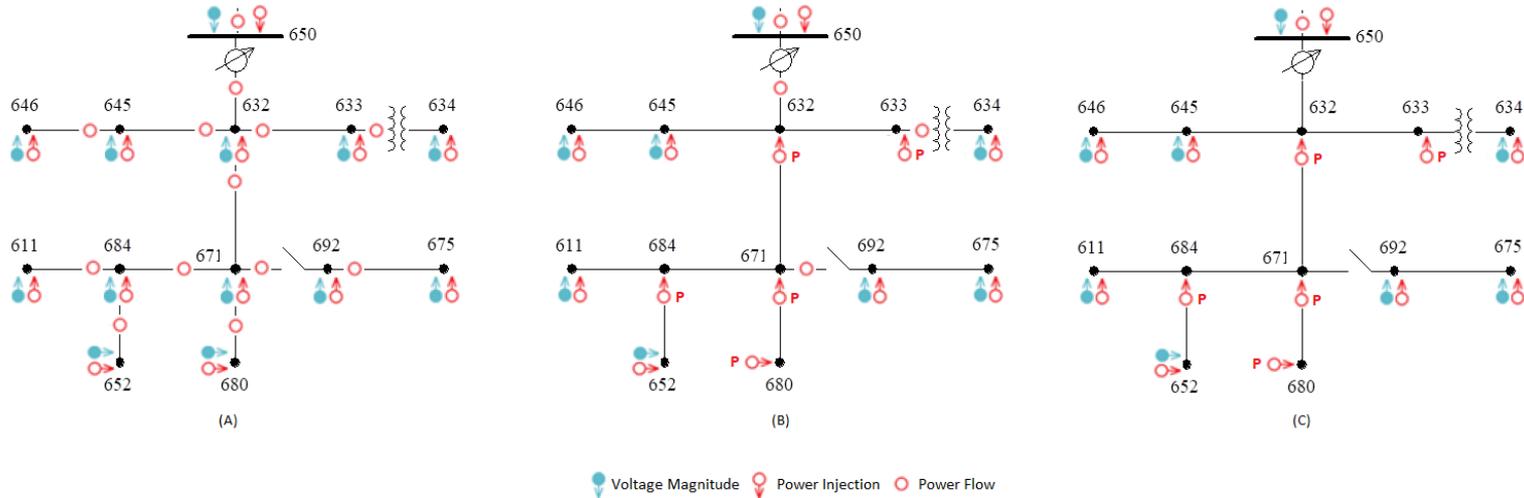
# Distribution State Estimation

- IEEE Test Feeders
  - 123 node feeder
  - 8500 node feeder



# Distribution State Estimation

- Results
  - Measurement scenarios



# Distribution State Estimation

- Results
  - MSE values
  - Diagonal of inverse of Gain matrix

Perfect Measurements

Scenarios	$V$	$\theta$	Combined
Case A	$1.6125 \times 10^{-7}$	$1.2403 \times 10^{-6}$	$8.8437 \times 10^{-7}$
Case B	$7.6933 \times 10^{-6}$	$2.6239 \times 10^{-5}$	$1.9335 \times 10^{-5}$
Case C	$6.5733 \times 10^{-6}$	$5.0437 \times 10^{-5}$	$3.5966 \times 10^{-5}$

Gaussian Noise

Scenarios	$V$	$\theta$	Combined
Case A	$7.5934 \times 10^{-4}$	$4.859 \times 10^{-3}$	$3.4829 \times 10^{-3}$
Case B	$1.7352 \times 10^{-3}$	$7.8424 \times 10^{-3}$	$5.7013 \times 10^{-3}$
Case C	$1.7767 \times 10^{-3}$	$9.7926 \times 10^{-3}$	$7.0580 \times 10^{-3}$

Diagonal of  $G^{-1}$

Scenarios	Average	Maximum
Case A	$3.2902 \times 10^{-4}$	$4.6 \times 10^{-3}$
Case B	$3.3896 \times 10^{-4}$	$5.2 \times 10^{-3}$
Case C	$6.6890 \times 10^{-4}$	$1.2 \times 10^{-2}$

# Bad Data Processing

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- LNR test
  - 1. Solve WLS and form residual vector
  - 2. Compute the normalized residuals
  - 3. Find  $k$  such that  $r_k^N$  is the largest one
  - 4. If  $r_k^N > c$ ,  $k$  is suspected of BD; usually  $c = 3$
  - 5. Eliminate or correct  $k$ -th measurement and go back to 1

