



# DOE/OE Transmission Reliability Program

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## A persistence Measure and VARPRO-Based Modal Analysis of Ambient Sychrophasor Data

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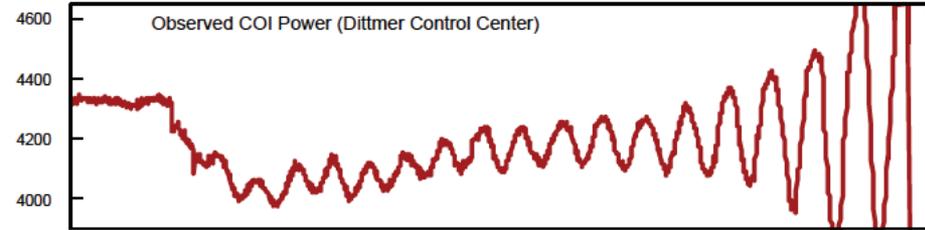


CERTS Review: June 13, 2017, Washington, DC

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ELECTRIC RELIABILITY  
TECHNOLOGY SOLUTIONS

# Background: Monitoring Damping

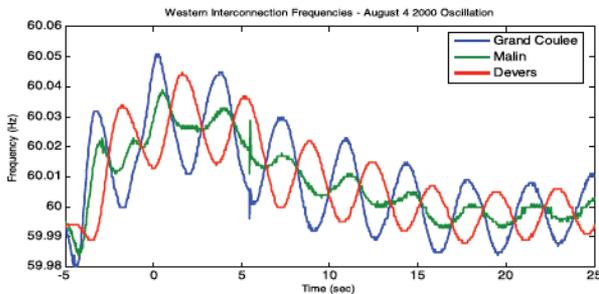
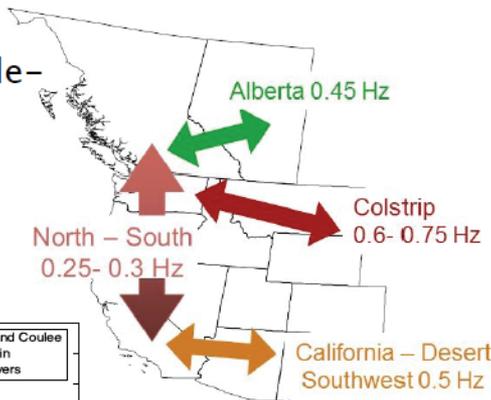
Sustained oscillations show lack of control in the grid, and can lead to blackouts.



## Wide-Area View of Oscillations with Synchrophasors

Synchro-phasors provide wide-area geographic visibility of power oscillations:

- Is it a local or inter-area oscillation?



It would be useful to monitor system damping from ambient data, prior to a disturbance.



