

Reduced Order Models of Distribution Dynamics with Application to FIDVR

Scott Backhaus
LANL

Michael Cherkov (LANL), Soumya Kundu (LANL), Charlie Ducult (École Normale Supérieure), Vladimir Lebedev (Landau Institute), Inrina Stolbova (Moscow Institute of Physics)

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Program Overview

Partners: LANL, Cal Tech, Columbia, and U. of Michigan

Collaborators: MIT, Landau Institute, ENS-Paris, NICTA-Australia, Moscow Inst. of Physics, U. of Washington,...

Research Areas

- Power System Control Under Uncertainty
 - *Chance-Constrained Optimal Power Flow (LANL, Columbia, Michigan)*
 - *Distributed Control of Load for Frequency Control (Cal Tech, LANL)*
- Transmission Effects of Distribution Grid Dynamics
 - *PDE Models of Distribution Dynamics (LANL, Michigan, Landau Institute, ENS-Paris)*
 - *Distribution Dynamics Model Reduction (LANL, Michigan)*
- Coupled, Interdependent Infrastructures—Gas-Grid Coupling
 - *Stochastic Temporal Dynamics of Coupled Power and Gas Systems (LANL)*
 - *Coupled Gas-Grid Reliability, Operations, and Design (LANL, NICTA-Australia, MIT)*

Outreach

- *Winter School 2015—January 15-17*
- *Winter Conference 2015—January 18-19,*

Outreach

Winter School (Jan 15-17, 2015)

- 9 X 2-hour lectures from experts in Distributed Control, Optimization, and Stochastic Methods
 - Focused on graduate students and postdocs
 - Application of these methods to grid control, design and optimization
-
- Ian Hiskens (Michigan)
 - Florian Dorfler (UCLA/ETH)
 - Steven Boyd (Stanford—not confirmed)
 - Daniel Bienstock (Columbia)
 - Steven Low (Cal Tech)
 - Pascal vanHentenryck (NICTA-Australia)
 - Antonio Conejo (Ohio State)
 - Duncan Callaway (UC Berkeley)
 - Konstantin Turitsyn (MIT)

Winter Conference (Jan 17-18, 2015)

16 invited presenters

- Ian Dobson (Iowa State)
- Seth Blumsack (Penn State)
- Paul Hines (Vermont)
- David Hill (Sydney)
- Bernie Lesieutre (Wisconsin—TBD)
- Javad Lavaei (Columbia)
- Krishnamurthy Dvijotham (Washington/Cal Tech)
- Chris DeMarco (Wisconsin—TBD)
- Alejandro Dominguez-Garcia (Urbana)
- Goran Andersson (ETH)
- Jakob Stoustrup (PNNL)
- Shmuel Oren (UC Berkeley)
- P.R. Kumar (Texas A&M)
- Eugene Litvinov (ISO-NE)
- Janusz Bialek (SkTech)
- Michael Ferris (Wisconsin)

Context/Vision—Distribution Dynamics

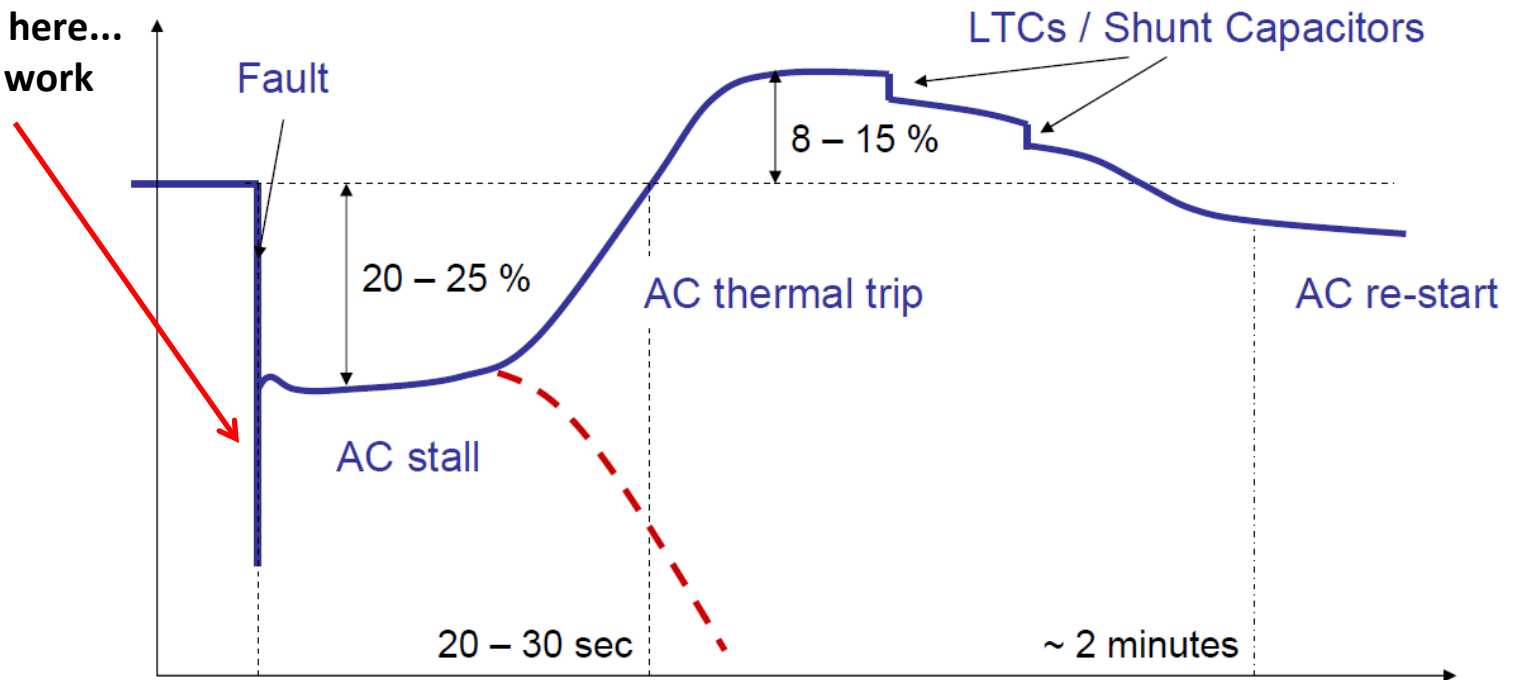
- *Existing dynamical simulations of high voltage transmission grids typically use:*
 - *detailed models of generators and transmission*
 - *simplified aggregate models of loads that do not account for the complex spatiotemporal interactions of the loads*
- *The need for better dynamical load models*
 - *Encroaching on stability boundaries—Impact of load dynamics is growing*
 - *Collective, nonlinear (and undesired) dynamical load behaviors (FIDVR) driven by typical transmission grid behavior, e.g. normal fault clearing.*
 - *Deployment of active consumer loads will yield new “load” dynamics.*
- *Our approach*
 - *Model/Understand the complex spatiotemporal interactions of loads*
 - *Develop low-dimensional representations suitable for simulations of transmission dynamics*

Presentation Outline

- Project Purpose—Develop understanding of FIDVR dynamics (and other complex distribution dynamics) and fast/simple models for integration into transmission simulations
- Significance and Impact—Improved understanding of the effect of complex load dynamics on transmission dynamical stability without significant increase in computational burden
 - FIDVR Example—What are the dynamics under consideration?
- Technical Approach
 - Distribution Dynamics Model
 - Analysis of Dynamics—Comparison with related work
 - Model Uncertainty—Inclusion of Disorder
- Technical Accomplishments
 - FIDVR critical clearing time
 - Effects of disorder/load uncertainty
 - Low-Dimensional Models
- Conclusions
- Future Work