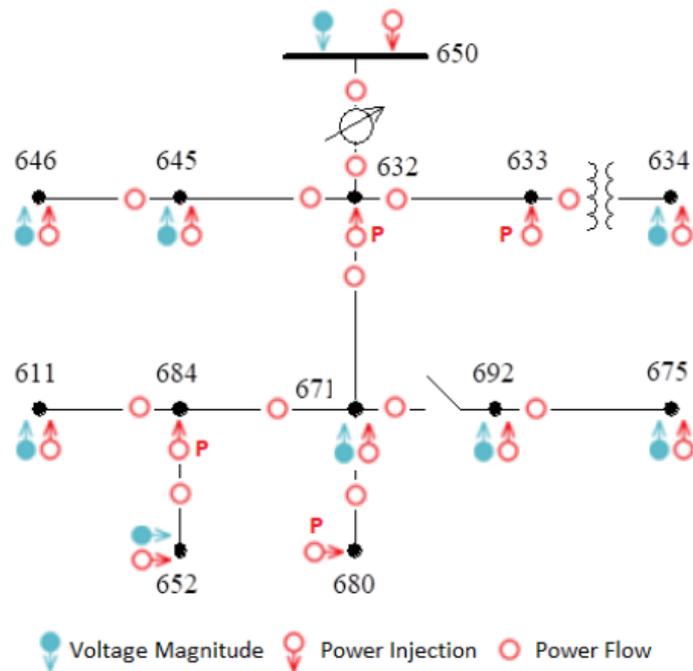
- Correction of BD

- $$z_i \approx z_i^{bad} - \frac{R_{ii}}{\Omega_{ii}} r_i^{bad}$$

# IEEE 13-Node Feeder

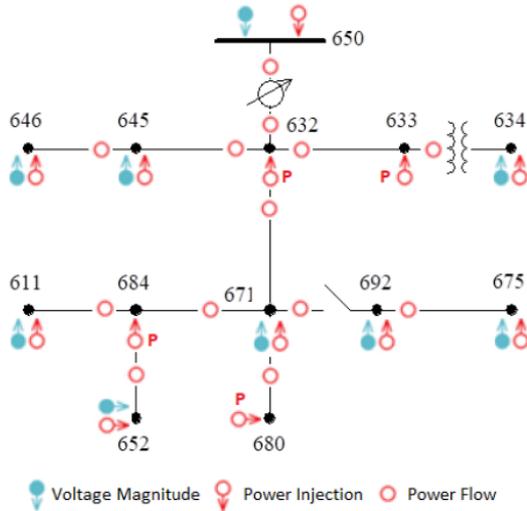
- Perfect and noisy measurements
- Different magnitudes of errors
  - 20, 25, 30, and 50  $\sigma$
  - $\sigma$ : standard deviation

Parameter	Value
$\sigma_{inj}$	0.001
$\sigma_{flow}$	0.001
$\sigma_v$	0.001
$\sigma_{nullInj}^p$	0.0001
tolerance	$10^{-4}$
Iteration Limit	30



# IEEE 13-Node Feeder with Bad Data

- Detection and correction results



BD magnitude ( $\sigma$ )	BD detected	Perc. (%)
20	136	97.84
25	136	97.84
30	139	100
50	139	100