D. Kosterev, J. Undrill, "Oscillations in Power Systems," NASPI Jun. 3, 2011

# Details: The Challenges

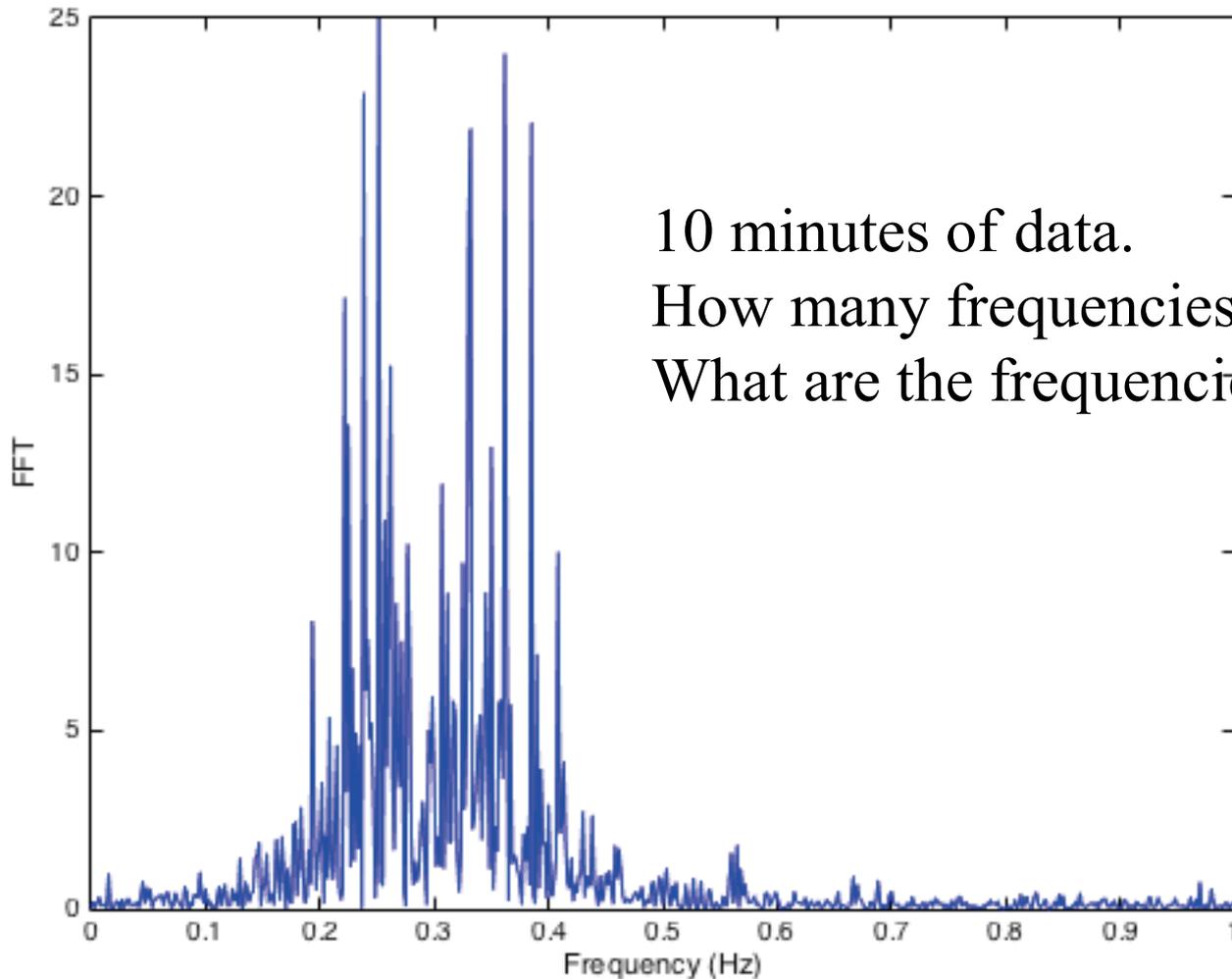
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- Ambient data is noisy.
- Modal analysis is difficult with a short time windows.
- Estimating multiple mode frequencies and damping involves estimating many parameters using low SNR information. Not robust.