Significance and Impact—FIDVR Example

Induction motor stalling
dynamics occurs here...
Focus of current work

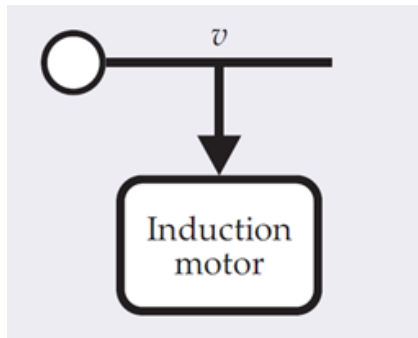


Related work in this general area

- PNNL—statistical model of stalling and thermal tripping
- Iowa State—statistical model of stalling with power flows
- LBNL/ASU/SEL—PSCAD and RTDS simulation of stalling dynamics

Technical Approach—Distribution Dynamics Model

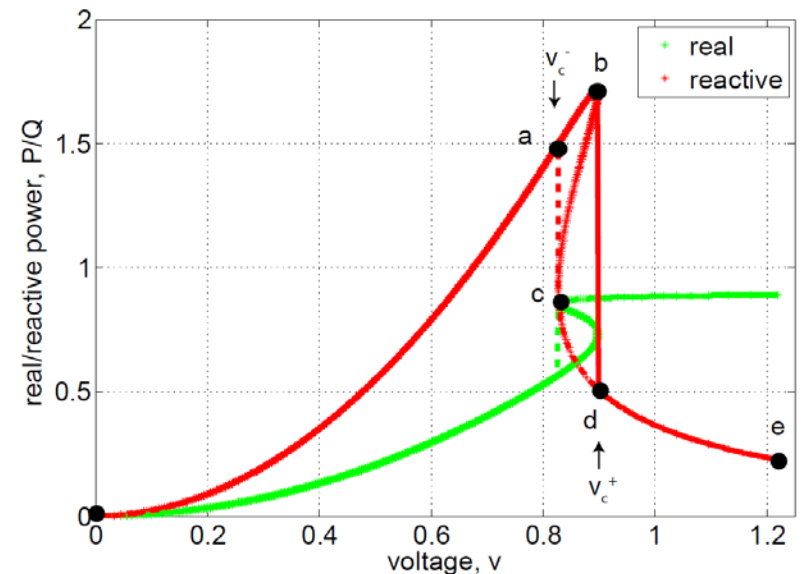
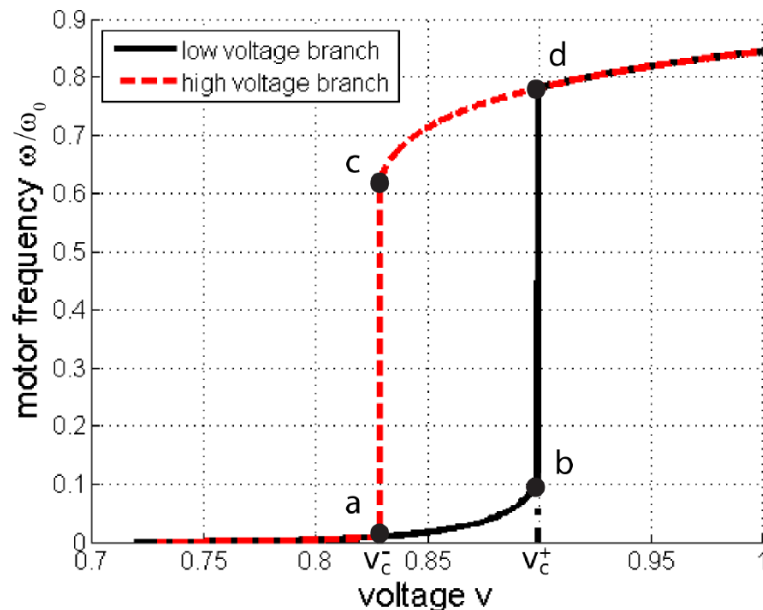
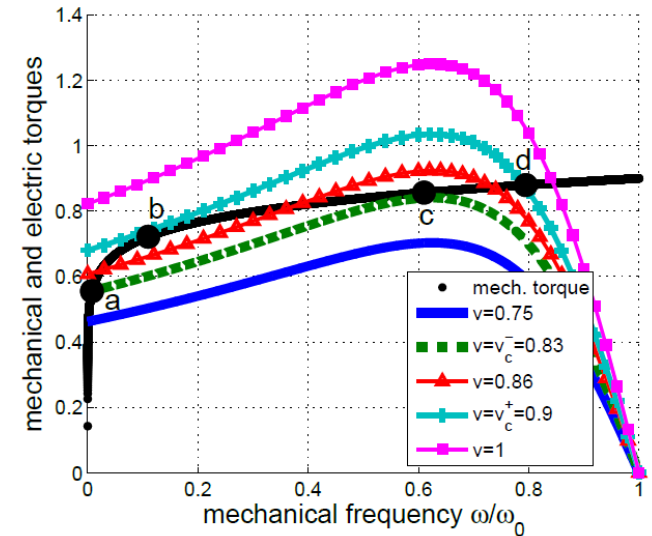
Induction Motor Dynamical Model



$$\mu \frac{d}{dt} \omega = \frac{p}{\omega_0} - t_0 \left(\frac{\omega}{\omega_0} \right)^\alpha,$$

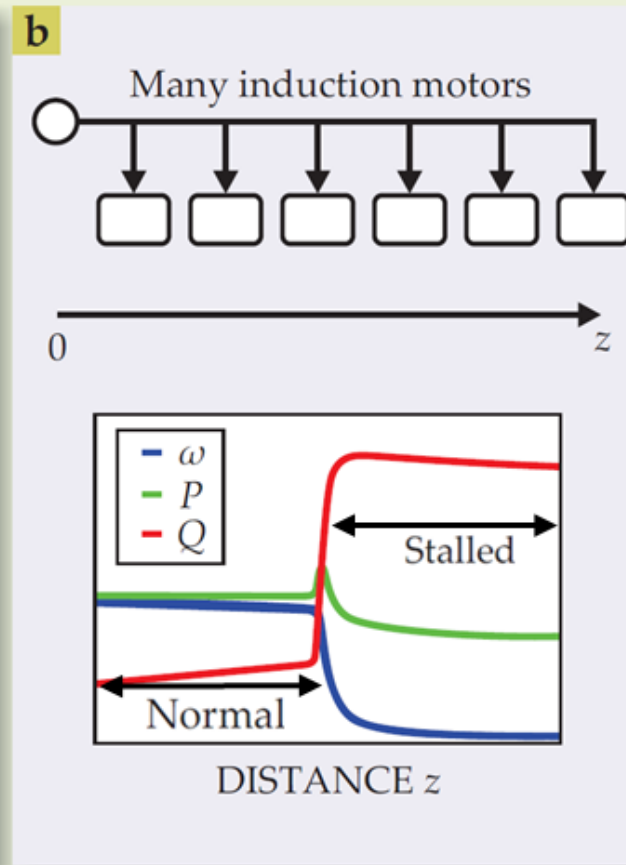
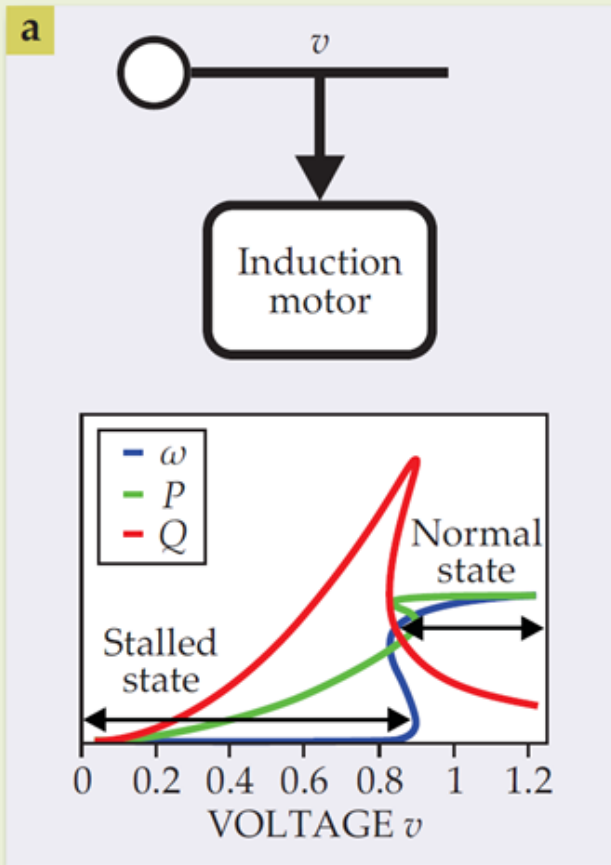
$$p = \frac{s r_m v^2}{r_m^2 + s^2 x_m^2},$$