# Least Absolute Value Formulation

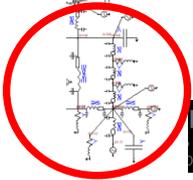
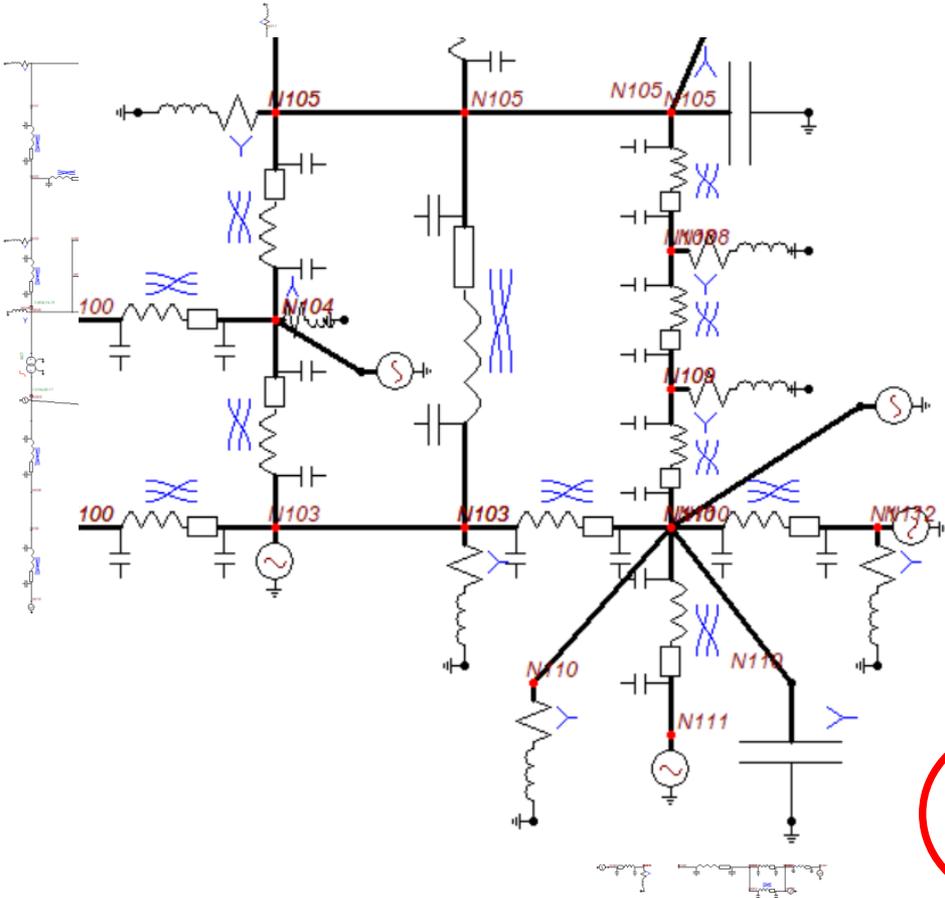
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$$\min_r C^T \cdot |r|$$
$$Z = h(\hat{x}) + r$$
$$Z_e = h_e(\hat{x})$$