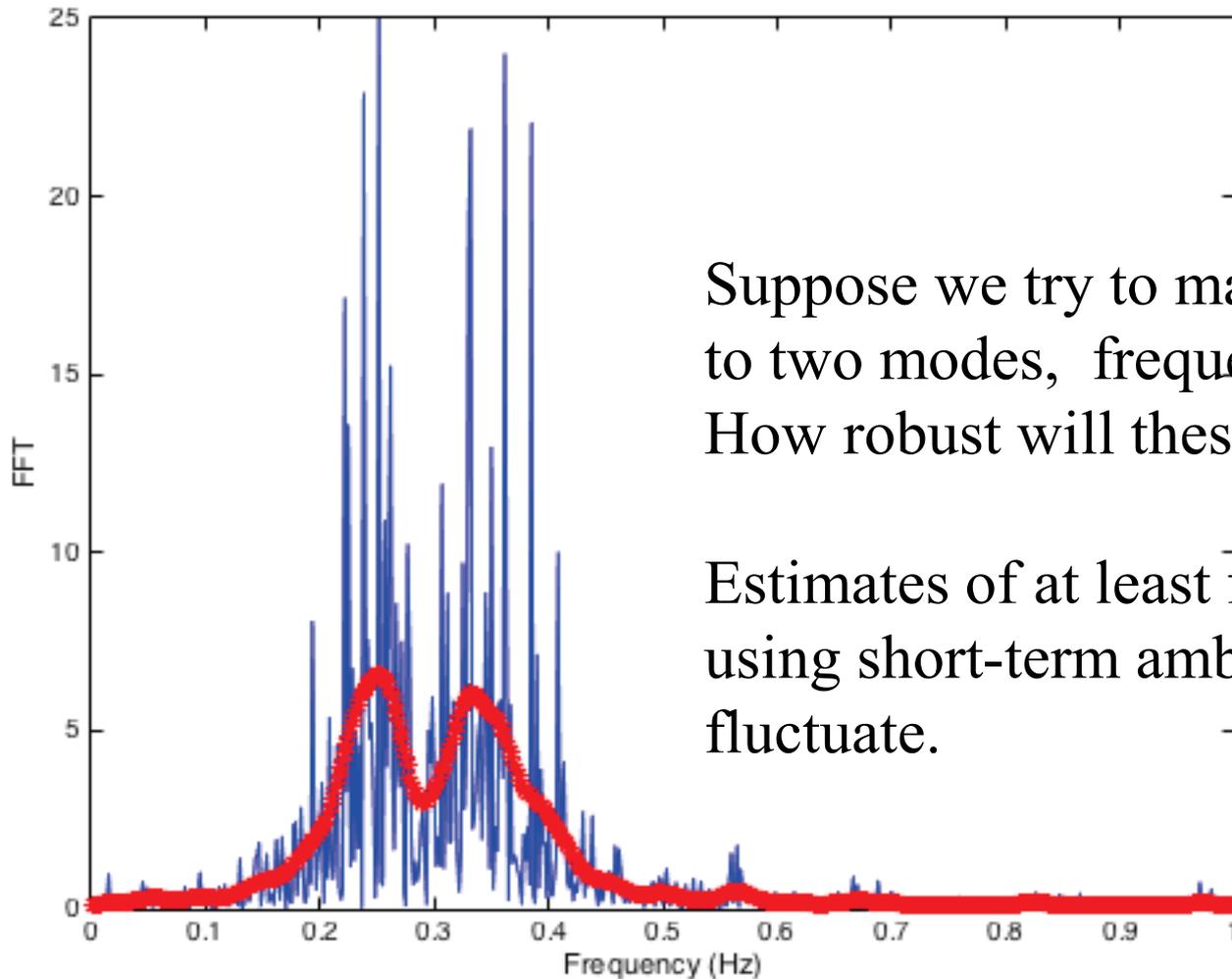
# Challenges

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# Challenges

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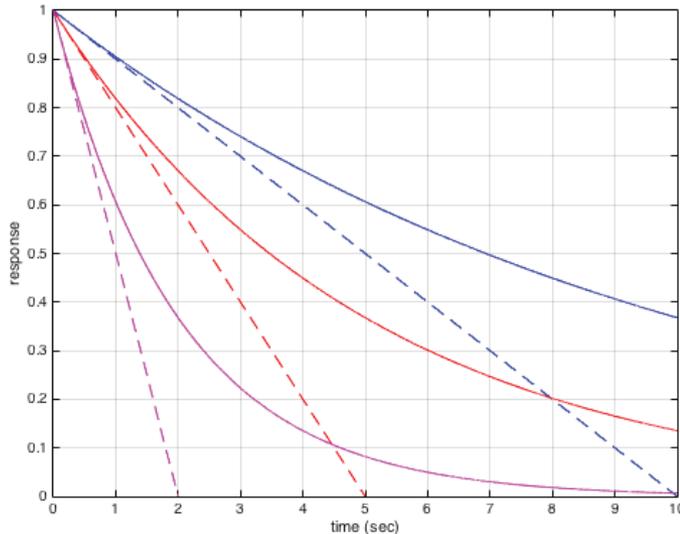
Suppose we try to match data to two modes, frequency and damping. How robust will these estimates be?

Estimates of at least four parameters using short-term ambient data will fluctuate.

# Introduce a *persistence* measure !

- Instead of a modal decomposition (or in addition to), calculate a single **persistence** measure of the duration/decay of a natural response.

The most obvious example is an exponential time-constant.



$$h(t) = e^{-\frac{t}{T}} u(t)$$

The larger the time constant, the longer the "duration" or "persistence" of the response.