$$q = \frac{s^2 x_m}{r_m^2 + s^2 x_m^2} v^2.$$



Technical Approach—Distribution Dynamics Model

Spatially Continuous Power Flow



Power flow equations

$$\partial_z \rho = -p - r \frac{\rho^2 + \phi^2}{v^2},$$

$$\partial_z \phi = -q - x \frac{\rho^2 + \phi^2}{v^2},$$

$$\partial_z v = -\frac{r\rho + x\phi}{v}.$$

Motor dynamics

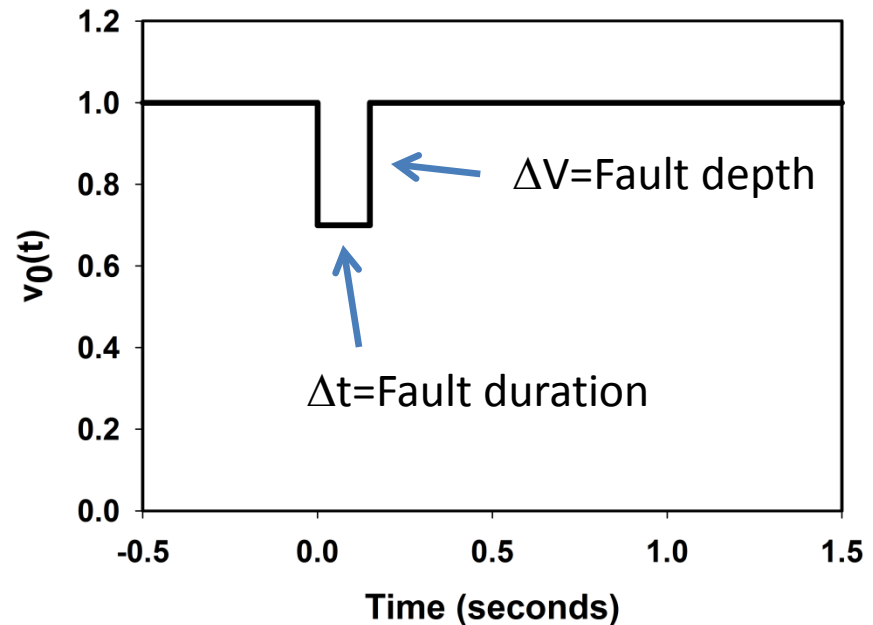
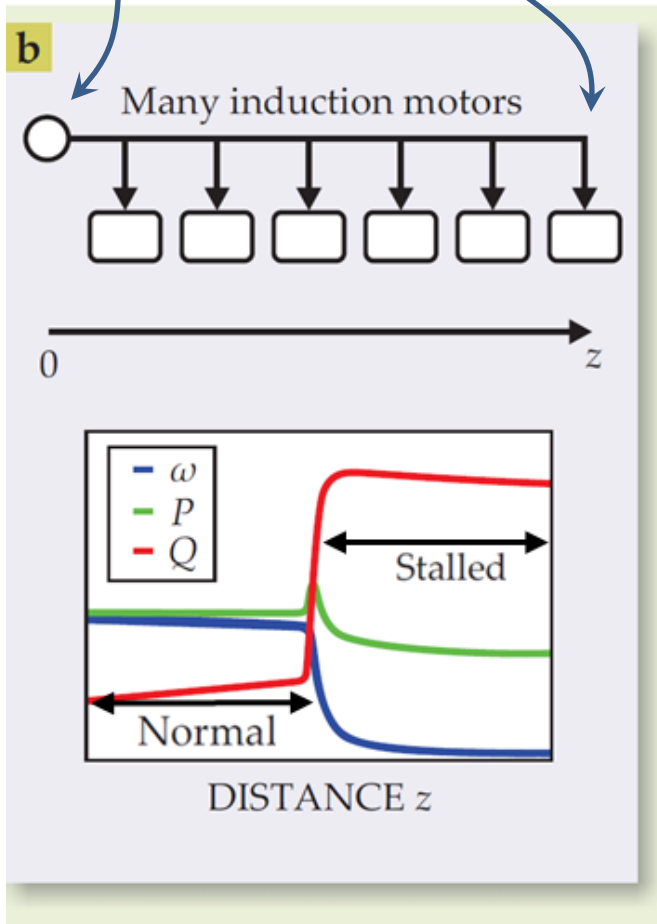
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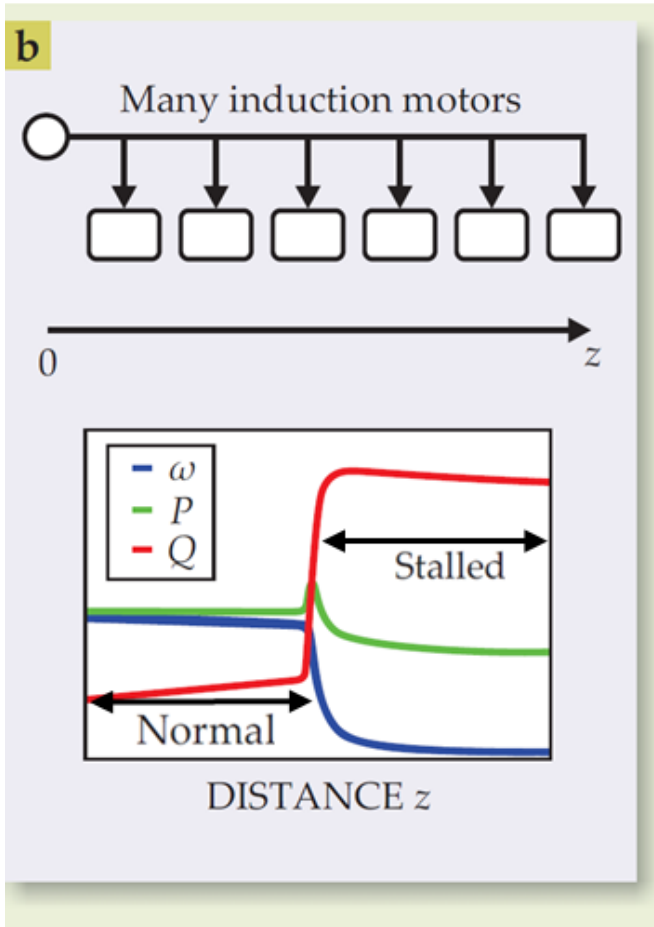
Technical Approach—Distribution Dynamics Model Boundary and Initial Conditions

$$v(0) = v_0, \quad \rho(L) = \phi(L) = 0$$



- Using “simplified” boundary conditions that do not include transmission impedance
- Separates the distribution dynamics from quasi-static transmission impedance effects
- Impedance is included during integration into transmission simulations