- Robust against measurement errors
- Easily incorporates equality constraints

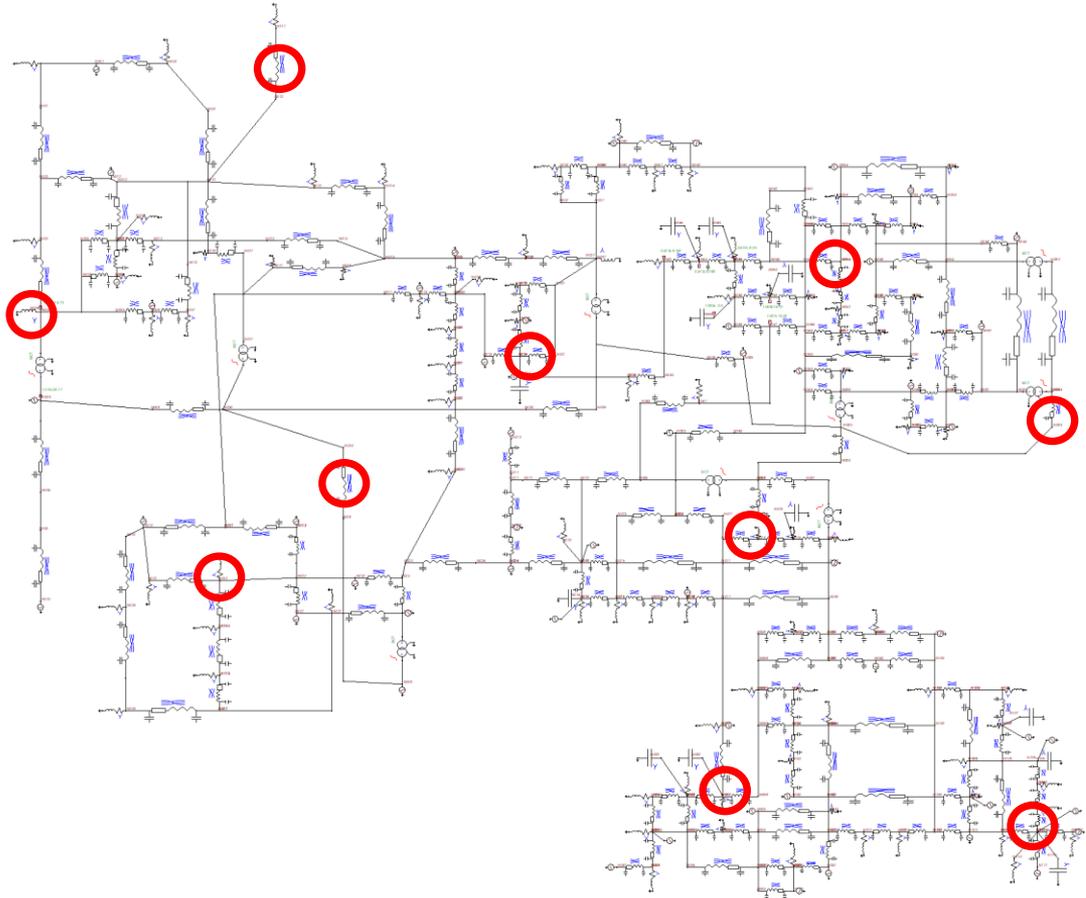
# Simulations

3-Phase Model  
IEEE 118 Bus Test  
System

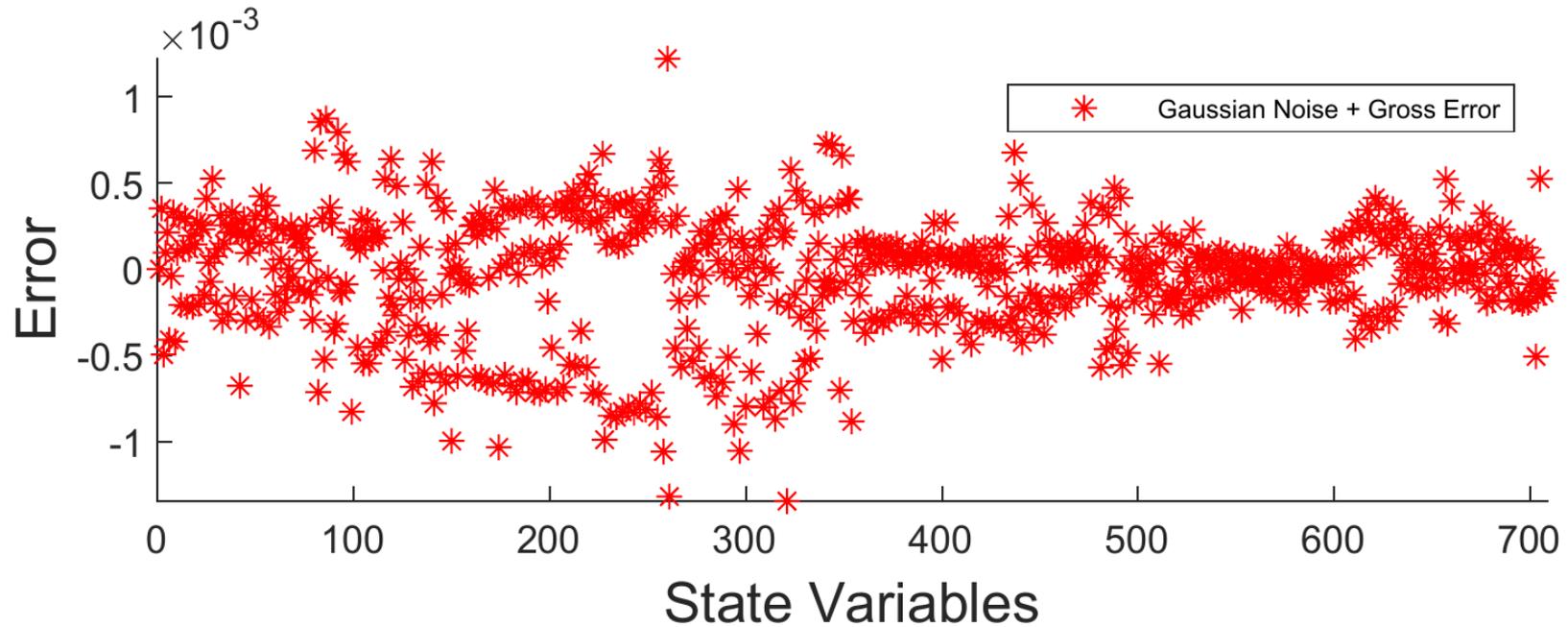


# Simulation Results – Noise + Gross Errors

Measurement	Bus From	Bus To	Phase	Error
P_flow	14	15	A	1 pu
P_flow	69	47	B	1 pu
P_flow	89	85	A	1 pu
Q_flow	8	30	C	1 pu
Q_flow	32	113	B	1 pu
Q_flow	47	46	A	1 pu
P_Inj	-	103	C	1 pu
Q_Inj	-	10	B	1 pu
V_mag	-	2	A	1 pu
P_flow	12	117	B	phase swap
P_flow	12	117	C	phase swap