# Introduce a Persistence Measure

$$\Upsilon = \left\| \frac{R(\tau)}{R(0)} \right\|_2$$

System Persistence Measure

$$\Upsilon = \frac{\int_{w=-\infty}^{\infty} S(w)^2 dw}{\left( \int_{w=-\infty}^{\infty} S(w) dw \right)^2}$$

Important Properties:

- Scales linearly with “stretching” of impulse response, regardless of shape.
- For exponentials, doubling the time constant, doubles the measure.
  - For single mode, non-oscillatory exponentially-decaying impulse response, **it equals the time constant**;
  - For single mode, oscillatory exponentially-decaying impulse response **it is half the time constant**.

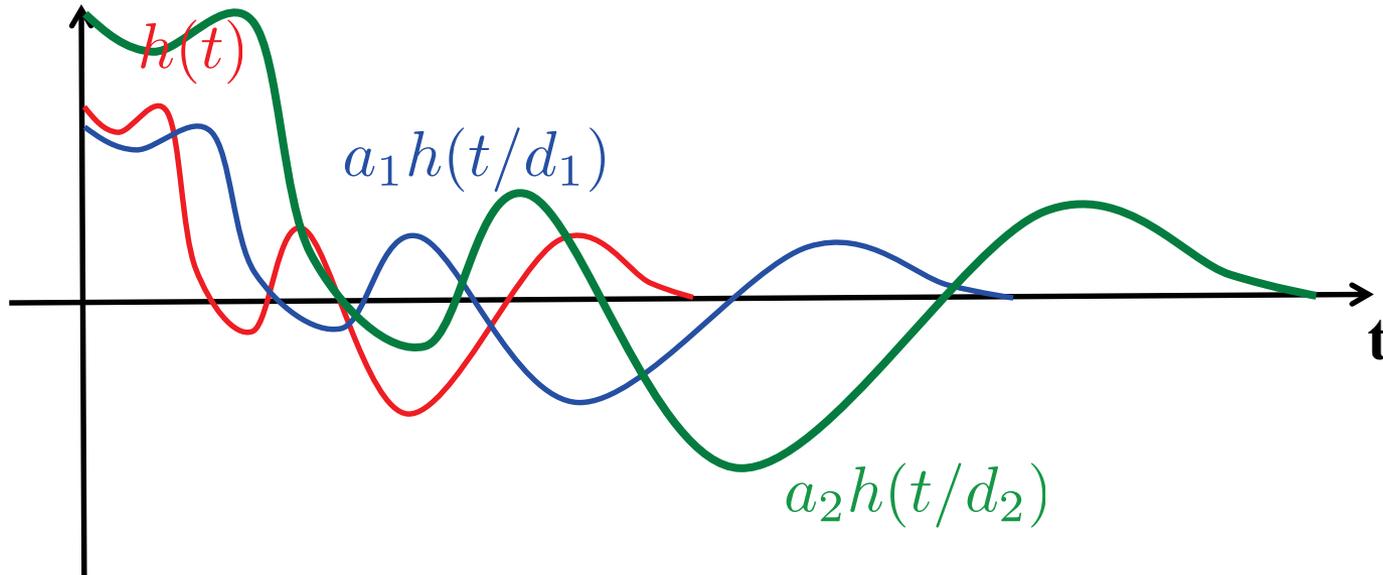


Calculable from the autocorrelation!