Technical Approach—Model Uncertainty

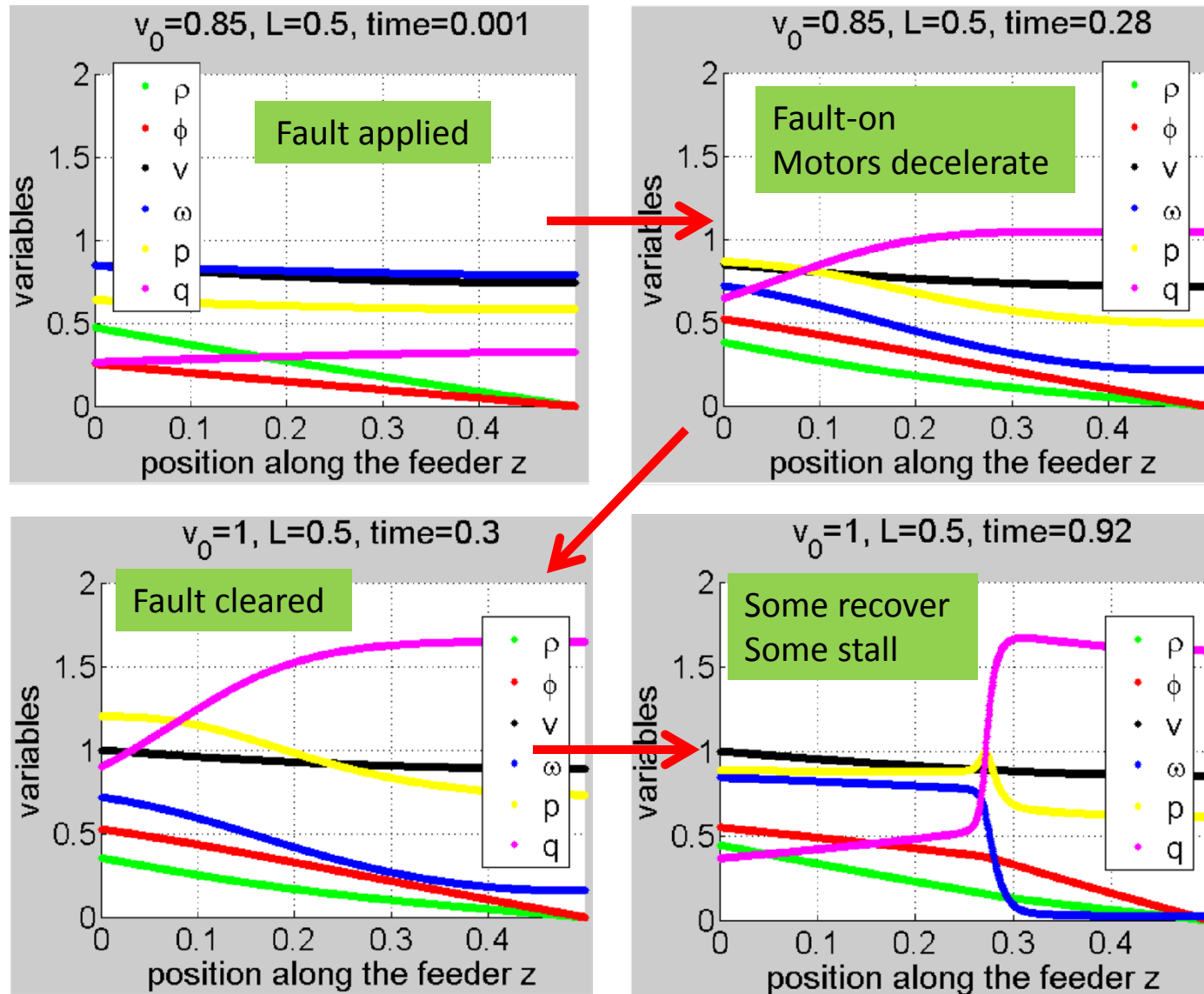


- Distribution circuit load composition is not very well known
- We account for this in general way by including randomness in load parameters
- Example: Uncertainty in motor loading

$$\delta(z) = \tau_0(z) - \bar{\tau}_0$$

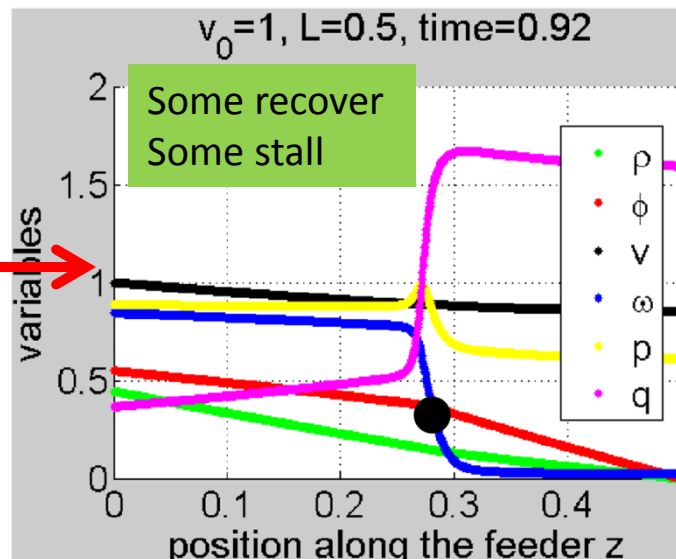
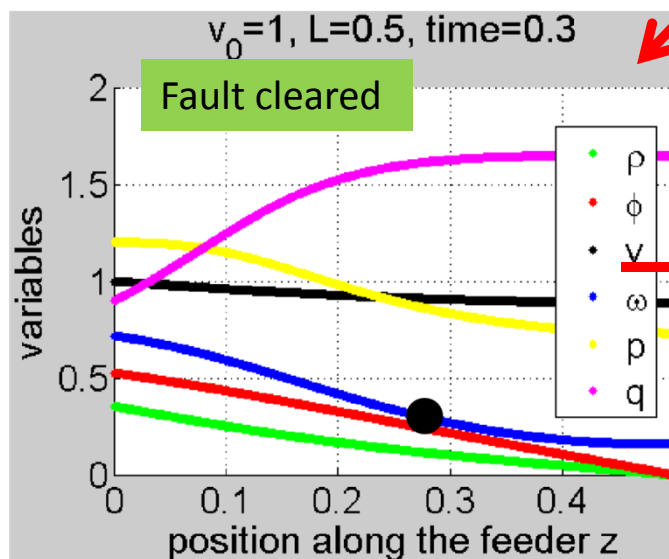
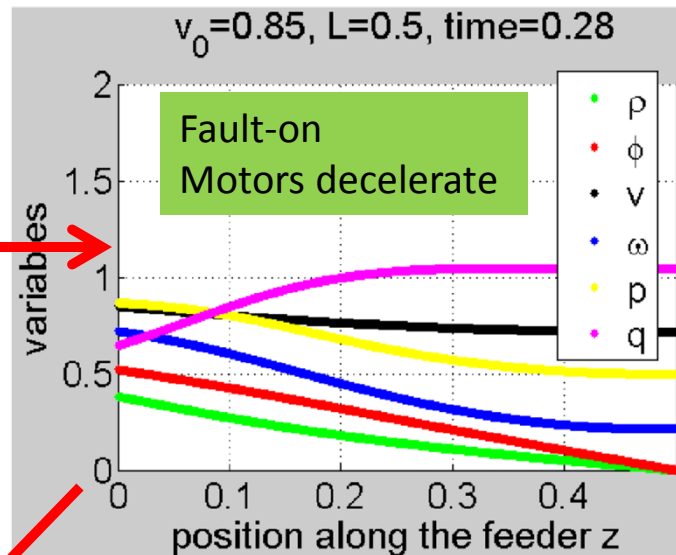
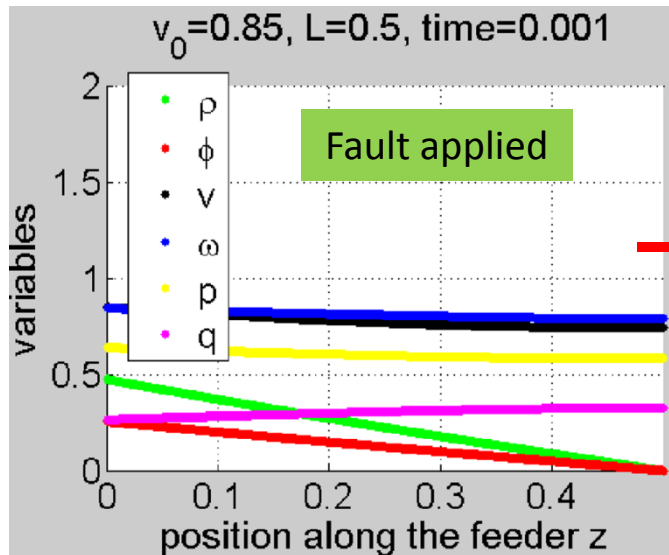
$$\mathbb{E} [\delta(z_1)\delta(z_2)] = (\tau_0\Delta)^2 \exp(-|z_1 - z_2|/z_d)$$