# Simulation Results – Noise + Gross Errors



# Simulation Results – Noise + Gross Errors

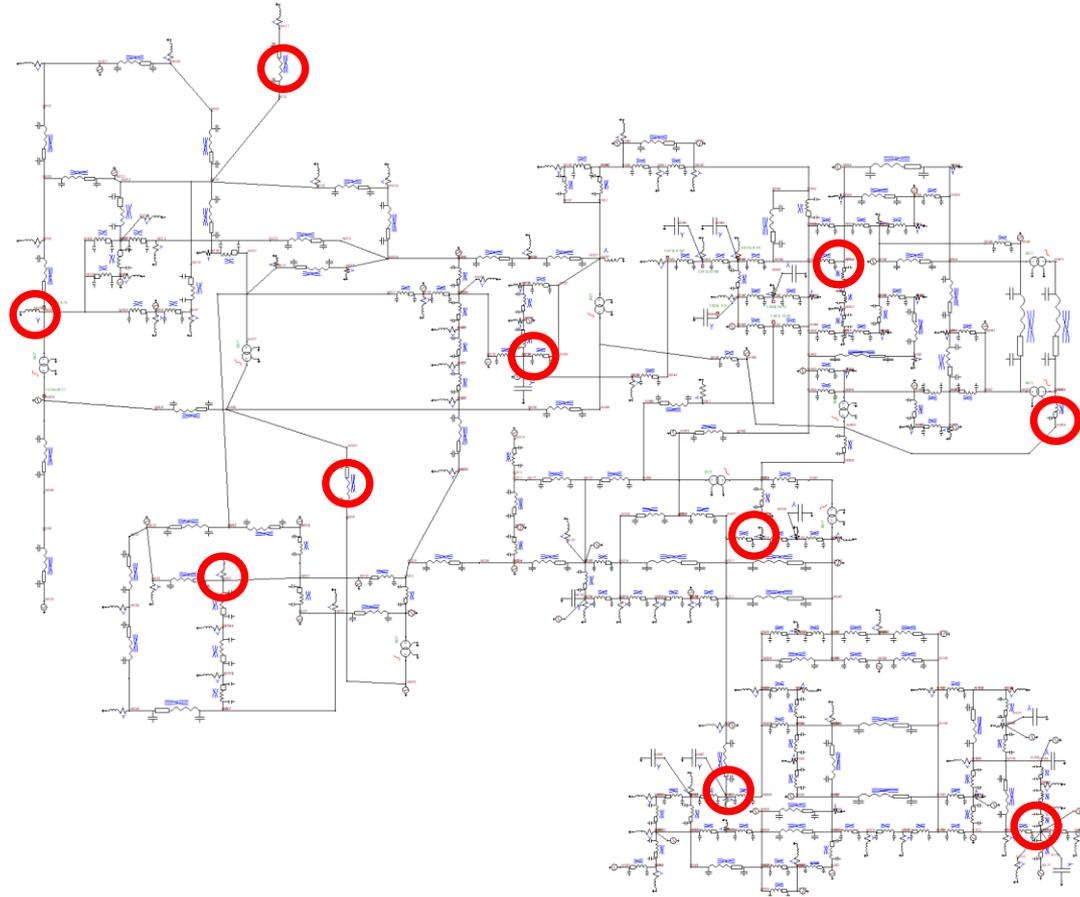
## Gross Error Added

Measurement	Bus From	Bus To	Phase	Error
P_flow	14	15	A	1 pu
P_flow	69	47	B	1 pu
P_flow	89	85	A	1 pu
Q_flow	8	30	C	1 pu
Q_flow	32	113	B	1 pu
Q_flow	47	46	A	1 pu
P_Inj	-	103	C	1 pu
Q_Inj	-	10	B	1 pu
V_mag	-	2	A	1 pu
P_flow	12	117	B	phase swap
P_flow	12	117	C	phase swap

## Simulation Results

Type	Bus From	Bus To	Estimated	Measured	Residues
P_flow	14	15	-0.0065	0.9925	0.9991
P_flow	69	47	0.2958	1.2947	0.9989
P_flow	89	85	0.3617	1.3600	0.9983
P_inj	0	103	0.0856	1.0889	1.0032
Q_flow	8	30	0.1506	1.1518	1.0012
Q_flow	32	113	-0.0865	0.9129	0.9994
Q_flow	47	46	-0.0041	0.9960	1.0001
Q_inj	0	10	-0.2568	0.7406	0.9975
V_mag	0	2	0.6875	1.6083	1.0008
P_flow	12	117	0.1114	0.0949	0.0165
P_flow	12	117	0.0959	0.1118	0.0159