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# Stretching Property



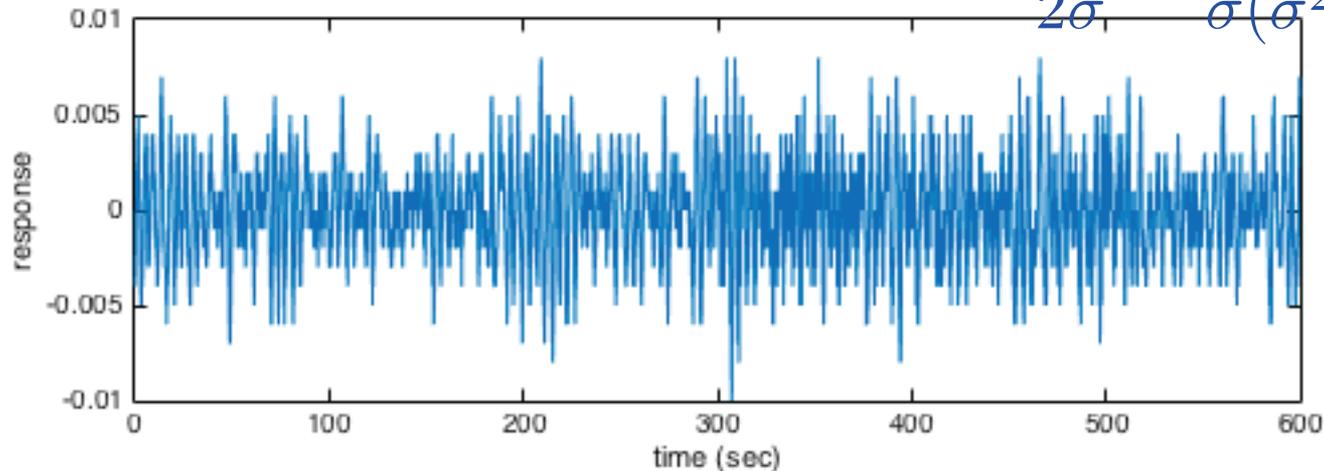
$$\begin{aligned} h(t) &\rightarrow \Upsilon_0 \\ a_1 h(t/d_1) &\rightarrow d_1 \Upsilon_0 \\ a_2 h(t/d_2) &\rightarrow d_2 \Upsilon_0 \end{aligned}$$

All these signals have the same shape. They differ in amplitude and stretching. The metric scales only with time-stretching. (Indifferent to amplitude.)



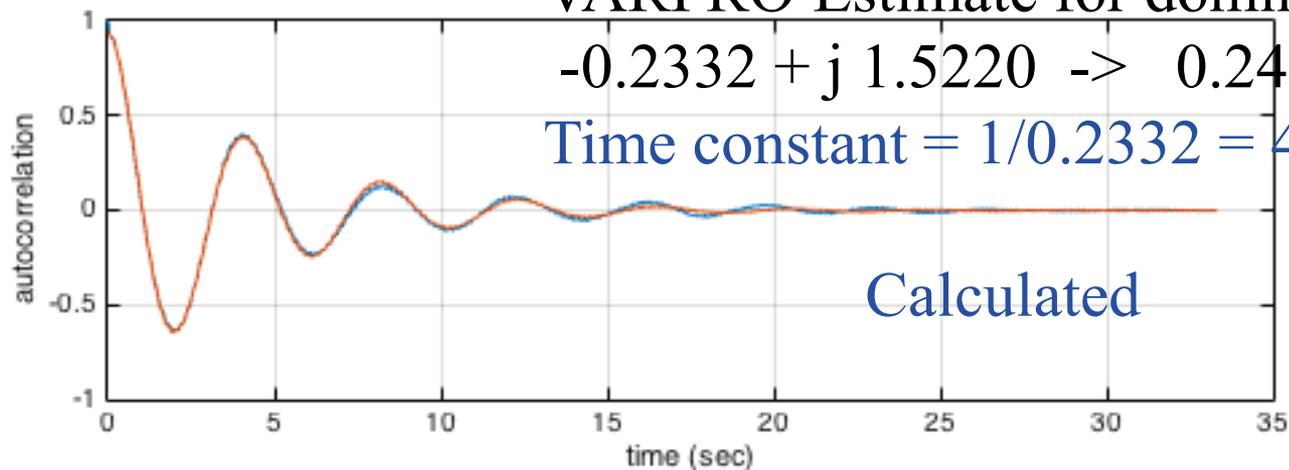
# Example (real data)

$$\Upsilon = \frac{-1}{2\sigma} + \frac{-2\sigma^6}{\sigma(\sigma^2 + \omega_0^2)(2\sigma^2 + \omega_0^2)^2}$$



VARPRO Estimate for dominant mode exponent  
 $-0.2332 + j 1.5220 \rightarrow 0.24$  Hz at 15% damping