Technical Approach—Analysis of Dynamics Spatiotemporal Interaction of Load Dynamics



Technical Approach—Analysis of Dynamics

Final Location of Normal/Stalled Interface— $T_{\text{net}}=0$

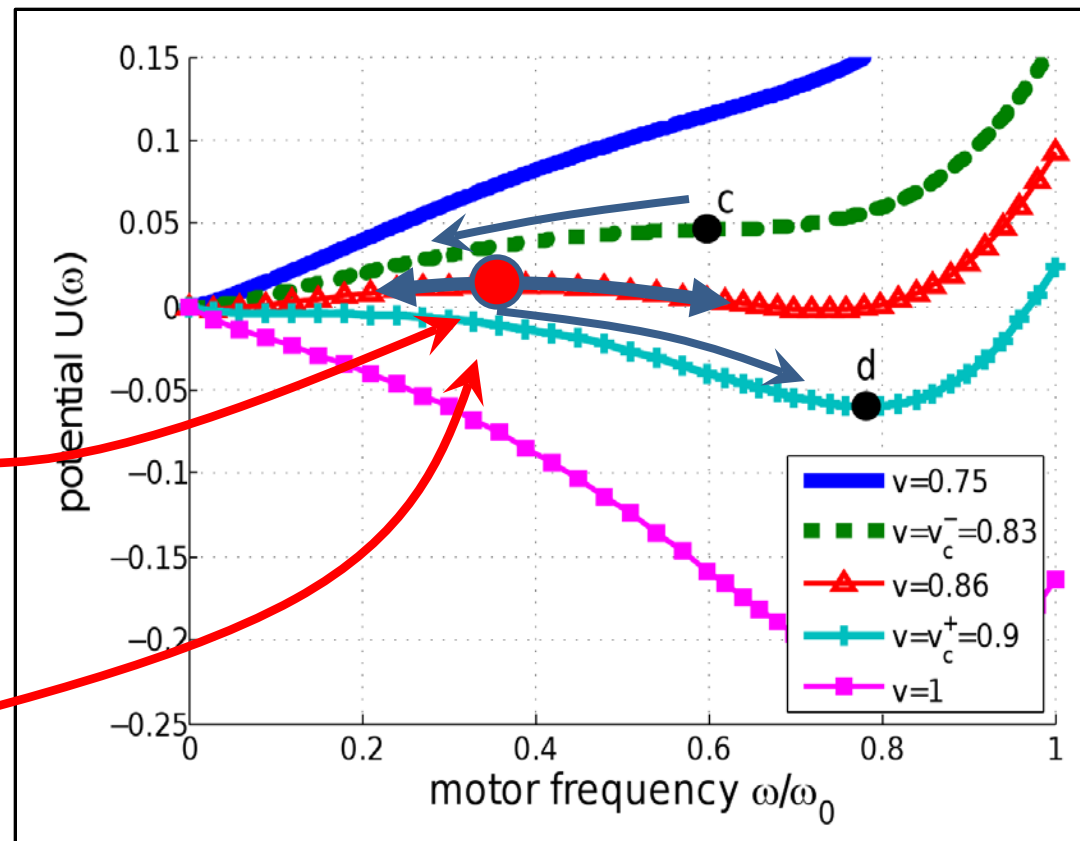
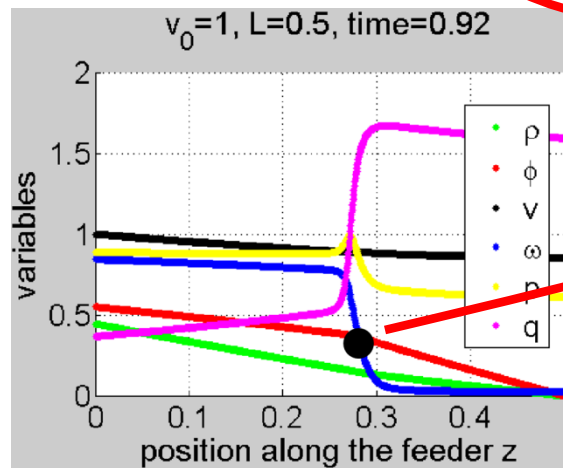
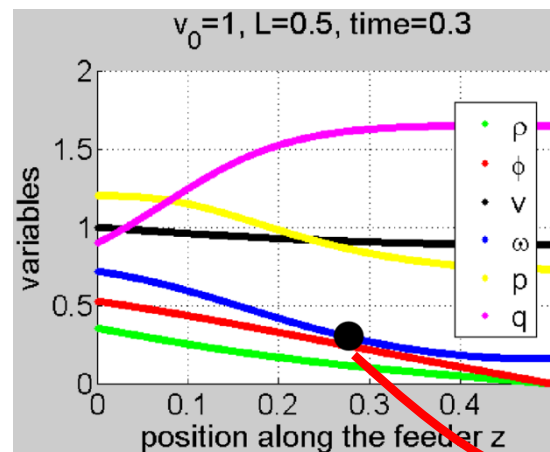


Technical Approach—Analysis of Dynamics

Energy Function—Frozen Voltage

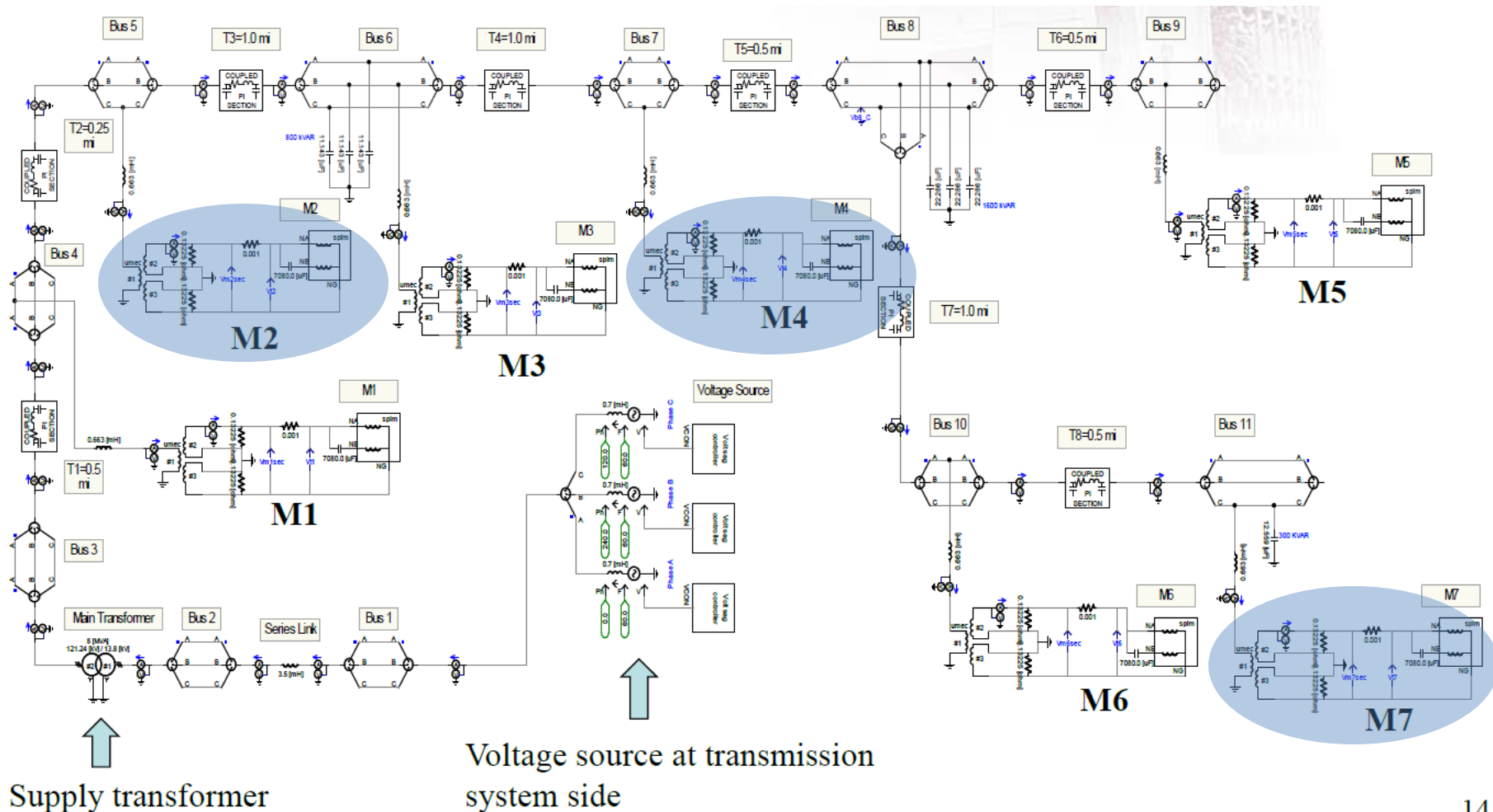
Post-fault voltage determines energy landscape