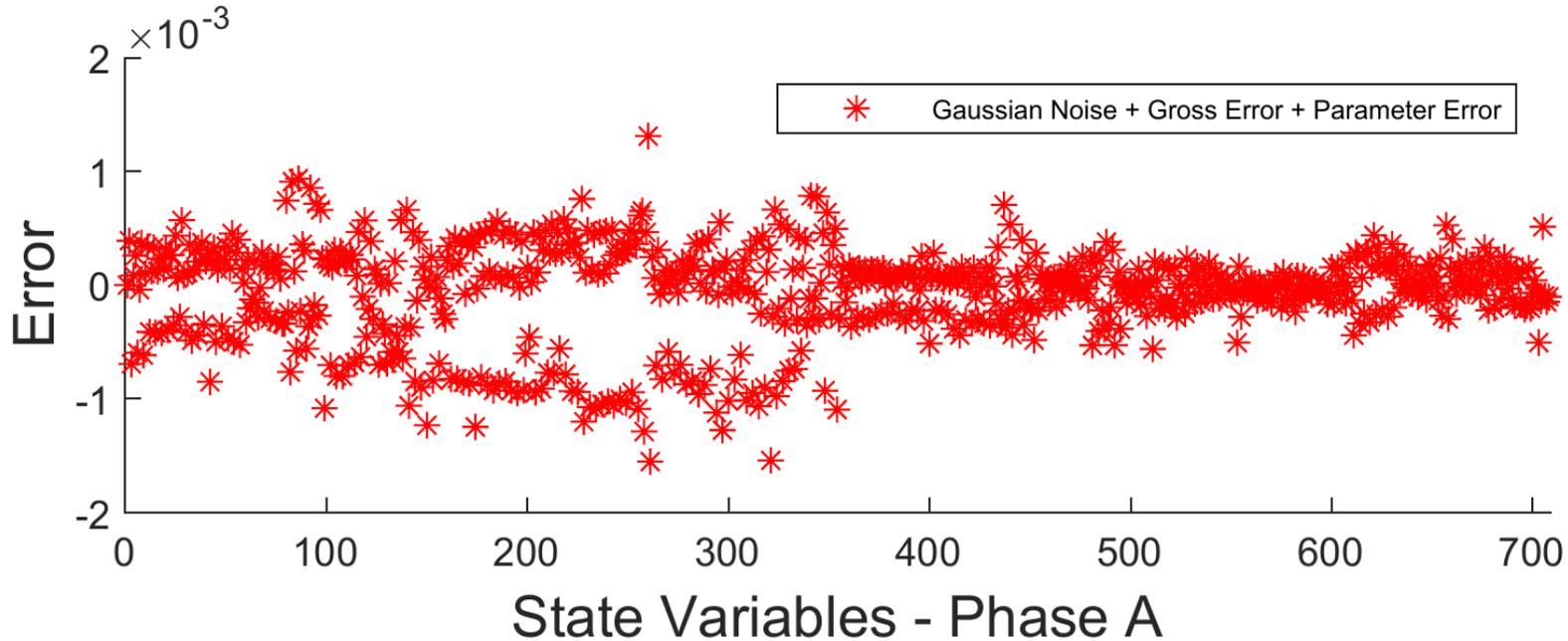
# Simulation Results – Noise + Gross Errors + Bad Parameters



# Simulation Results – Noise + Gross Errors + Bad Parameters

Bus From	Bus To	Phase	R	X	B	R	X	B	R	X	B
			A	A	A	B	B	B	C	C	C
62	67	A	0.05050	0.16652	0.01976	0.02020	0.06661	-0.00564	0.02020	0.06661	-0.00564
62	67	B	0.02020	0.06661	-0.00564	0.05050	0.16652	0.01976	0.02020	0.06661	-0.00564
62	67	C	0.02020	0.06661	-0.00564	0.02020	0.06661	-0.00564	0.05050	0.16652	0.01976

# Simulation Results – Noise + Gross Errors + Bad Parameters



# Conclusion

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- WLS and LAV based DSE are implemented and tested.
- Large numbers of bad data favors LAV implementation.
- Future work:
  - Implement cases with distributed solar PVs
  - Combine DSE and TSE
  - Implement both as multi-area distributed SE

# Questions?