Time constant =  $1/0.2332 = 4.29$  seconds

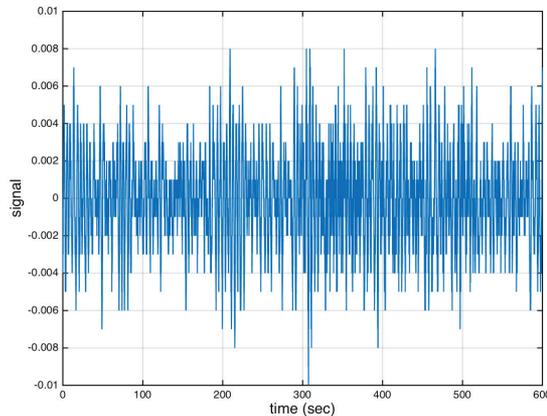


$$\Upsilon = 2.20$$

$$2\Upsilon = 4.40$$

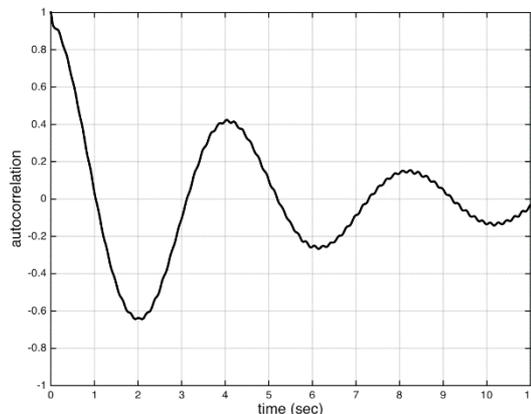
# Mode Estimation via Curve Fitting

- Apply VARPRO **curve-fitting** technique to modal analysis of ambient data.



The “easy” curve is the autocorrelation of the random-looking signal.

This auto correlation may be analyzed using model-fitting (Yule-Walker, subspace methods, etc.) or curve fitting techniques.



Our approach uses curve-fitting.



# Summary: Results for past year

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- **Added Persistence Measure to real-time monitoring.**
- **Added First-turn relative damping estimate.**
- **Under-the-hood improvements to algorithms** (calibrating finite window-based calculations)
- **Implemented in BPA real-time phasor measurement laboratory.**
- **Produced initial papers on our methods**
  - Lesieutre, B.C. and S. Roy, “A System Response Persistence Measure for use in Ambient Data Monitoring,” to be presented at the 2017 North American Power Symposium.
  - Roy, S, and B.C. Lesieutre, “A Sample-Autocorrelation-Based Approach for Monitoring Power-System Damping from Ambient Synchrophasor Data,” to be presented at the 2017 North American Power Symposium