Post-fault motor angular speed determines final motor state



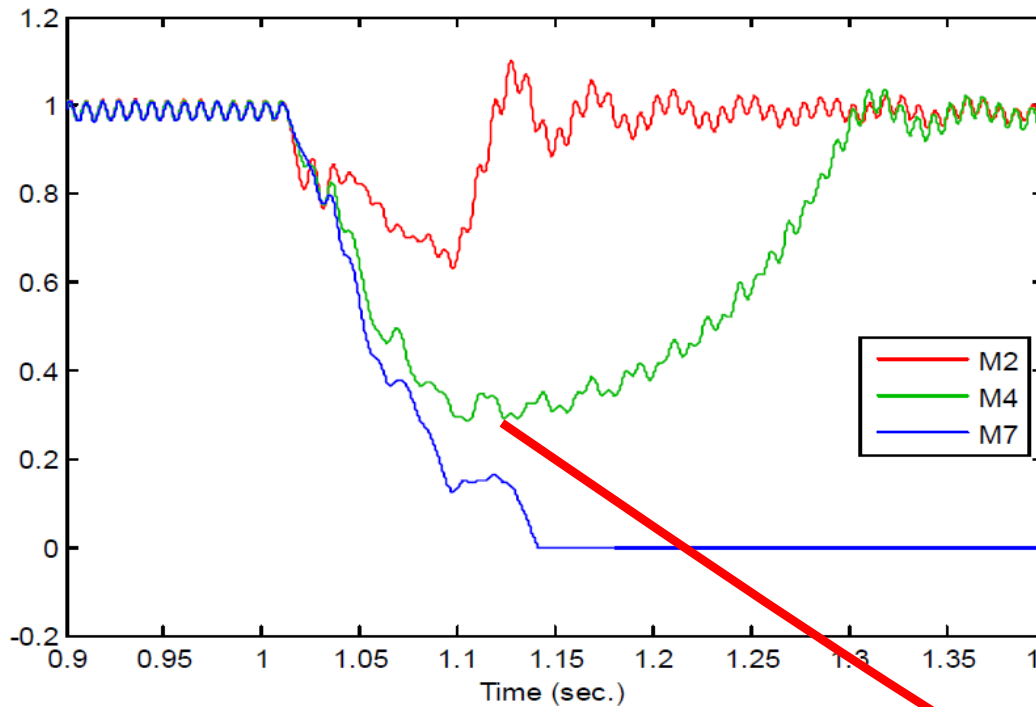
Technical Approach—Comparison to Related Work

PSCAD Model of Motors and Distribution Circuit (ASU)



Technical Approach—Comparison to Related Work

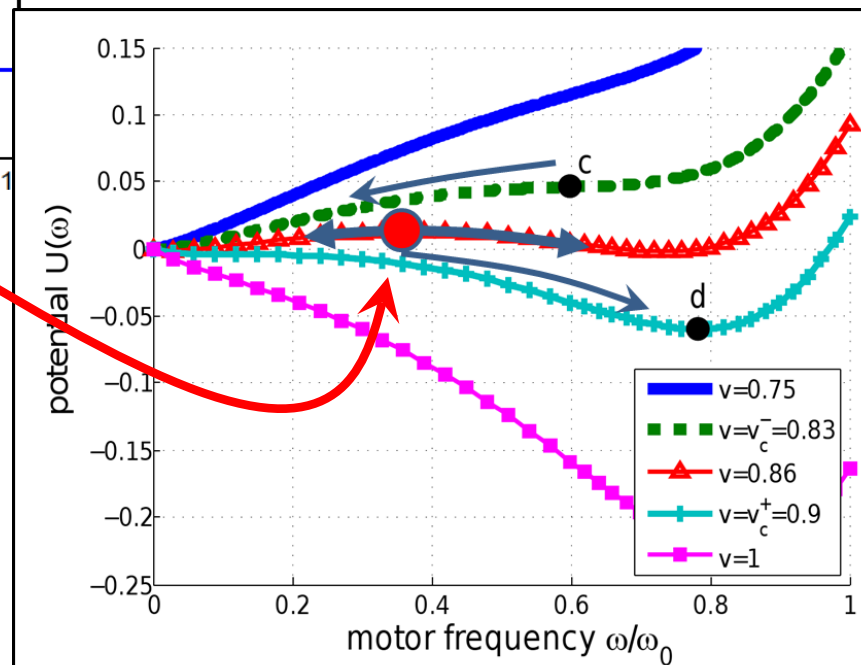
PSCAD Model of Motors and Distribution Circuit



Dynamics of PSCAD model are consistent with our continuum power flow/phasor dynamics model

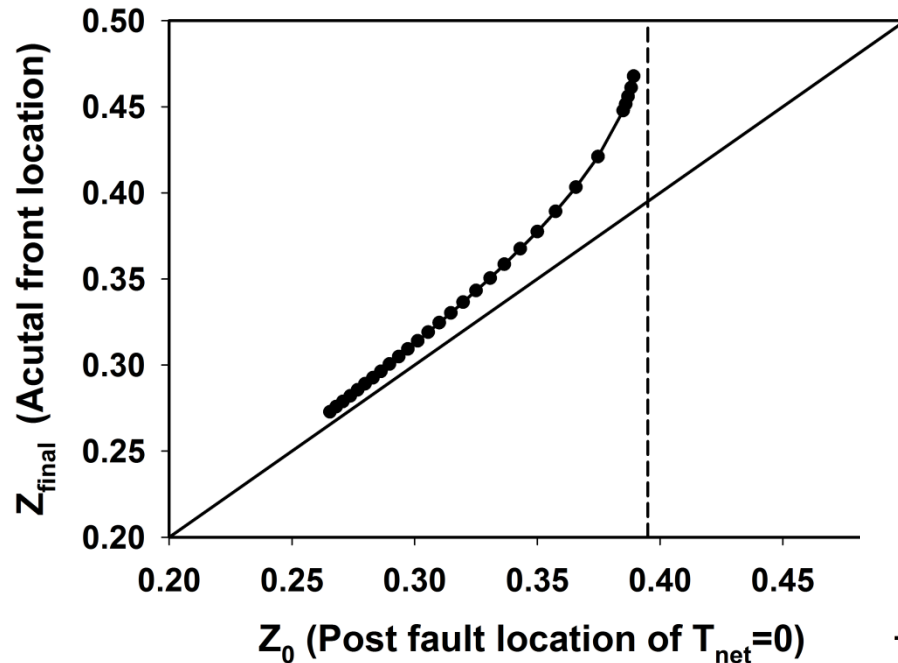
PSCAD model accounts for:

- Motor electrodynamics
- Angle dependent torque
- Resolves AC cycle
- Fault relative to AC phase

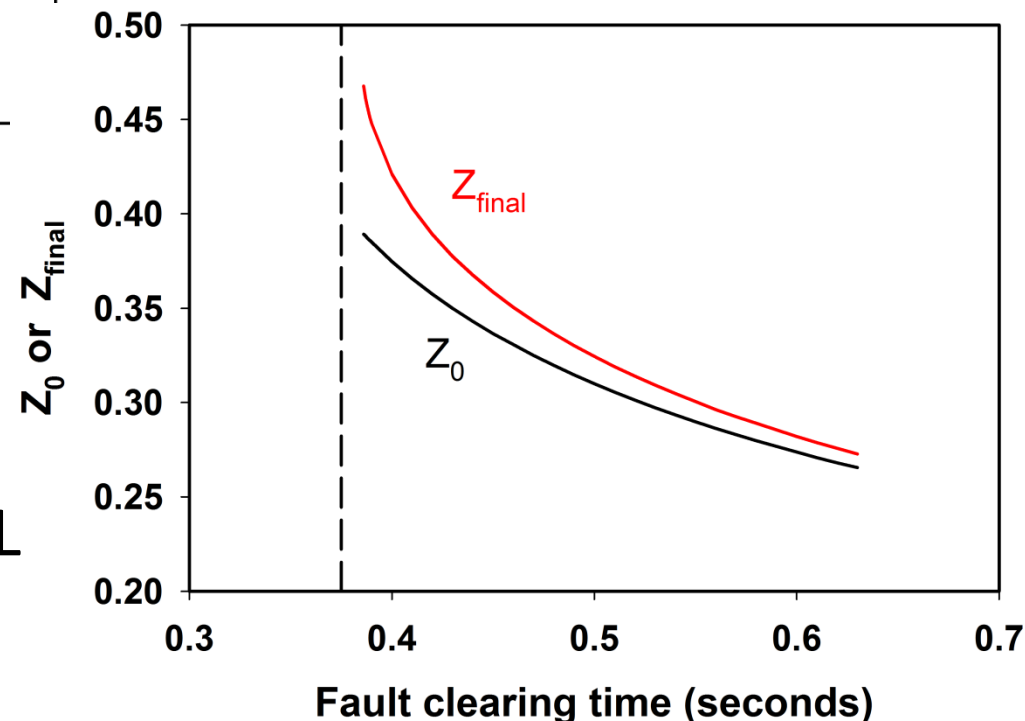


Technical Approach—Analysis of Dynamics

Accuracy of the $T_{\text{net}}=0$ Condition

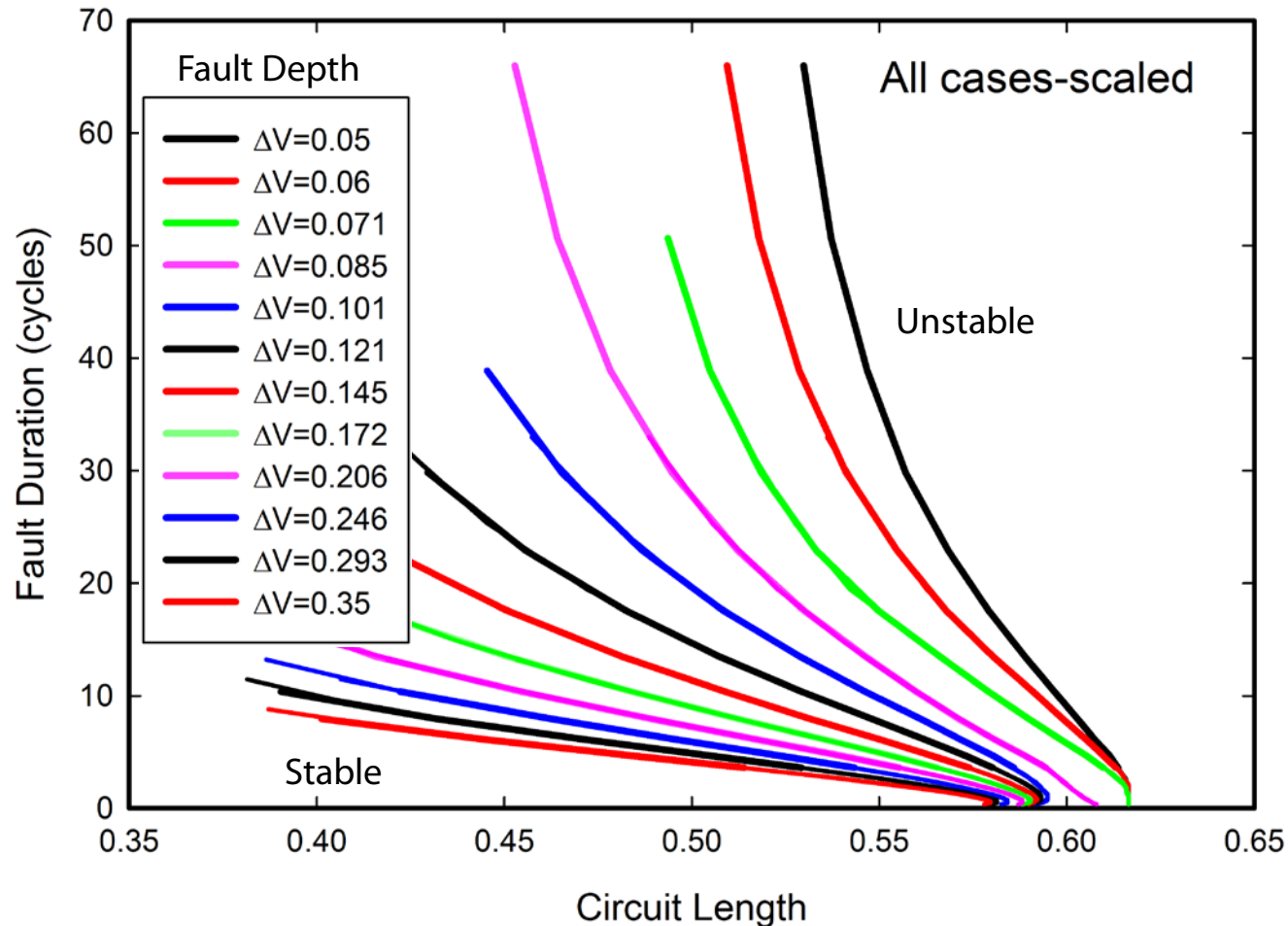


- $T_{\text{net}}=0$ condition provides a conservative estimate of
 - Final front location
 - Critical clearing time

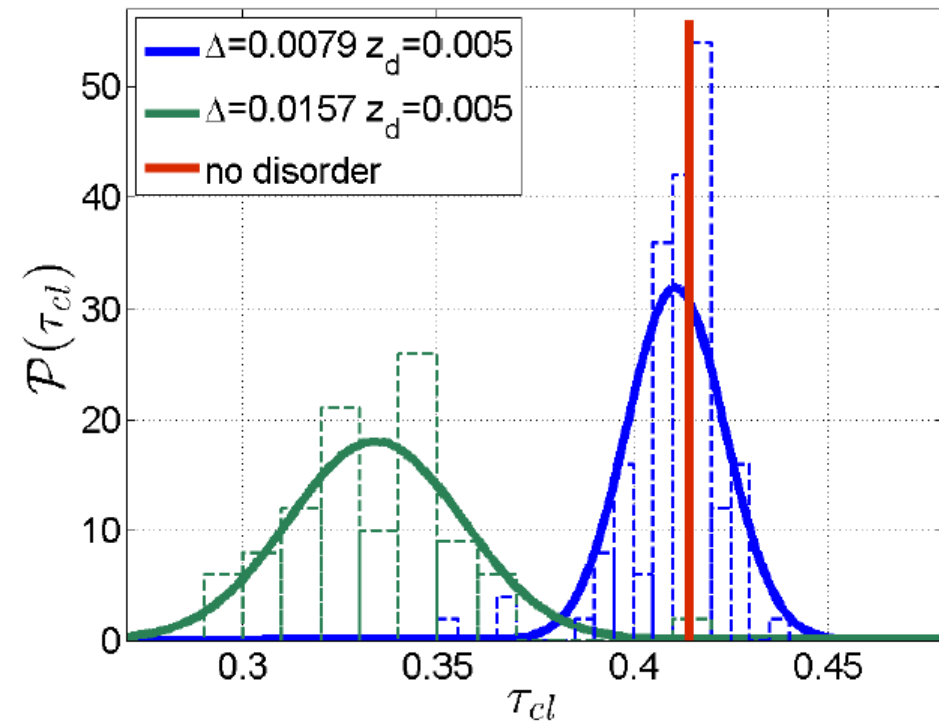


- Condition becomes less accurate as Z_0 approaches L
 - Finite size effects

Technical Accomplishments—Critical Clearing Time Computed Using the $T_{\text{net}}=0$ Condition



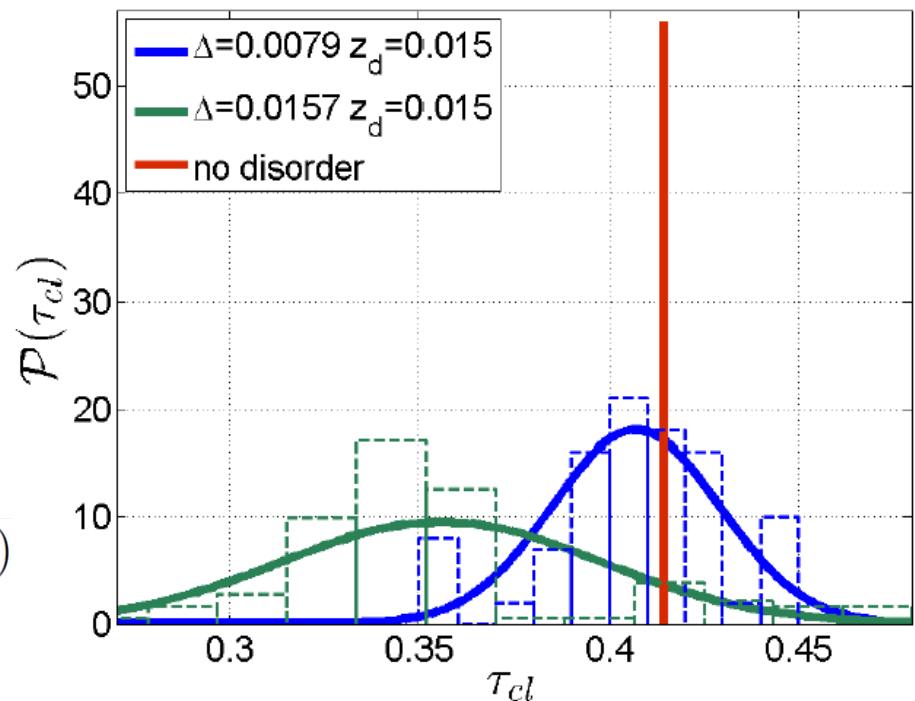
Technical Accomplishments—Effects of Model Uncertainty—Distribution of Critical Clearing Times



$$\delta(z) = \tau_0(z) - \bar{\tau}_0$$

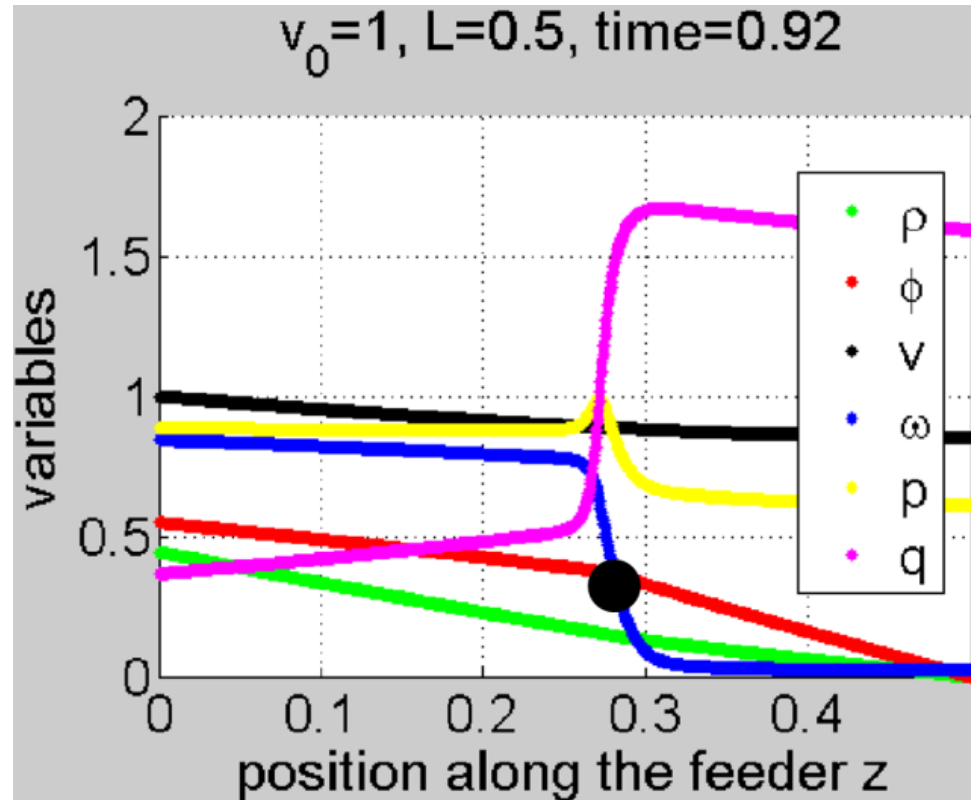
$$\mathbb{E}[\delta(z_1)\delta(z_2)] = (\tau_0\Delta)^2 \exp(-|z_1 - z_2|/z_d)$$

- Distribution circuit load composition is not very well known
- We account for this in general way by including randomness in load parameters



Technical Accomplishments—Low-Dimensional Models—Path Forward

- Normal/Stalled interface is the salient low-dimension feature the dynamics.
- Approximately constant motor speed ω on either side of the front
- Front location can be predicted based on $T_{\text{net}}=0$ point
- Algebraic relationships for pre/post-fault P and Q



Conclusion

- Developed a continuum power flow/phaser motor dynamics of distribution dynamics
 - Captures the salient features of FIDVR dynamics—comparable to PSCAD models
 - Used energy arguments to improve the understanding of the spatiotemporal aspects of induction motor stalling and FIDVR
 - Computed critical clearing times for one “class” of distribution circuit
 - Quantified the effect of load uncertainty on critical clearing times

Future Work—FY15

- Extension to a wider range of circuits, loading and fault conditions to understand its accuracy
 - GridLabD distribution circuit taxonomy
 - transmission line impedance
- Leverage the normal/stalled front for a low-dimensional model of the dynamics
- Investigate higher-order collective effects/interactions:
 - FIDVR cascading between circuits in a substation
 - FIDVR cascading to adjacent substations
 - Integrate reduced-order models into transmission simulations
- Validation on real-world event data
- Extend to smart/active load dynamics

Acknowledgements/Contacts

Contact:

Scott Backhaus

[*backhaus@lanl.gov*](mailto:backhaus@lanl.gov)