# Modemeter

Genessee-MiraLoma

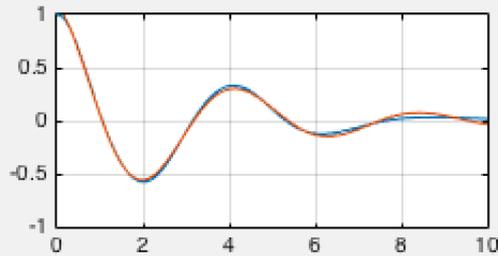


03/14/2017  
06:02:00

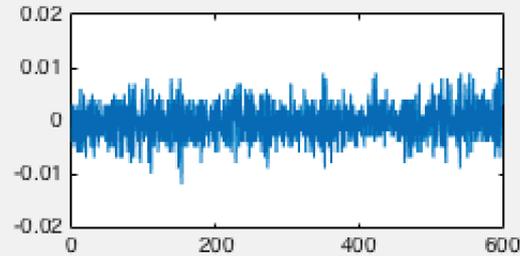
Get New Data

Pause

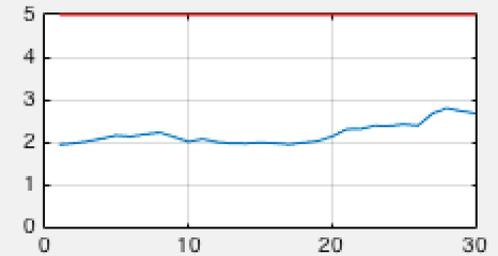
Autocorrelation and Fit



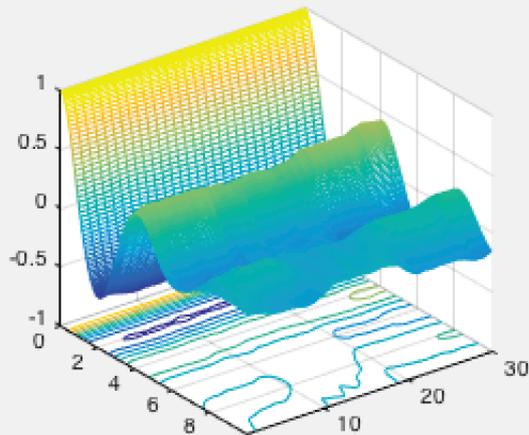
Signal



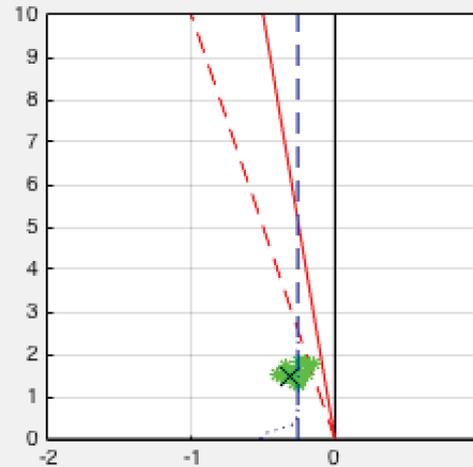
Persistence Measure



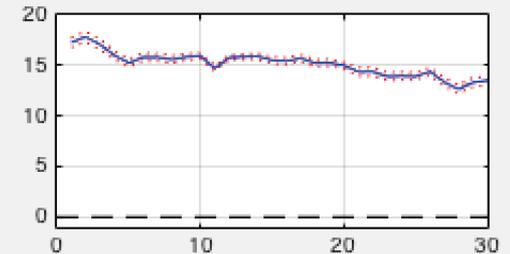
Autocorrelation History



S-Plane



First-Turn Percent Damping



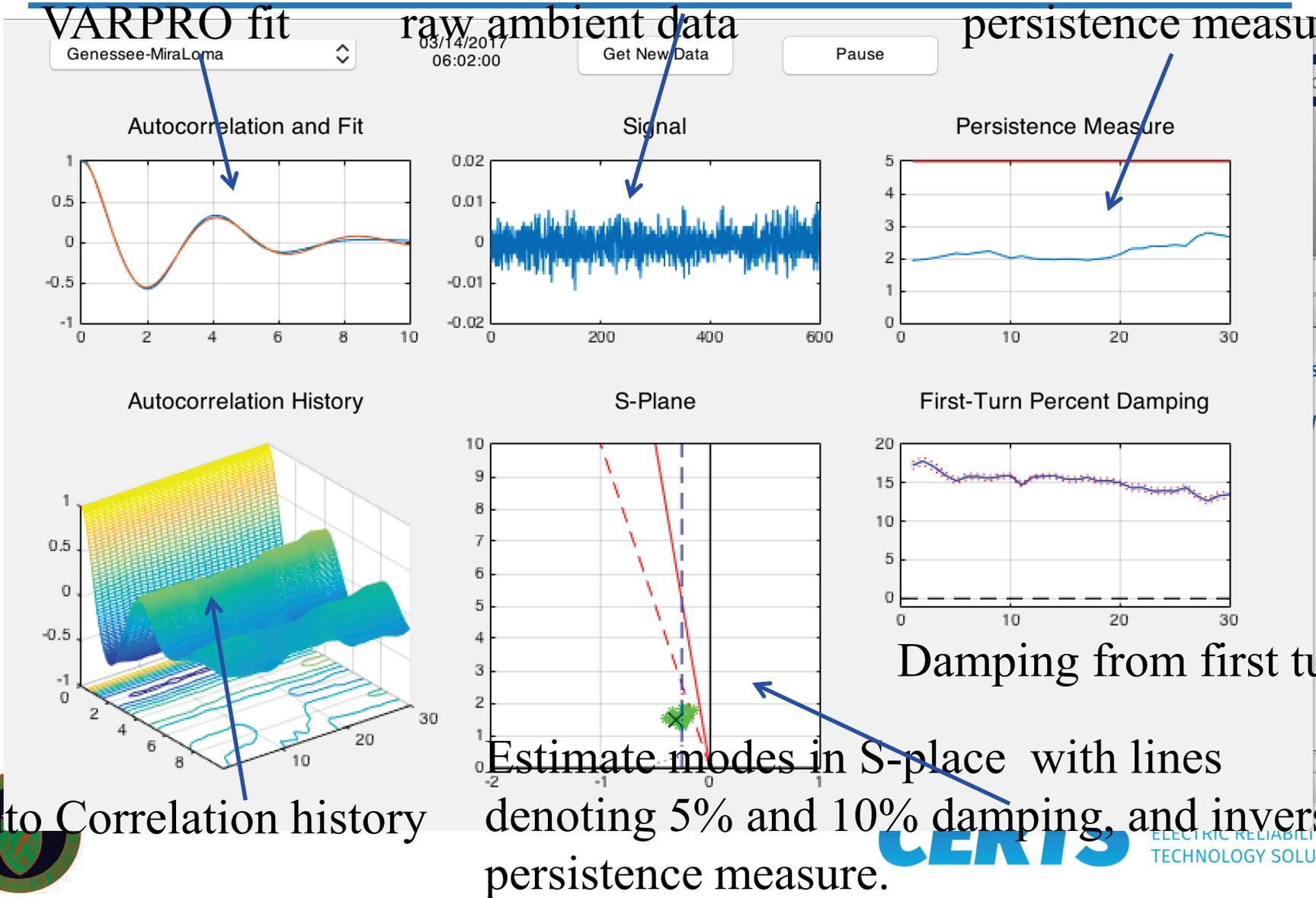
# Modemeter

Autocorrelation and

VARPRO fit

raw ambient data

persistence measure.



Auto Correlation history

Estimate modes in S-plane with lines denoting 5% and 10% damping, and inverse persistence measure.

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# Looking Forward

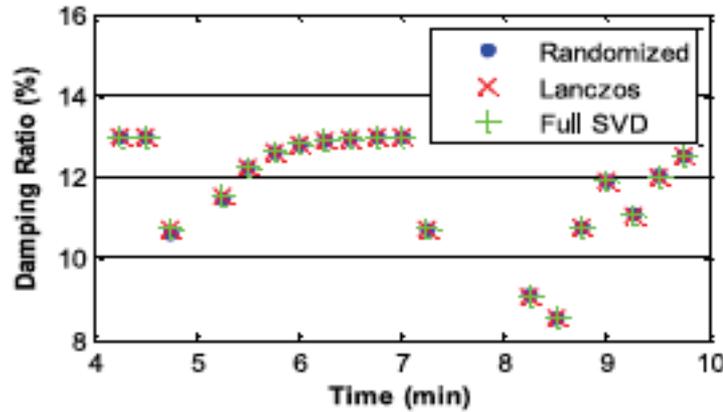
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Some technical things

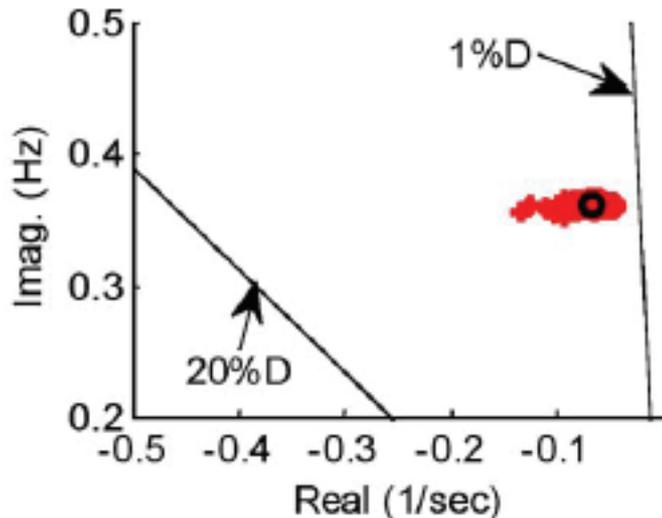
- Frequency-domain form of metric, and variants.
- Multiple signals
- More testing
- More publishing
- **Technology Transfer**



# Background: Monitoring Damping



Wu et al. IEEE Transactions on Smart Grid, May 2017



Yule-Walker method

Subspace method

**Accurately and consistently estimating damping is difficult using ambient data**



Trudnowski et al., IEEE Transactions on Power Systems, May 2008